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# PRACTICAL PHYSICS

( For First Year T. D. C. Students )

By

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## **INTRODUCTION**

The keen desire for experimentation and keen sense of observation lead a student of science to learn things thoroughly and sometimes to reveal the secrets of nature. A student of physics is required to be more skilled in performing experiments and more analytical in interpreting his results. Inside the laboratory a student is required to be perfectly disciplined to have the maximum advantage of the facilities available to him.

Laboratory is the sacred place of learning and it contains things which are our national property meant to be used by students in their turn. One should know about the use of every piece of apparatus before he handles it otherwise there is every possibility of spoiling or damaging it and such losses we are ordinarily unable to afford.

In the present pattern of science education in our country where number of students are increasing and the laboratory facilities are limited; a student is required to make the best use of the opportunities available to him. Inside the laboratory one is required to have the keen sense of fellow feeling amongst his class-fellows, obedient to his instructors and generous to lab-bearers. To have the full benefit of his laboratory opportunity, he is required to organise his working as follows:-

- (a) Preparation outside the laboratory.
- (b) Performance of an experiment.
- (c) Recording.

**Preparation outside the laboratory**—As a practice, generally, students are given a laboratory programme in advance at the beginning of every academic session which has to be followed rigidly by every student in order to complete his practical work usefully in time. Of course, sometimes, it becomes inevitable to re-adjust it due to certain unavoidable reasons and students are required to take the due notice of such changes in their own interest.

As every student is aware of the fact that he has to perform a certain experiment on fixed date. He is, therefore, required to

prepare for the experiment before hand. It is that a student should be very inquisitive to understand of performing a certain experiment. This inquisitiveness naturally, lead him to think about the experiment of his inquisitiveness he will read the principles. Its practical realization will make him aware of the apparatus required and its particular use. He should be keen to know the limitations of his apparatus and how the result can be affected.

To prepare for an experiment every student should have an extra exercise-book, in which he should write down the formula to be used, explaining the symbols after understanding the relevant theory. A neat diagram and observations should also be already made by him. If he has got some observations which he does not understand, he must clear them with the help of his teacher. To ensure proper preparation the teacher should put some questions to the students. This practice decisively, will give better results.

**Performance of an experiment**—As soon as a student has been admitted to perform a certain experiment in the laboratory, he should collect all necessary apparatus for that experiment and arrange them in a planned manner. After ascertaining that the apparatus is in the working order, one should immediately proceed to perform the experiment and take all the observations in a pre drawn tabular form. He should take as many observations as he can take conveniently during the allotted time. If any piece of apparatus is found to be not in the working order, or if a certain discrepancy is observed in the different sets of observations, the matter should be brought to the notice of the teacher.

If any apparatus is damaged or lost by a student, it should also be immediately reported to the teacher concerned. The damage can be replaced by the other apparatus. If certain mistakes are observed in the observations taken, then they should be struck off by drawing a line over them and fresh readings should be taken.

After completing the experiment, calculation should be finished in the laboratory itself and the result obtained should be communicated to the teacher. On his approval the result should be recorded in the well bound practical book.

For calculation purposes, one should know how to use trigonometrical tables, log tables, square and square root tables, reciprocal tables etc.

Sometimes the result is better interpreted in terms of graphs, therefore, plotting of graph and its interpretation should also be studied by students.

Recording—A well bound practical book is used for this purpose where right hand pages are ruled and left hand pages are plain.

The experiments whose results have been approved by the teacher should be recorded in the practical book as far as possible before performing the next experiment. The method of recording is given with each experiment described in the book but a general method is pointed out below in brief.

Experiment No.	(On the top of the ruled page)
Date	In the left hand column of the right hand side ruled page.
Object	Right side
Apparatus	Right side
Diagram or figure	Plain paper on the left side
Theory	Right side
Procedure	Right side
Observations	Right side
Calculations	Left side in neat manner
Result or interpretation	Right side
Percentage error	Right side
Precautions	Right side
Sources of error	Right side

After recording an experiment it should be produced before the teacher for examination before the next assigned experiment is started.

Use of mathematical tables—Use of mathematical tables except the log tables is simple and one can pick up their use just being properly instructed. The use of log tables need some understanding and we discuss their use in short.

The expression

$$a^n = b$$

mathematically can be written as

$$\log_a b = n$$

It is read—log of  $b$  to the base  $a$  is equal to  $n$ . For example

$$10^2 = 100$$

$$10^3 = 1000$$

can be expressed as logarithms as follows

$$\log_{10} 100 = 2$$

$$\log_{10} 1000 = 3$$

Generally for the purposes of calculations we use the log with base 10 and four figure tables. Log tables are useful to perform multiplication, division, evolution and involution. The basic rules of these operations with the logarithmic system are—

$$\text{If } x = abc$$

$$\text{Then } \log x = \log abc \\ = \log a + \log b + \log c \quad \dots\dots(1)$$

$$\text{If } y = \frac{c}{d}$$

$$\text{Then } \log y = \log \frac{c}{d} \\ = \log c - \log d \quad \dots\dots(2)$$

$$\text{If } x = a^n$$

$$\text{Then } \log x = \log a^n \\ = n \log a \quad \dots\dots(3)$$

$$\text{If } y = \sqrt[m]{b}$$

$$\text{Then } \log y = \log \sqrt[m]{b}$$

$$= \frac{1}{m} \log b \quad \dots\dots(4)$$

It is understood that base in all these expressions is 10. Obviously the multiplication and division are reduced respectively to the addition and subtraction of the logarithmic values. To find the result antilog tables are to be considered.

To find log of a quantity—it consists of two steps—(i) to write the characteristic, and (ii) to write the mantissa. Characteristic has to be written on the basis of understanding.

(i) In case of quantities greater than one, characteristic is one less than the number of digits. For example, characteristics of 4739, 473·9, 47·39 and 4·739 are 3, 2, 1 and 0 respectively.

(ii) In case of quantities less than one the characteristic is negative and it is numerically one more than the number of zeros following the decimal point on the right side. The negative nature of the characteristic is represented by the small horizontal line over the number expressing the characteristic. For example, characteristics of 4739, 473·9, 004739, 0004739 are respectively  $\overline{1}$ ,  $\overline{2}$ ,  $\overline{3}$ , and  $\overline{4}$ .

**Determination of mantissa**—In fact log tables are used to determine mantissa. For all the numbers from 4739 . . . 0004739 the mantissa is the same and independent of the decimal point. First we locate the first two digits in the first vertical column. In our example we locate 47 and then in the horizontal to column of 47 we note down the number below the third digit. Here we shall note down the number below 3 which is 6749 and then to this number we add the number given in the mean difference column below the fourth digit 9 in the horizontal column of 47. This number is 8 from the log table. Therefore, the mantissa for 4739 is ( $6749 + 0008 = 6757$ ). When mantissa is known, it is combined with the characteristic to get the log of that quantity.

The following examples further explains the process of getting log for a quantity —

S. No.	Quantity	Characteristic	Mantissa (from log table)	log of the quantity
1	4739·0	3	$6749 + 0008 = 6757$	$3\cdot6757$
2	473·9	2	6757	2·6757
3	47·39	1	6757	1·6757
4	4·739	0	6757	0·6757
5	·4739	$\overline{1}$	6757	$\overline{1}\cdot6757$
6	·04739	$\overline{2}$	6757	$\overline{2}\cdot6757$
7	·004739	$\overline{3}$	6757	$\overline{3}\cdot6757$
8	·0004739	$\overline{4}$	6757	$\overline{4}\cdot6757$
9	·00004739	$\overline{5}$	6757	$\overline{5}\cdot6757$

**To find antilogarithm**—For this process first mantissa is used. It is very similar to the process of taking the mantissa of a quantity. First in the antilogarithm table the first two digits of the mantissa are located and then the number in front of these

digits below the third digit are written. Finally the mean difference corresponding to the fourth digit is added to the previously obtained number. The decimal to this will be decided on the basis of the characteristic.

The following example gives the whole process.

$$Y = \frac{1000 \times 4 \times 980 \times 250}{3 \cdot 142 \times (0 \cdot 05)^2 \times 0 \cdot 062}$$

$$\log Y = \log (1000 + \log 4 + \log 980 + \log 250) - (\log 3 \cdot 142 + 2 \log 0 \cdot 05 + \log 0 \cdot 062)$$

$$\log 1000 = 3 \cdot 0000$$

$$\log 3 \cdot 142 = 0 \cdot 4972$$

$$\log 4 = 0 \cdot 6021$$

$$\log 0 \cdot 05 = \overline{2} \cdot 6990$$

$$\log 980 = 2 \cdot 9912$$

$$\log 0 \cdot 05 = \overline{2} \cdot 6990$$

$$\log 250 = 2 \cdot 3979$$

$$\log 0 \cdot 062 = \overline{2} \cdot 7924$$

$$\text{Add} = 8 \cdot 9912$$

$$\text{Add} = \overline{4} \cdot 6876$$

$$\overline{4} \cdot 6876$$

$$\text{Difference} = 12 \cdot 3036$$

$$\log Y = 12 \cdot 3036$$

$$Y = \text{Antilog } 12 \cdot 3036$$

$$Y = 2012 \times 10^{32} \text{ dynes/sq. cm.}$$

*Note:—Before using the logarithmic process of calculations, one must solve for addition and subtraction and express quantities in decimal fraction.*

**Graph and its uses**—In the study of certain physical phenomena a graph is plotted between the independent and dependent variables always taking the independent variable along the X-axis and dependent variable along the Y-axis. In plotting the graph the following points should be taken care of:—

- (1) Suitable scales for independent and dependent variables should be selected so that the full graph paper is used. These scales must be mentioned along the axis.

- (2) The origin should be selected properly depending on whether variable quantities are both positive or one positive and another has negative value also. In case both are positive, the lower left corner can be taken as origin. If dependent variable has negative values also, then middle point at the bottom should be taken as origin.

(3) The points on the graph paper are marked as dots or small circles etc. After marking all the points the smooth curve should be drawn which may pass through all the points or equal number of points exist on either side of it having about the same distance from the curve.

Graphs are used—(a) To prove certain laws, for example (i) a straight line plot between load and extension proves Hooke's law. (ii) a straight line plot between  $P$  and  $\frac{1}{V}$  proves Boyle's law.

(b) To understand the dependence of dependent variable on independent variable. For example the straight line plot between resistance ( $R$ ) and length of the wire ( $l$ ) shows that resistance is directly proportional to the length of the wire.

(c) To find out certain variable quantities accurately. For example in the constant volume air thermometer experiment, two points are taken on the curve and  $\beta$  is calculated from these two values only. It is equivalent to calculating with different sets of observations and then averaging the results.

In the Newton's law of cooling experiment, rate of cooling is determined from the graph.

## FRICITION

**Friction**—When a body is pulled over the surface of another body, an opposing force acts at the surface of contact. This opposing force is produced due to the roughness of the surfaces and it tends to stop the moving body. This property of the body is called **friction** and the force opposing the motion is known as the **force of friction**. The force of friction is always greater for dry surfaces.

**Limiting Friction**—When the pull to move a body on the surface of another is increased slowly then a stage is reached that the body just starts to move. This is known as the state of **limiting equilibrium** and the opposing force is called the **force of limiting friction**.

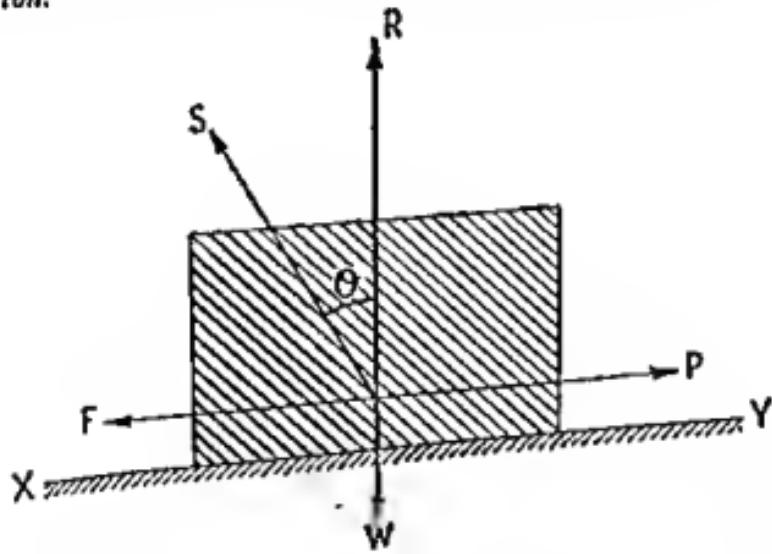


Fig. 1.1

Suppose a rectangular body is placed on a horizontal plane XY (Fig. 1.1). Its weight  $W$  acts in the downward direction and

the reaction of the plane 'R' in the upward direction, where  $R=W$  according to the Newton's third law of motion. If parallel to the plane a pull  $P$  is applied to the body, the force of friction  $F$  acts opposite to  $P$ . But on increasing the pull  $P$  slowly a state is just reached when the body tends to move which is the state of limiting equilibrium. In this state the force of friction is maximum.

Let  $S$  be the resultant of the upward reaction  $R$  and limiting force of friction  $F$ , then the angle between  $S$  and  $R$  is known as the *angle of friction*. The ratio of the limiting force of friction  $F$  and the reaction  $R$  is called the coefficient of friction and generally written as  $\mu$ .

$$\therefore \mu = \frac{F}{R}$$

$$\begin{aligned} \text{Since } F &= S \sin \theta \\ \text{and } R &= S \cos \theta \end{aligned}$$

$$\text{Hence } \tan \theta = \frac{F}{R} = \mu$$

The limiting values of  $\mu$  are—

$\mu=0$ , for perfectly smooth surfaces,

$\mu=1$ , for perfectly rough surfaces.

#### Laws of limiting friction

1. The force of friction acts in the direction opposite to the direction of motion.
2. The ratio of the limiting force of friction and the upward reaction is known as the coefficient of friction.
3. The coefficient of friction depends on the nature of the surfaces in contact and the upward reaction. It is independent of the shape and area of the surfaces.

#### EXPERIMENT 11

**Object**—To determine the coefficient of friction ( $\mu$ ) between two plane surfaces.

**Apparatus**—A wooden rectangular base having the plane glass top and at one side fitted with a smooth pulley, a rectangular wooden block fitted with one hook, thread, pan, weights and spirit level.

### Formula

$$\mu = \frac{F}{R}$$

Where  $\mu$  = coefficient of friction

$F$  = Limiting force of friction

= Weight of the pan + weights placed in the pan

$R$  = Normal reaction

= Weight of the rectangular wooden block + weight placed on this block.

### Method

1. First of all weigh the rectangular wooden block and the pan. Suppose their weights are  $M_1$  and  $M_2$ , respectively.

2. Level the apparatus with the help of the spirit level and make it horizontal. Then place the wooden block over it and tie the thread to its hook. Pass this thread over the pulley and fasten the pan to the free end of the thread.

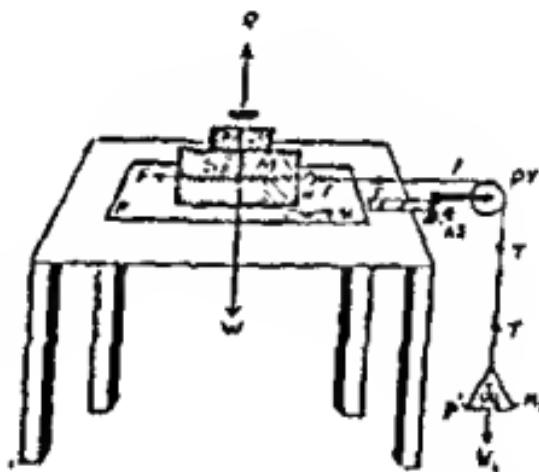


Fig. 1.2

3. Place a weight  $M_3$  on the wooden block and then place some weight on the pan. Increase the weight in the pan gradually till the block just starts to slide. Suppose the weights in the pan are  $M_4$ .

4. Repeat the experiment placing different weights on the wooden block. It may also be repeated using different wooden blocks.

## FRICTION

### Observations

Weight of the wooden block =  $M_1$  gm.

Weight of the pan =  $M_3$  gm.

Serial No.	Weight placed on the block $M_2$ gm	Reaction $R = (M_1 + M_2)$ gm	Weights placed on the pan $M_3$ gm	Force of friction $F = (M_3 + M_4)$ gm	$\mu = \frac{F}{R}$
1					
2					
3					
4					
5					
6					

Average = \_\_\_\_\_

### Calculations

$$\mu = \frac{F}{R}$$

Since,  $F = (M_3 + M_4)$  gm

and  $R = (M_1 + M_2)$  gm

$$\therefore \mu = \frac{(M_3 + M_4)}{(M_1 + M_2)}$$

### Result

Coefficient of friction between glass and wooden

Surface  $\mu =$

Standard  $\mu =$

Percentage error = %

### Precautions

1. The lower surface should be horizontal.
2. Pulley should offer least possible friction.
3. The thread from hook passing over the pulley should remain horizontal.
4. In case the experiment is repeated with different blocks, they should be equally rough and should be equally dry or moist.

## EXPERIMENT 1.2

**Object**—To find out the coefficient of friction between two given surfaces with the help of inclined plane.

**Apparatus**—Adjustable inclined plane apparatus, a rectangular block of wood, weights and spirit level.

The apparatus consists of horizontal wooden base WB and there is another plane IP which is hinged at H and can be kept inclined in the vertical plane at any angle  $\theta$ , with the horizontal plane with the help of knob K and the circular scale CS. (Fig. 1.3)

**Principle**—We have already seen that the relation between the angle of friction and the coefficient of friction is

$$\mu = \tan \theta$$

If  $\theta$  is determined we can find out  $\mu$  with the help of the tangent tables. As shown in the

Fig. 1.3, a wooden block of mass  $M_1$ , with a weight  $M_2$ , placed on it, i.e., the total weight  $W = (M_1 + M_2)$  is placed on the plane IP and the inclination of IP is slowly increased till the wooden piece along with its weight can just slide. We can perform

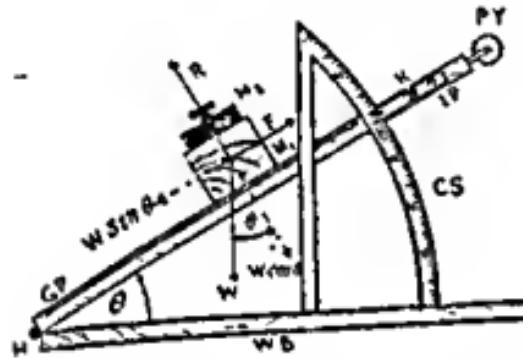


Fig. 1.3

this experiment without placing any weight on the wooden block as well. In this limiting equilibrium state of friction, we have

$$F = W \sin \theta$$

$$\text{and } R = W \cos \theta$$

$$\text{Hence } \frac{F}{R} = \tan \theta$$

and we know from the definition

$$\mu = \frac{F}{R}$$

$$\mu = \tan \theta$$

It is obvious that  $\mu$  is independent of the weight of wooden block or any other weight if placed on it.

### Method

1. Level the base WB with the help of the spirit level.
2. Place the wooden block on the inclined plane IP and adjust its inclination such that the block may start to slide downwards. If necessary tap the plane gently. Fix the inclination with the help of the knob K.
3. Read the angle of inclination with the help of the circular scale CS.
4. Repeat the experiment after placing certain weights on the wooden block.
5. Repeat the experiment with other faces of the wooden block touching the plane IP.

### Observations

#### Observation table

Serial No.	Angle of friction for first face $\theta_1$	Angle of friction for second face $\theta_2$	Average $\theta = \frac{\theta_1 + \theta_2}{2}$
1			
2			
3			
4			

Average  $\theta =$

### Result

Standard result—

Percentage error = %

### Precautions

Same as in case of previous experiment

### Oral questions

1. What is the limiting force of friction?
2. What are the factors governing the limiting force of friction?
3. State the law of limiting friction.
4. Explain the term normal reaction.
5. Define the coefficient of friction.

6. Give some examples where you have realised the phenomenon of friction in daily life.
7. What is the importance of friction in daily life ?
8. What is the practical importance of the study of the coefficient of friction ?
9. Does the force of friction depend on the areas in contact?
10. How does an error occur in the coefficient of friction if the pulley is not perfectly smooth ?
11. Do you think that the pulley is completely smooth ? If no then what happens to your results ?
12. Define the angle of friction.
13. Does it depend on the normal reaction ?

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# 2

## YOUNG'S MODULUS OF ELASTICITY

Elasticity—A body, on the application of an external force, undergoes a change in its shape and size and on the withdrawal of the deforming force it regains its original position, then it is said to be *elastic*. This property of the matter is called *elasticity*. If on the withdrawal of the deforming force a body returns to its original position completely, it is said to be *perfectly elastic* and otherwise the deformed position is retained exactly, then the body is said to be *perfectly plastic*. Perfect elasticity and perfect plasticity are the two limiting cases and all the material bodies adjust between these two limits.

Strain—The internal force deforms a body. The deformation is considered relative to its original size and shape. Suppose a wire of original length  $L$  cm is increased in length by 1 cm by applying a force  $F$ . Then the strain is measured as the ratio of the increase in length to the original length.

$$\therefore \text{Longitudinal strain} = \frac{l}{L}$$

Similarly a body of the original volume  $V$  c.c. undergoes a change of  $\delta$  c.c. in its volume on the application of an external force, then,

$$\text{Volume strain} = \frac{\delta}{V}$$

Obviously, the strain has no unit being the ratio of the two quantities of the same nature.

Stress—Whenever an external force is applied on a body, it is deformed and an internal reaction is developed within the body which tends to bring the body to its original position. The internal reaction is equal and opposite to the deforming force with in elastic



## EXPERIMENT 2-1

**Object**—To determine the Young's modulus of a given wire.

**Apparatus**—A young's modulus apparatus, a metre scale, weights and a screw gauge.

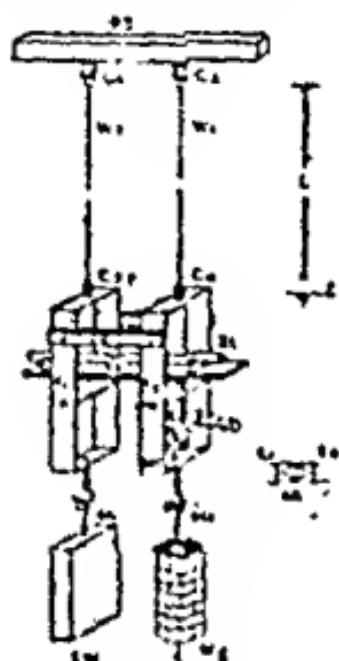


Fig. 21      of  $W_2$  produced by the weight  $W_3$

$C_1, C_2, C_3, C_4$ —Clips to hold the wires

CR—Common rod between the metal frames

**Formulas**

$W_1, W_2$ —Two wires of the same given metal

$F_1, F_2$ —Rectangular metal frame

RS—Common rigid support

SL—Spirit level

GS—Circular scale

MS—Main scale

$H_1, H_2$ —Hangers

$W$ —Weight suspended to straighten the wire  $W_2$

$L$ —Original length of the wire  $W_2$  (inside  $C_1$  and  $C_2$ )

$M_2$ —Weight applied to the wire  $W_1$

$\delta$ —Increase in the length

(2) Put certain weight in the hanger of the experimental wire  $W_1$  to remove kinks.

(3) Measure the length of the experimental wire  $W_1$  from lower end of  $C_1$  to upper end of  $C_1$ .

(4) Now adjust the circular scale to bring the bubble in the centre of the spirit level. Load the experimental wire in the steps of 1 Kg. With the help of the circular scale bring the bubble in the centre of spirit level and take down the respective reading on the main scale as well as the circular scale. It can be loaded up to 6 kg.

(5) Unload the wire in the steps of 1 Kg. Adjust the spirit level and take down the respective readings.

(6) Find out the mean reading for each load with the help of the readings taken while the load increasing and decreasing.

(7) Find out the increase in length for certain load making use of observations in a systematic manner. For example, subtracting the readings for loads 1, 2, 3 Kg from those of 4, 5, 6 Kg respectively. Thus three sets for increase in length for 3 Kg load are obtained. Calculate the mean value.

(8) Note down the pitch, least count and zero error of screw gauge. Measure the diameter of the experimental wire at least at four different points and at every point in mutually perpendicular directions. Calculate mean diameter and then find out the radius of the wire.

(9) Finally calculate the Y using the formula.

#### Observations

Pitch of the spherometer = cm

Least count of the spherometer = cm

Length of the wire = L = 245 cm

Observation table for extension of the wire (I)

No. S.	Load	Reading of micrometer screw						Extension for 3 Kg.	
		Load increasing		Load decreasing		Mean reading $\frac{a+b}{2}$			
		M.S.	C.S.	M.S.	C.S.				
1	1 Kg		a		b		A	$(D-A)=$ 0.136 cm.	
2	2 Kg						B		
3	3 Kg						C	$(E-B)=$ 0.134 cm.	
4	4 Kg						D		
5	5 Kg						E	$(F-C)=$ 0.138 cm.	
6	6 Kg						F		

Mean extension = 0.136 cm  
for 3 Kg

## Observations for radius of the wire.

Pitch of the screw gauge = cm

Least count of the screw = cm

Zero error of the screw gauge =

## Observation table for radius of wire (r)

No. S.	Reading in one direction			Reading in other direction			Mean diameter $\frac{A+B}{2}$
	M.S.	C.S.	Corrected diameter A	M.S.	C.S.	Corrected diameter B	
1.							
2.							
3.							
4.							
5.							
6.							
7.							

Mean diameter = 0.084 cm  
∴ Average r = 0.042 cm

## Calculations

$$Y = \frac{MgL}{\pi r^2 l}$$

$$= \frac{3000 \times 980 \times 245 \times 7}{22 \times .042 \times .042 \times 1.36}$$

$$= \left( \frac{3 \times 98 \times 245 \times 7}{22 \times 42 \times 42 \times 1.36} \right) \times 10^{11}$$

$$\approx X \times 10^{11}$$

X stands for the quantity inside the bracket.

$$\log 3 = 0.4771$$

$$\log 22 = 1.3424$$

$$\log 98 = 1.9912$$

$$2 \log 42 = 3.2464$$

$$\log 245 = 2.3892$$

$$\log 1.36 = 0.1335$$

$$\log 7 = 0.8451$$

$$\text{Add} = 4.7223$$

$$\text{Add} = 5.7026$$

$$4.7223$$

$$\text{Diff.} = 0.9803$$

$$\text{Antilog } 0.9803 = 9.557$$

$$\therefore Y = 9.557 \times 10^{11} \text{ dynes/sq. cm.}$$

Result—Young's modulus for brass,  $Y = 9.557 \times 10^{11}$  dynes/sq.cm

Standard result,  $Y = 9.9 \times 10^{11}$  dynes/sq. cm.

Percentage error = %

Precautions—(1) There should be no kinks in the wire.

(2) Wire should be loaded and unloaded gently and some time should be given before taking the observations.

(3) Load should not increase more than half the breaking load.

(4) Bubble should be brought in the centre of the spirit level before taking the reading.

(5) Reading for radius should be taken more carefully as its value appears in the formula.

## EXPERIMENT 2.2

Object—Verify Hooke's law

Apparatus—Young's modulus apparatus, loads,

It can also be proved by showing that  
Load  $\propto$  extension

Method—Same as in the experiment 21 except that the radius of the wire and extension for certain fixed load need not be found out.

#### Observations

Observation table for Hooke's law verification.

S. No.	Load	Reading of micrometer screw						
		Load increasing		Load decreasing		Mean reading $\frac{a+b}{2}$	Extension in cm.	
		M.S.	C.S.	Total a	M.S.	C.S.	b	
1	0 Kg.							(B-A) = A = 0.136
2	1 Kg.							(C-A) = B = 0.273
3	2 Kg.							(D-A) = C = 0.405
4	3 Kg.							(E-A) = D = 0.545
5	4 Kg.							(F-A) = E = 0.684
6	5 Kg.							(G-A) = F = 0.818
7	6 Kg.							G =

A graph is plotted between the load and extension taking

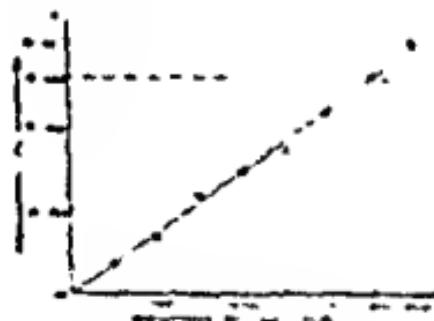


Fig. 22

Load along the X-axis and extension along the Y-axis. The straight line is obtained as shown in the Fig. 22.

**Result**—The graph plotted between load and extension comes to be a straight line which proves the Hooke's law.

**Precautions**—Same as in experiment 2.1

#### **Oral questions**

- (1) Explain elasticity, coefficient of elasticity, elastic limit and elastic fatigue.
- (2) Define strain, stress and Young's modulus of elasticity and mention their respective units.
- (3) State Hooke's law and how will you prove it.
- (4) Explain why two similar wires are used in the Young's modulus apparatus ?
- (5) Which is more elastic, rubber or steel ?
- (6) What is the significance of Young's modulus in practical life.
- (7) Explain why do you use the micrometer screw to measure the extension while the metre scale or tap for measuring the length of the wire ?
- (8) Why do you measure the radius of the wire more accurately ?
- (9) Explain the terms—Pitch, least count, zero error and backlash error.
- (10) How do you eliminate the backlash error ?

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# 3

## BOYLE'S LAW

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The study of the gaseous state of matter is in fact the study of variation of its volume, pressure and temperature in a systematic manner. Every gas below the critical temperature is known as vapour and it is liable to condense if pressure is increased. It was Boyle who first made a systematic study of the dependence of the volume of a given mass of a gas on its pressure when temperature remains constant and the relation observed by him is known as Boyle's law. His observation is not true for vapour state.

Boyle's law states "The volume of a given mass of a gas at constant temperature is inversely proportional to its pressure."

If  $P$  and  $V$  are the pressure and volume of a given mass of a gas at a constant temperature  $T$ , then according to Boyle's law, we have

$$P \propto \frac{1}{V}$$

$$\text{or } P = K \frac{1}{V}$$

$$\text{or } PV = K \{ \text{constant} \}$$

When the pressure of the gas is varied isothermally, i. e., by maintaining the constant temperature, the volume also changes and according to Boyle's law, we have the following relation—

$$P_1 V_1 = P_2 V_2 = P_3 V_3 = \dots = K \{ \text{constant} \}$$

Where  $P_1, P_2, P_3$  are the different pressures and  $V_1, V_2, V_3$  are the corresponding volumes of the gas.

### Limitations of Boyle's law

1. Boyle's law is accurate at low pressures and does not hold true at very high pressures.

2. For ordinary gases it is accurate at a certain temperature known as Boyle's temperature. Boyle's temperature is three times the critical temperature for a gas.

3. Vapours do not obey Boyle's law. If water vapours are present in any gas, on increasing the pressure the gas may be saturated with water vapours.

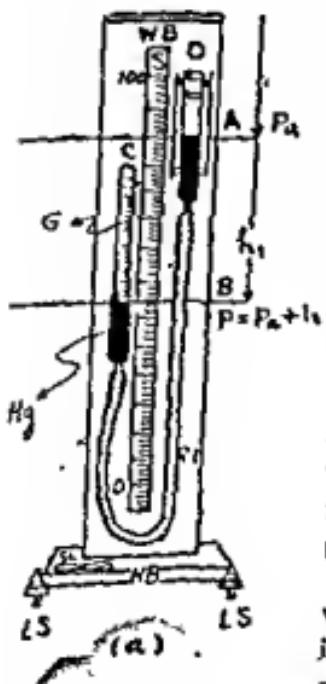
For ideal gases the Boyle's law is vigorously true for all ranges of temperature and pressure but real gases suffer from certain limitations which have been pointed out above in short.

### EXPERIMENT 3-I

**Object**—Verify Boyle's law.

**Apparatus**—Boyle's law apparatus, a barometer etc.

**Description of the Boyle's law apparatus**—It consists of a vertical wooden stand fitted with a metre scale S as shown in the Fig. 3-I and there are two slots on either side of the scale. In one slot there is fitted a tube C graduated in cubic centimetres with its upper end closed. In another slot there is fitted an open tube O. The tube O can be slid up and down in the slot. Both the glass tubes are connected by rubber tubing R.T. The rubber tubing and a part of tubes O and C contain pure mercury. There is dry air enclosed in the upper portion of the tube C. The base of the apparatus is fitted with three levelling screws to make the scale perfectly vertical.



**Theory**—Boyle's law states that the volume of a given mass of a gas varies inversely to its pressure when temperature remains constant.

Let P and V be the pressure and the volume of a given mass of a gas respectively.

$$\therefore P \propto \frac{1}{V}$$

$$\text{or } PV = \text{constant (k)}$$

Hence according to Boyle's law

$$P_1 V_1 = P_2 V_2 = P_3 V_3 = \dots \dots \dots K$$

If the gas is enclosed in a tube of uniform cross-section  $V \propto l$  where l is the length of the air column.

Therefore, according to Boyle's law, we have

$$P_1 l_1 = P_2 l_2 = P_3 l_3 = \dots \dots$$

$$\text{and } P \propto \frac{1}{l}$$

#### Method

1. Read the atmospheric pressure and the room temperature with the help of a barometer and a thermometer respectively.

2. Make the apparatus perfectly vertical with the help of levelling screws and raise the open tube O to a convenient height as shown in (fig. 31). Now take down the readings of the upper end of the tube C and the positions of convex meniscus of mercury in both the tubes C and O. If C is graduated, the volume of the gas can be read directly.

3. Note the difference of the closed end of C and the convex meniscus of mercury in C which gives h, i.e., the height of the column of gas.

4. Note down the difference of mercury meniscus in the tubes C and O and let it be h'. As it is clear from the fig. 31 the pressure of the gas is greater than that of atmosphere by h. Therefore the gas pressure  $P = \text{atmospheric pressure } P_a + h$

5. Slowly slide the tube O downwards in steps and take down at least six readings with the gas pressure greater than that of atmosphere.

6. Then slide the tube O in such a way that the mercury level in O is lower than that of C and in these cases the gas pressure is less than that of atmosphere as shown in the fig. 3-2. Take down at least six readings when the gas pressure is less than the atmospheric pressure. In these cases the gas pressure  $P = \text{atmospheric pressure } P_a - h$ .

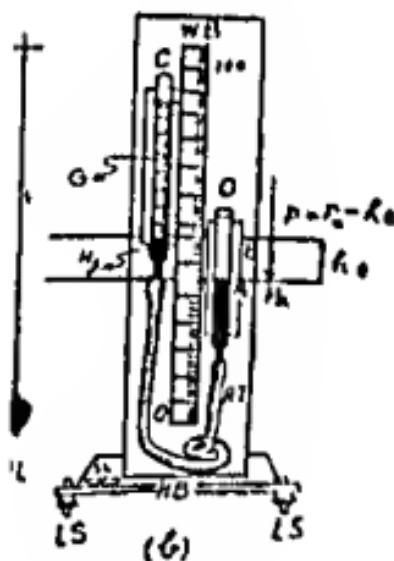


FIG. 3-2

### Observations

Atmospheric pressure in the beginning	=	cm
" " in the end	=	cm
Mean atmospheric pressure $P_a$	=	..
Room temperature in the beginning	=	°
" " in the end	=	°

### Calculations

**Result**—The product  $PV$  is constant which proves the law.

In case the tube C is not graduated in cc. the graph between  $P$  and  $\frac{1}{V}$  is plotted.

When a graph between  $P$  and  $\frac{1}{V}$  is drawn it comes to be a straight line as shown in the fig. 3.3 which further verifies the Boyle's law.

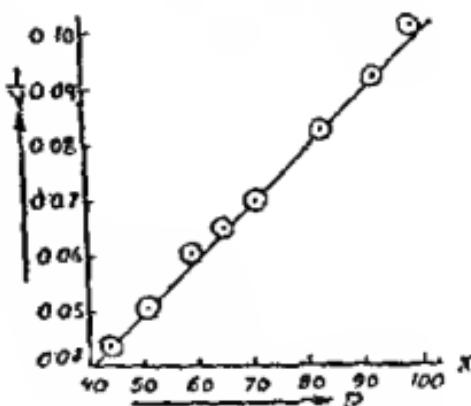


Fig. 3.3

### Precautions

- Some time should be given before taking each reading to ensure the change to be isothermal.

- The mercury level should be read for the highest point of the convex meniscus.

## EXPERIMENT 3.2

**Object**—To find out the atmospheric pressure using the Boyle's law apparatus.

**Apparatus**—Same as in the previous experiment.

**Theory**—(i) From Boyle's law, we have

$$P_1 V_1 = P_2 V_2$$

Where  $P_1$  and  $P_2$  are  $(P_a \pm h_1)$  and  $(P_a \pm h_2)$  respectively  
Therefore,

$$(P_a \pm h_1)V_1 = (P_a \pm h_2)V_2$$

If  $h$  is positive on both sides, then

$$(P_a + h_1)V_1 = (P_a + h_2)V_2$$

$$\text{or } P_a(V_1 - V_2) = h_2 V_2 - h_1 V_1$$

$$\text{or } P_a = \frac{h_2 V_2 - h_1 V_1}{V_1 - V_2}$$

Similarly  $P_a$  can be calculated from different sets of readings.

(ii) By plotting the graph—If we plot the graph with a suitable scale taking  $h$  along the X-axis and  $\frac{1}{V}$  along the Y-axis we obtain a straight line as shown in the fig. 3.4

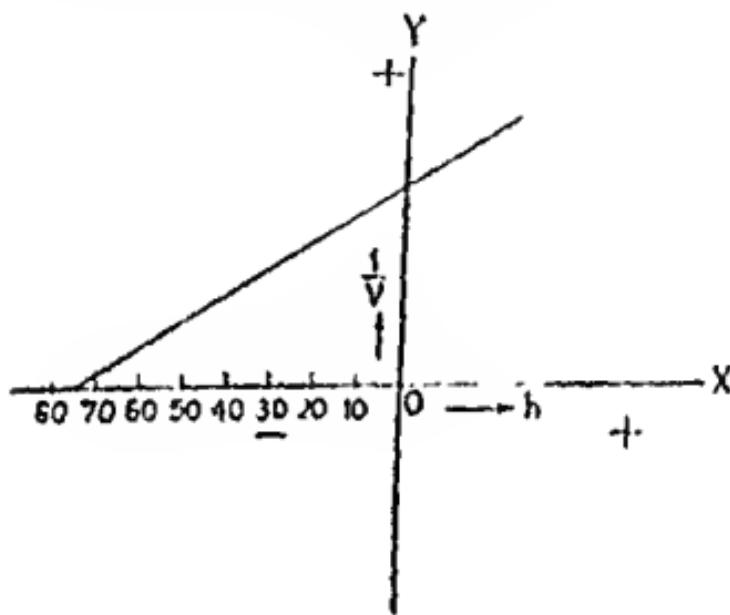


Fig. 3.4

The intercept on the X-axis gives the atmospheric pressure.

**Method**—Same as in the previous experiment.

#### Observations

Readings of the upper closed end of C = \_\_\_\_\_ cm

S.No.	Mercury level in C	Mercury level in O	Difference of levels in C and Oths	Volume of the gas V	1/V
1.					
2.					
3.					
4.					
5.					
6.					

**Calculations****Result -**

"Atmospheric pressure	=	cm
Correct result at that place	=	cm
(From barometer)		

Percentage error = %

**Precautions—** Same as in the previous experiment.

**Oral questions**

1. Explain Boyle's law.
2. Point out the limitations of Boyle's law.
3. What is an isothermal change ? Give some examples of such changes.
4. What do you understand by ideal gas and real gas ?
5. What is the difference between a gas and a vapour ?
6. Explain the critical temperature of a gas.
7. If there is water vapour in a closed tube, will the Boyle's law hold true ?
8. Define pressure and mention its unit.
9. What is atmospheric pressure ? How do you express it ?
10. How will you express it in usual units of pressure ?
11. How do you find the pressure of the gas enclosed in the Boyle's law apparatus ?

Why mercury is preferred in the Boyle's law apparatus over other liquids ?

How do you ensure the change to be isothermal in your experiment ?

Explain adiabatic change and give some examples of it.

What do you understand by Boyle's temperature ? What is its significance ?

---

#### **Procedure**

1. Put sufficient water in the boiler and put it on the burner or heater.
2. Make the electric connections as shown in the figures 4.1 and 4.2.
3. Note down the pitch and the least count of the spherometer.
4. Measure the length of the experimental rod.
5. Put a thermometer through the cork in the jacket just to make its bulb touching the rod and note down initial temperature.
6. Take the initial reading of the spherometer when its middle leg is made to touch the free end of the rod. The contact is ensured by the deflection in the voltmeter. Read this setting repeatedly and record in the table. Rotate the spherometer such that the free end can expand freely.
7. Now pass the steam in the jacket and wait till the temperature of the rod becomes constant. Note down the temperature.
8. Take the final reading with spherometer and repeat it number of times.
9. Find out the mean expansion of the rod and calculate

## Observations

Initial length of the rod at room temperature = cm

Initial temperature = °C

Pitch of the spherometer = cm

**Least count** = **cm**

Final temperature = °C

### Observation table for expansion

## Calculations

$$\alpha = \frac{L_2 - L_1}{L_1 (t_2 - t_1)}$$

$$\alpha = \frac{0.065}{50.1 \times (98.5^\circ - 30^\circ)} \quad \text{Since } L_2 - L_1 = 0.065 \text{ cm}$$

$$\alpha = \frac{0.065}{50.1 \times 68.5} \quad \text{and } L_1 = 50.1 \text{ cm}$$

$$\log 0.065 = 2.8129 \quad | \quad \log 50.1 = 1.6998$$

$$3.5355 \quad | \quad \log 68.5 = 1.8357$$

$$\text{Diff.} = 3.2774 \quad | \quad \text{Add} = 3.5355$$

$$\log \alpha = 3.2774$$

$$\therefore \alpha = \text{antilog } 3.2774$$

$$\text{or } \alpha = 0.0000167 \text{ per degree centigrade}$$

## Result

Standard result—

Percentage error—

## Precautions

1. There should be taken sufficient water in the boiler.
2. Rubber tubings should be properly placed to avoid the collection of condensed water in them.
3. The end of the exit rubber tube should be dipped in water so that steam coming from the jacket may be condensed.
4. Spherometer reading should be taken when contact is ensured by deflection in the voltmeter.
5. Back lash error should be avoided.
6. For final reading the temperature should be constant for 10 minutes.

## Oral Questions

1. Define the coefficient of linear expansion and mention its unit.
2. Why do you use spherometer to find the expansion in length?
3. What is the use of electric circuit in this experiment.
4. What is the practical importance of the knowledge of coefficient of linear expansion?
5. Why some space is left between two pieces of rail? Is it experiment?

# 5

## THERMAL EXPANSION OF LIQUIDS

In general all liquids expand on heating except water between  $0^{\circ}\text{C}$  and  $4^{\circ}\text{C}$  and some aqueous solutions. Liquids do not have their own shape but they acquire the shape of the containers containing them. The cubical expansion of liquid, in general, consists of two parts relative to the container. If we neglect the expansion of the container, the expansion of liquid is apparent expansion which is less than the true expansion. When account is taken into consideration of the expansion of the container, then it is called the real expansion. Thus there are two distinct coefficients of cubical expansion of liquids.

### Coefficient of apparent expansion

It is defined as the apparent increase in volume per unit volume per degree rise in temperature when the liquid is heated in a container which expands on heating. It is represented by  $C_a$ .

### Coefficient of real expansion

It is defined as the actual increase in volume per unit volume per unit degree rise in temperature. It is represented by  $C_r$ .

$C_r$  is greater than  $C_a$  by the coefficient of cubical expansion of the material of the container. If liquid is contained in a glass vessel and coefficient of cubical expansion of glass is  $C_g$ , then -

$$C_r = C_a + C_g.$$

## EXPERIMENT 5.1

**Object**—To determine the coefficient of apparent cubical expansion of a liquid using a weight thermometer\*.

**Apparatus**—A weight thermometer, liquid thermometer, a balance, weight box, water bath, burner or heater etc.

$$\text{Formula} \quad C_a = \frac{m}{M_t \times t}$$

Where  $C_a$  = Coefficient of apparent expansion

$m$  = mass of liquid expelled from the weight thermometer on heating up to constant temperature (temperature of boiling water).

$M_t$  = Mass of liquid left in the weight thermometer at the boiling temperature of water.

$t$  = difference of temperature of the boiling water and room temperature.

**Procedure**

1. Wash the weight thermometer with nitric acid, dry it and then weigh it empty.

2. To fill the liquid in the weight thermometer, suspend it from a thread and dip its mouth in the hot liquid contained in a beaker as shown in the fig. 5.1. Now heat the weight thermometer so that air inside it will expand and will go out. On cooling the air inside it contracts and the liquid rushes in.

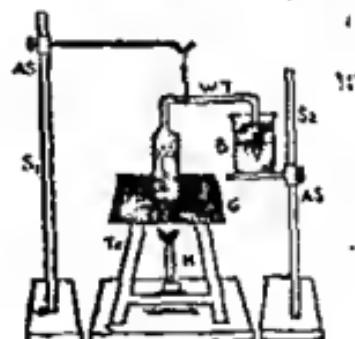


Fig. 5.1

\*The specific gravity bottle may be used in place of a weight thermometer and in working it is very convenient.

3. Again heat it so that some air will go out and on cooling more liquid will rush into the weight thermometer.

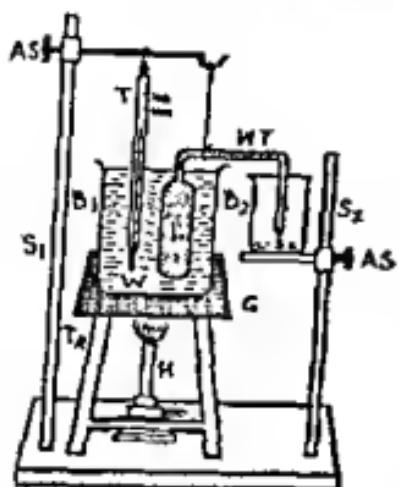


fig. 5.2

4. By alternate heating and cooling fill the weight thermometer completely with the liquid at the room temperature. Wipe it and find out its mass with liquid.

5. Suspend the weight thermometer in the water bath with its mouth inside beaker  $S_1$  as shown in the fig. 5.2 and then heat it.

6. The liquid from the weight thermometer comes out in the beaker on heating. It continues till the boiling point of water is reached and then no more liquid flows out.

7. Wipe the weight thermometer, cool it and then weigh it.

8. Take down the room temperature. It is better if it is taken at the beginning of the experiment also.

9. Calculate the coefficient of apparent cubical expansion of the given liquid.

#### Observations

1. Mass of the empty weight thermometer	- gm
2. Mass of the weight thermometer filled with liquid at room temperature	- gm
3. Mass of the weight thermometer filled with liquid at boiling point of water	- gm
4. Room temp. at the beginning of the experiment	- °C
5. Room temp. at the end of the experiment	- °C
6. Boiling point of water	- °C

**Calculations**

$$C_a = \frac{1.545}{51.260 \times 73.5}$$

$$\therefore \log C_a = (\log 1.545) - (\log 51.260 + \log 73.5)$$

$$\begin{array}{r} \log 1.545 = 0.1889 \\ \quad\quad\quad 3.5761 \\ \hline \text{Diff.} = 4.6128 \\ \log C_a = 4.6128 \end{array}$$

$$\begin{array}{r} \log 51.26 = 1.7098 \\ \log 73.5 = 1.8663 \\ \hline \text{Add} = 3.5761 \end{array}$$

$$C_a = \text{Antilog } 4.6128$$

$$= 0.0004101 \text{ per } ^\circ\text{C}$$

**Result**

Coefficient of apparent cubical expansion

of the given liquid =

Standard result =

Percentage error = %.

**Precautions**

1. Air bubbles should be removed from the weight thermometer.
2. Liquid should be heated before filling to save the weight thermometer from cracking.
3. Weight thermometer should be handled gently.
4. In transit no liquid should come out of the weight thermometer

**Oral Questions**

1. Define the coefficient of apparent cubical expansion and mention its unit.
2. How do you relate the coefficient of apparent expansion to that of real expansion?
3. Why do you call it weight thermometer?
4. Can you find out  $C_a$  of all liquids by this?

5. Does a liquid expand uniformly at all temperatures ?
6. What is the practical application of the knowledge of thermal expansion of liquid ?

*Note—The same experiment can be performed with the help of a specific gravity bottle and it is easier to fill the liquid in*

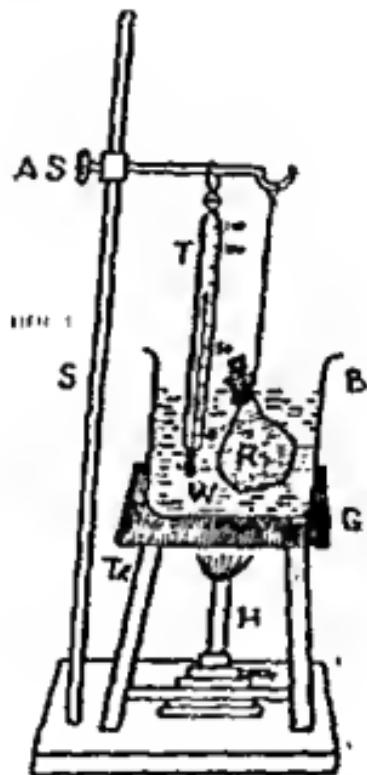


Fig. 5.3

this bottle than in the weight thermometer. We need not heat and cool it alternately to fill the liquid. Rest of the procedure is the same. Specific gravity bottle is shown in the fig. 5.3 when it is heated to expell the liquid out of it at the boiling temp. of water.

## CONSTANT VOLUME GAS THERMOMETER

---

The state of a gas is characterised by three quantities, viz, its pressure  $P$ , volume  $V$  and temperature  $T$ . These quantities are inter-dependent and their dependence is studied by keeping one of them constant and varying the second to study the variation of the third. Here the volume of a given mass of a gas is kept constant and by varying the temperature the variation in pressure is studied which gives the law of pressure.

The variation of pressure of a given mass of a gas is uniform with respect to temperature when volume is kept constant. This property is used for measuring temperatures hence the apparatus to study the variation of pressure with respect to temperature when volume is kept constant is called constant volume gas thermometer Pressure coefficient

It is defined as the ratio of the increase in pressure of the gas at constant volume, per degree rise of temperature, to its pressure at  $0^{\circ}\text{C}$ . If  $P_0$  and  $P$  be the pressure of a given mass of a gas, keeping its volume constant, at  $0^{\circ}\text{C}$  and  $t^{\circ}\text{C}$  respectively, then

$$P = P_0 (1 + \beta t)$$

Where  $\beta$  = pressure coefficient

$$\beta = \frac{P - P_0}{P_0 \times t}$$

### EXPERIMENT 6-I

**Object**—Study the variation of pressure with temperature using constant volume air thermometer and determine the pressure coefficient of air.

**Apparatus**—Constant volume air thermometer, ordinary thermometer, tripod stand, water bath, stirrer, wire gauge, burner etc.



2. Immerse the glass bulb G B completely in the water inside beaker B as shown in the fig. 6.1 and read the initial temperature (room temperature) after stirring the water.

3. To keep the volume of air constant fix a mark and it is M in case of fig. 6.1

4. Read the atmospheric pressure with the help of a Fortin's barometer correct up to mm.

5. Read the mercury level in the tube O T at room temperature.

6. Now heat the water in the beaker B with the help of burner or heater or whatever heating device is provided in the laboratory till water starts boiling. Stir it thoroughly and after 5 minutes when temperature has become constant adjust the position of the tube O T such that mercury level in capillary tube stands against the mark M. Then read the mercury level in O T and temperature of boiling water.

7. To cool the water in the beaker B put off the burner. Stir it well and after the interval of every  $5^{\circ}\text{C}$  take down the reading of mercury level in open tube O T after adjusting its position to bring the mercury level in the capillary against M.

8. Read the barometer in the end also.

9. Find out the difference for mercury level in case of every observation and by adding it to the atmospheric pressure. Obtain the pressure exerted by air enclosed in G B.

10. Plot a graph between temperature and air pressure and select two suitable points on the graph to calculate  $\beta$ . With the help of these values calculate  $\beta$ .

#### Observations

Atmospheric pressure at the beginning of experiment - cm

" " - end " " - cm

Average atmospheric pressure  $P_a$  - cm

### Description of constant volume air thermometer

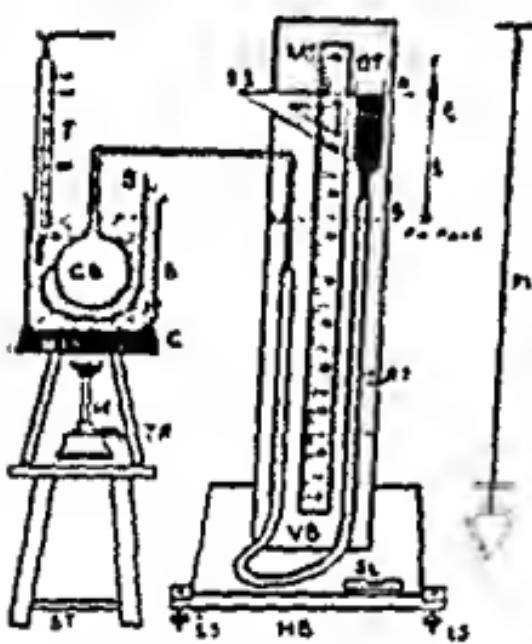


Fig. 6.1

and there a scale fitted to the vertical stand.

#### Theory

At the constant volume the ratio of the increase in pressure of a given mass of a gas for the rise of  $1^{\circ}\text{C}$  to its pressure at  $0^{\circ}\text{C}$  is defined as pressure coefficient. It is measured with the following formula

$$\beta = \frac{P - P_0}{P_0 \times t}$$

Obviously the pressure of the gas is measured at  $0^{\circ}\text{C}$  and  $t^{\circ}\text{C}$ . It is more convenient to take the room temperature and the temperature of boiling water or any pair of temperatures selected between these two temperatures.

$$\text{Since } P_1 = P_0 (1 + \beta t_1) \quad \dots \dots \dots (1)$$

$$\text{Or } P_2 = P_0 (1 + \beta t_2) \quad \dots \dots \dots (2)$$

From (1) and (2) we obtain

$$\beta = \frac{P_2 - P_1}{P_1 t_2 - P_2 t_1}$$

It consists of a glass bulb G as shown in the figure 6.1. Glass bulb is connected to a thick capillary tube bent twice at right angles. There is glass tube OT fitted to a vertical stand and can be moved up and down. OT is connected to the capillary tube through a rubber tubing RT. Glass bulb and part of capillary tube is filled with air and tube OT and rubber tubing RT contain mercury. The base of the vertical stand is fitted with levelling screws

$$= \frac{86.4 - 70.4}{70.4 \times 98 - 86.4 \times 31}$$

$$= \frac{16}{70.4 \times 98 - 86.4 \times 31}$$

$$\log 70.4 = 1.8482$$

$$\log 98 = 1.9912$$

$$\text{Add } X = 3.8394$$

$$\text{Antilog } X = 6908.0$$

$$\log 86.4 = 1.9370$$

$$\log 31 = 1.4914$$

$$\text{Add } Y = 3.4284$$

$$\text{Antilog } Y = 2681.0$$

$$\therefore \beta = \frac{16}{6908 - 2681}$$

$$= \frac{16}{4227}$$

$$\log \beta = \log 16 - \log 4227$$

$$= 1.2041 - 3.6260$$

$$= -1.5781$$

$$\therefore \beta \approx \text{Antilog } -1.5781$$

$$= -0.003785 / {}^{\circ}\text{C}$$

$$2. \quad \beta = \frac{P_{100} - P_0}{P_0 \times 100}$$

$$= \frac{87.5 - 64.1}{64.1 \times 100}$$

$$= \frac{23.4}{6410}$$

$$\log \beta = \log 23.4 - \log 6410$$

$$= 1.3692 - 3.8069$$

$$= -1.5623$$

$$\therefore \beta \approx \text{Antilog } -1.5623$$

$$= -0.003663 / {}^{\circ}\text{C}$$

Result

Pressure coefficient of air =  $-0.003663 / {}^{\circ}\text{C}$

Standard result =

Percentage error = %

Precautions

1. The glass bulb G B should contain dry air.
2. The mercury used should be pure and dry and should not stick to the sides of the apparatus. There should be no traces of mercury in the glass bulb.

## PRACTICAL PHYSICS

#### **irrigation cable**

**Calculations—Plot a graph** between temperature and air pressure taking temperature along the X-axis and air pressure along the Y-axis. As shown in the figure 6.2 it comes to be a straight line which shows that air pressure is directly proportional to the temperature when volume of the given mass of a gas (air) is kept constant.

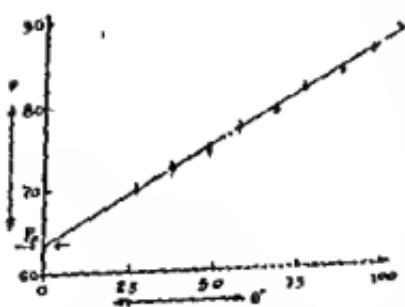


Fig. 6·2

Fig. 6.2  
From the graph select any two suitable points which can be  $0^{\circ}\text{C}$  and boiling point of water and find out the corresponding values from the graph and calculate  $\beta$ .

Any other two points except  $0^{\circ}\text{C}$  and boiling point of water  
be taken but they should be far apart

2. To calculate melting point of wax, we have to measure the air pressure at  $0^{\circ}\text{C}$ , boiling point of water, i. e., at  $100^{\circ}\text{C}$  and at the melting point of wax which are  $P_0$ ,  $P_{100}$  and  $P$  respectively. Then with the help of the formula given above the melting point of wax can be determined.

$P_0$  and  $P_{100}$  can be obtained from graph also.

#### Observations

Same as in experiment 6.1 plus additional observations for air pressure at  $0^{\circ}\text{C}$  and boiling point of water and melting point of wax.

$P_0$  and  $P_{100}$  can also be obtained from the graph.

#### Calculations

(i) Plot the graph as described already.

$$(ii) \quad t = \frac{P - P_0}{P_{100} - P_0} \times 100$$

#### Result

Standard result

Percentage error

#### Precautions

Same as in experiment 6.1

#### Oral Questions

1. Define the pressure coefficient. Mention its unit. What is its value for perfect gases?
2. Why do you insist to fill the dry air in the glass bulb of the constant volume air thermometer?
3. What are the advantages of mercury used in a gas thermometer?
4. Can we use water for mercury?
5. How do you keep the volume of the gas constant?
6. How will you measure the melting point of wax by the gas thermometer?
7. Can we measure the temperature of human body by this thermometer?
8. What is the relation between pressure and temperature of a given mass of a gas at constant volume?
9. What are the important precautions?
10. Explain the absolute zero.

3. The glass bulb should be completely immersed in water in the beaker B and should be stirred well before each reading.
4. While cooling the gas the open tube should be lowered so that on contraction of air on cooling mercury may not rush into the glass bulb G B.
5. The reading for temperatures between room temperature and boiling point of water should be taken while cooling the air in G B.

### EXPERIMENT 6·2

**Object**-To measure the melting point of wax using the constant volume air thermometer.

**Apparatus**-Same as in the experiment 6·1.

**Theory**-The melting point of wax can be determined either ( i ) with the help of the graph plotted between the temperature and pressure, or ( ii ) it can be calculated by the following formula also

$$t = \frac{P - P_0}{P_{100} - P_0} \times 100$$

Where  $P_0$ =Air pressure at  $0^\circ\text{C}$

$P_{100}$ =Air pressure at boiling point of water

$P$ =Air pressure at melting point of wax.

$t$ =Melting point of wax

#### Procedure

1. The experiment is performed as described in experiment 6·1 and graph between temperature and air pressure is also plotted as already described.

To measure the melting point of wax the glass bulb OB is immersed in a container full of wax. The container is heated and when wax starts to melt the open tube OT is so adjusted that mercury in the capillary stands against the fixed mark M. The observation of mercury level in OT is taken. When all the wax melted then it is permitted to solidify. Again when wax starts to solidify the open tube OT is so adjusted that mercury level in the capillary stands against the fixed mark M. The mercury level in OT is noted. Hence  $P$  the air pressure at melting point of wax is found. From the graph, the temperature corresponding to  $P$  gives the melting point of wax.

2. To calculate melting point of wax, we have to measure the air pressure at  $0^{\circ}\text{C}$ , boiling point of water, i. e., at  $100^{\circ}\text{C}$  and at the melting point of wax which are  $P_0$ ,  $P_{100}$  and  $P$  respectively. Then with the help of the formula given above the melting point of wax can be determined.

$P_0$  and  $P_{100}$  can be obtained from graph also.

#### Observations

Same as in experiment 6.1 plus additional observations for air pressure at  $0^{\circ}\text{C}$  and boiling point of water and melting point of wax.

$P_0$  and  $P_{100}$  can also be obtained from the graph.

#### Calculations

(i) Plot the graph as described already.

$$(ii) \quad t = \frac{P - P_0}{P_{100} - P_0} \times 100$$

#### Result

Standard result

Percentage error

#### Precautions

Same as in experiment 6.1

#### Oral Questions

1. Define the pressure coefficient. Mention its unit. What is its effect on gases?

to fill the dry air in the glass bulb of

thermometer?

of mercury used in a gas thermometer?

## 7

**THERMAL CONDUCTIVITY****EXPERIMENT 7.1**

**Object**—To determine the thermal conductivity of a good conductor given in the form of a cylindrical bar.

**Apparatus**—Searle's apparatus, four thermometers, a boiler, measuring flask, vernier calliperse, metre scale, weight box, stop watch, burner etc.

**Description of Searle's apparatus**

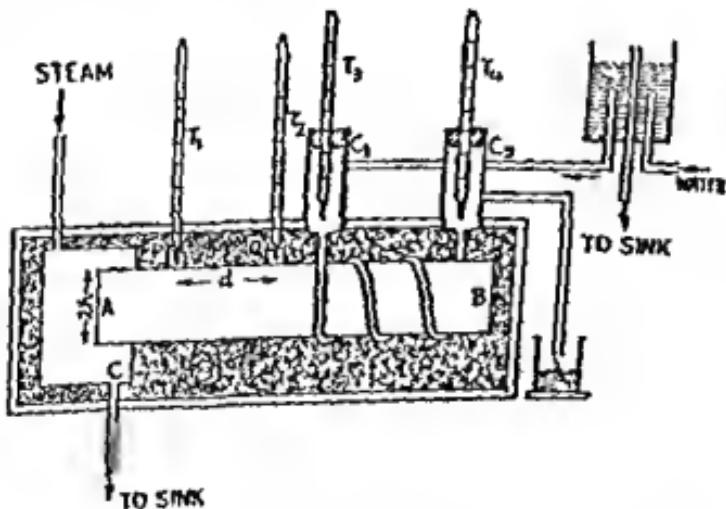


Fig. 7.1

A B is a metal rod whose coefficient of thermal conductivity is to be determined. The end A is enclosed in a steam chamber

in which steam can continuously be passed. The other end B is surrounded by the thin copper tubing in the form of spiral. Each end of this spiral terminates in the form of a cup and a thermometer is fitted in each of them through corks as shown in the fig.7.1. Two thermometers  $T_1$  and  $T_2$  are fitted into two holes in the rod A B at the points P and Q and in some good apparatus the bulbs of thermometers are in contact with rod by dipping them in mercury contained in small holes at P and Q which are at a distance of d cm. This whole system is enclosed in a wooden box which is packed with cotton wool.

### Theory

The end A is heated by passing steam continuously in the chamber C. Heat flows through the rod A B towards the end B. The temperature of thermometers at P and Q rises continuously. A constant flow of water is maintained in the copper spiral tubing. The temperature of inflowing and out-flowing water is recorded by the thermometers  $T_3$  and  $T_4$  respectively.

When steady state of temperature is reached, all the four thermometers record constant temperatures. The amount of heat flowing through the bar per second is absorbed by the circulating water at the end B. Let m gm. be the mass of water flowing in t seconds and  $\theta_3$  and  $\theta_4$  be the temperatures recorded by the thermometers  $T_3$  and  $T_4$  fitted in the cups  $C_1$  and  $C_2$  at the entrance and exit of the spiral tubing respectively.

The heat taken up by water per second

$$Q = \frac{m}{t} (\theta_4 - \theta_3) \quad \dots\dots(1)$$

But the amount of heat Q flowing per second through the bar is given by

$$Q = K \cdot a \cdot \frac{(\theta_1 - \theta_2)}{d} \quad \dots\dots(2)$$

Where  $K$  = the coefficient of thermal conductivity

$a$  = area of cross-section of the rod A B

$\theta_1$  and  $\theta_2$  are temperatures recorded by thermometers at P and Q at a distance of d cm.

Equating (1) and (2), we have

$$K \cdot \frac{\pi}{d} \cdot \frac{(T_1 - T_3)}{l} = \frac{m}{t} \cdot (T_4 - T_3)$$

$$\text{or } K = \frac{m \cdot (T_1 - T_3) \cdot d}{t \cdot \pi \cdot (T_4 - T_3)}$$

### Coefficient of thermal conductivity

It is defined as the quantity of heat flowing per second through unit area of cross-section of an element of the material of unit thickness, when the difference of temperature between faces is unity. In C. G. S. system its unit is calories per sec sq. cm. per temperature gradient of  $1^{\circ}\text{C}$  per cm. Its dimensions are  $M^1 L^1 T^{-2} \theta^{-1}$ .

### Procedure

1. Measure the diameter of the experimental rod at four points with the help of a vernier calliperse.
2. Measure the distance  $d$  between the points P and Q with metre scale.
3. Carefully insert the thermometer  $T_1$ ,  $T_2$ ,  $T_3$  and  $T_4$ .
4. Pass the steam in the steam chamber C from a boiler.
5. The inlet of the copper tubing is connected to a constant level water reservoir to have a constant flow of water through spiral.
6. When steady state of temperature is reached, wait for 5 to 10 minutes and then note down the temperatures  $\theta_1$ ,  $\theta_2$ ,  $\theta_3$  and  $\theta_4$  from the thermometers  $T_1$ ,  $T_2$ ,  $T_3$  and  $T_4$  respectively.
7. Quantity of water flowing out in a known time  $t$  seconds is collected in a clean beaker. Measure its volume by a measuring flask.
8. Calculate  $K$  with the help of the formula (4).

S. No.	M. S. reading	Vernier Scale reading	Diameter of the rod
1			
2			
3			
4			
5			

	Mean value of diameter	cm
1. radius of the rod $r =$	cm	cm
2. The distance between $T_1$ and $T_2$ , d	-	cm
3. Temperature recorded by thermometer	$T_1, \theta_1 =$	°C
4.	" "	°C
5.	" "	°C
6.	" "	°C
7. Volume of water collected inside the beaker	-	cc
8. Time for which water is collected, t	-	sec

### **Calculus**

#### **Map of water collection**

$$k = \left(\frac{m}{t}\right) \frac{(F_1 - F_2 + d)}{g^2 (F_1 - F_2)}$$

$$R = \frac{m}{e} = 1.3 \text{ pm} \cdot \text{sec}$$

$$K = \frac{1.3(0.5 - 37.2) \times 9.53}{3.142 \times 1.26 + 1.26 \times 36.2 + 36.2} = 1$$

~~Log 1.3 = 0.1139~~

卷之三

Add 24234

卷之四

卷之二

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$\log 1.2 = 0.085$

卷之三十一

402 *Journal*

Applying T<sub>4</sub>44-144

**Result**

The coefficient of thermal conductivity of a rod of a given metal = 0.8596 calories/sec/sq.cm/1°C/cm.

Standard result =

Percentage error =

**Precautions**

1. The thermometers  $T_1$  and  $T_2$  must touch the rod or contact can be ensured by putting some mercury in the small holes drilled at the points P and Q.
2. The thermometers  $T_3$  and  $T_4$  should be inserted into the cups  $C_1$  and  $C_2$  up to the extent that they are well in water.
3. More accurate thermometers having the least count  $0.2^\circ\text{C}$  should be used.
4. The flow of water through the spiral should be sufficiently slow and regular.
5. Temperatures should be recorded after 5 to 10 minutes of reaching in the steady state of temperature.

**Oral Questions**

1. Define the coefficient of thermal conductivity. State its unit and dimensions.
2. Explain the steady state of temperature.
3. Why the box is packed with cotton and wool?
4. Explain the phenomenon of conduction of heat?
5. Why the flow of water in the spiral is required to be very slow?
- c. What are the possible sources of error in this experiment?

## NEWTON'S LAW OF COOLING

---

When a hot body is left to cool, it loses its heat by the process of radiation, convection and conduction. In case the process of radiation is significant and losses due to conduction and convection are negligible the Newton's law of cooling holds true provided the difference between the temperature of the hot body and that of surroundings does not exceed  $60^{\circ}\text{C}$  or  $70^{\circ}\text{C}$ . It is a special case of more general law, i. e., the Stefan's law which is true for all ranges of temperature difference between the hot body and the surroundings.

### Newton's law of cooling

It state that rate of cooling of a body is directly proportional to the excess of its temperature over that of surroundings provided the excess is not large. In short we can write—

*Rate of cooling  $\propto$  excess of temperature*

Suppose the temperature of a body falls from  $\theta_1$  to  $\theta_2$  in 1 second and the temperature of the surroundings is  $\theta$ .

$$\text{Rate of cooling} = \frac{(\theta_1 - \theta)}{t} \text{ calories per sec}$$

where  $w$  is the thermal capacity of the body

The average temperature of the body during this interval of 1 second =  $(\frac{\theta_1 + \theta_2}{2})^{\circ}\text{C}$

The excess of temperature =  $(\frac{\theta_1 + \theta_2}{2} - \theta)^{\circ}\text{C}$

$\therefore$  According to Newton's law of cooling, we have

$$\frac{w(\theta_1 - \theta_2)}{t} \propto (\frac{\theta_1 + \theta_2}{2} - \theta)$$

Since  $w$  is constant for that body, hence

$$\frac{\theta_1 - \theta_2}{t} \propto \left( \frac{\theta_1 + \theta_2}{2} - \theta \right)$$

i. e., the rate of fall of temperature is directly proportional to the excess temperature. In fact to verify the Newton's law of cooling this thing is shown to hold true. It can also be written as

$$\frac{d\theta}{dt} \propto \text{excess of temperature}$$

Where  $\frac{d\theta}{dt}$  = rate of fall of temperature

$$\frac{d\theta}{dt} = K \text{ excess of temperature} \quad (K = \text{constant})$$

### EXPERIMENT 8.1

Object—Verify Newton's law of cooling by plotting a cooling curve for a liquid.

Apparatus—Newton's law of cooling apparatus (it consists of a double walled vessel with a lid containing a calorimeter with stirrer), two thermometers reading up to  $\frac{1}{10}^{\circ}\text{C}$ , stop watch, heater or burner etc.

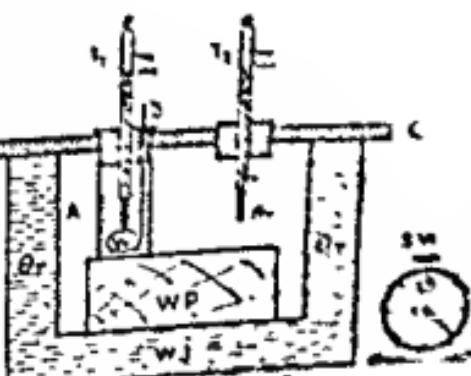
Formula—As we have already obtained from Newton's law of cooling that

$$\frac{d\theta}{dt} = K \text{ excess of temperature}$$

Where  $K = \text{constant}$

$$\frac{d\theta}{dt} = \text{rate of fall of temperature}$$

Procedure



1. Heat water in a beaker up to its boiling point.

2. Transfer the boiling water to fill the calorimeter A up to  $3/4$  of its capacity. Put the calorimeter A in its place in the Newton's law of cooling apparatus as shown in the figure (8.1).  $T_1$  is thermometer  $T_1$ .

fitted to record the temperature of cooling water and S is the stirrer.

3. Stir water continuously and take down the temperature of water at the interval of every half minute or one minute.

4. Plot a graph between the temperature and time taking a suitable scale. Temperature and time are taken along the y-axis and the x-axis respectively as shown in the figure 8·2.

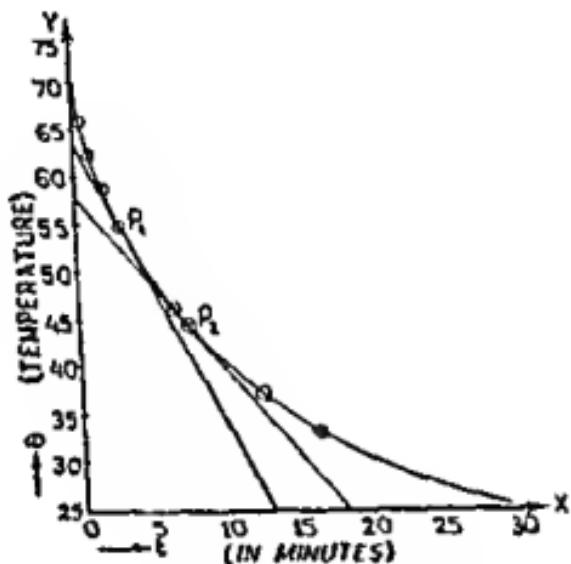


Fig. No. 8·2

5. Draw a number of tangents at the points P<sub>1</sub>, P<sub>2</sub> and so on. The tangents at different points gives the rate of fall of temperature corresponding to those points. Determine the excess of temperature at these points.

6. Now plot a graph between this excess of temperature and rate of fall of temperature, i. e.,  $\frac{d\theta}{dt}$  taking excess of temperature x-axis and  $\frac{d\theta}{dt}$  along the y-axis as shown in the

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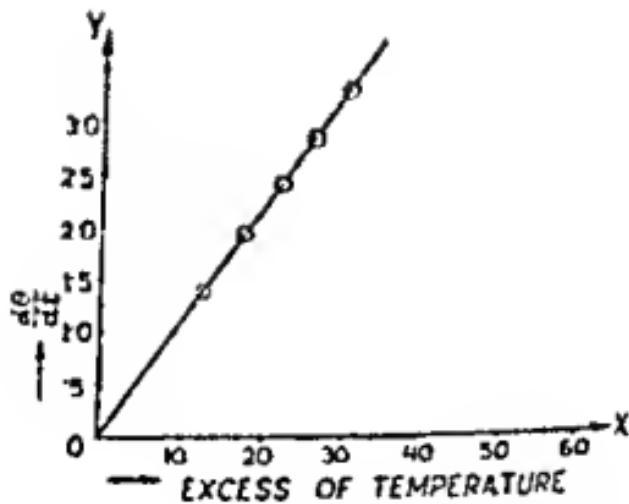


Fig. 8.3

**Observations**

S. No.	1	2	3	4	5	—	—	—
Time	0'	$\frac{1}{2}'$	1'	$1\frac{1}{2}'$	2'	—	—	—
Temperature	0°C	°C	°C	°C	°C			

Table from graph of fig. 8.2.

S.No.	Room temp.	Temp. of cooling water	Excess of temperature	Angle of the slope of tangent $\frac{ds}{dt} = \tan \theta$
1	.... °C	°C	°C	.....
2	" °C	°C	°C	.....
3	" °C	°C	°C	.....
4	" °C	°C	°C	.....
5	" °C	°C	°C	.....
6	" °C	°C	°C	.....
7	" °C	°C	°C	.....

### Calculations

$\frac{d\theta}{dt}$  is determined from the table of natural tangents. For a particular value of  $\frac{d\theta}{dt}$  we measure the angle between the tangent at that point of the curve in figure 8.2 and x-axis.

$$\frac{d\theta}{dt} = \frac{\text{Intercept cut by tangent on y-axis}}{\text{Intercept cut by tangent on x axis}}$$

### Result

The graph between  $\frac{d\theta}{dt}$  and excess of temperature comes to be a straight line which proves that the rate of cooling is directly proportional to the excess of the temperature.

If we calculate the ratio of  $\frac{d\theta}{dt}$  and excess of temperature which gives a constant K, this also proves the Newton's law of cooling.

### Precautions

1. The water should be stirred constantly.
2. Thermometers should read up to  $0.1^{\circ}\text{C}$ .
3. The curves plotted should be smooth. They should pass through the mean positions and if points are left, they should be on both sides of the curve almost in equal number and almost at the equal distances.

## EXPERIMENT 8.2

**Object**-To determine the specific heat of a liquid by Newton's law of cooling method.

**Apparatus**-Newton's law cooling apparatus (a double walled vessel containing two identical calorimeters), Two thermometers, stop watch, pipette, balance, weight box, given liquid, burner or heater,

### Theory

If two identical calorimeters contain equal volumes of two different liquids, the outer surfaces of the calorimeters are of the

same nature and both are cooled under same conditions, then the rates of cooling are equal.

Suppose two calorimeters of same size contain water and liquid and these are cooled from temperature  $\theta_1$  to  $\theta_2$  during the intervals  $t_1$  and  $t_2$  seconds respectively. Then

$$\text{Rate of cooling of water} = \text{Rate of cooling of liquid}$$

$$\text{Rate of cooling of water} = \frac{(m_1 + W)(\theta_1 - \theta_2)}{t_1} \text{ calories/sec}$$

$$\text{Rate of cooling of the liquid} = \frac{(m_2 S + W')(θ_1 - θ_2)}{t_2} \text{ calories/sec}$$

$$\therefore \frac{(m_2 S + W')(θ_1 - θ_2)}{t_2} = \frac{(m_1 + W)(θ_1 - θ_2)}{t_1}$$

$$\text{Or } S = \frac{1}{m_2} \left[ \frac{t_2}{t_1} (m_1 + W) - W' \right]$$

Where  $S$  = The specific heat of the liquid

$W$  = Water equivalent of the calorimeter containing water.

$W'$  = Water equivalent of the calorimeter containing liquid.

$m_1$  = Mass of certain volume of water taken.

$m_2$  = Mass of equal volume of liquid taken.

### Procedure

1. Weigh two identical clean calorimeters separately and calculate their water equivalents (mass  $\times$  specific heat = water equivalent of a body). Blacken them from outside.

2. Heat water and liquid in two separate beakers in a common bath up to  $70^\circ\text{C}$  or  $80^\circ\text{C}$ . Transfer equal volume of water and liquid into two identical calorimeters with the help of clean pipettes.

3. Put these calorimeters in their positions inside the thermos apparatus as shown in the figure 3.4. Press a thermometer in each apparatus so that the bulb is just above the liquid. Thermometers are also provided in

5. With the help of a stop watch note down the temperature of water and liquid alternately after every  $\frac{1}{4}$  minute till the temperature fall just  $5^{\circ}\text{C}$  to  $10^{\circ}\text{C}$  above the room temperature.

6. Note down the temperature of surroundings. It is better to note the temperature of surroundings at the beginning of the experiment also and then to find the mean of the two.

7. Weigh the two calorimeters separately with their contents.

8. Plot the cooling curves for water and liquid on the same graph paper taking the suitable scales. Time is taken along the x-axis and temperature along the y-axis.

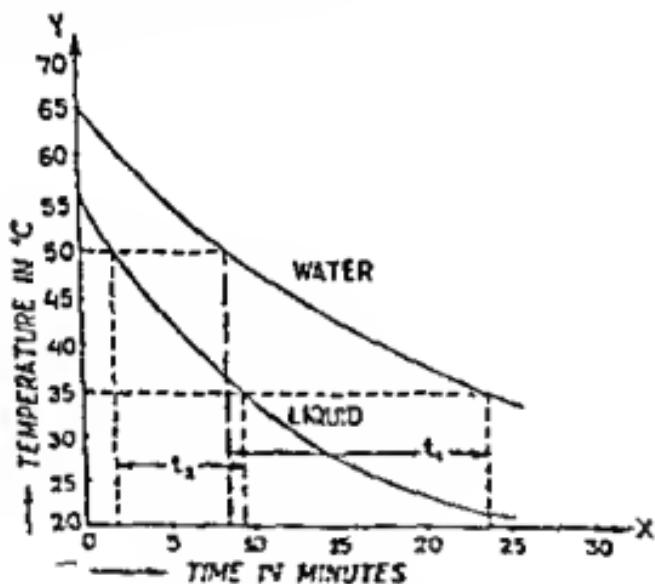


Fig. 8.4

9. From these curves, the time taken by water and liquid in cooling through the same range of temperature is noted.

10. Calculate the specific heat of the liquid using the formula given.

**Observations**

1. Mass of the first calorimeter = gm.  
 2. Mass of the second calorimeter = gm.  
 3. Mass of the first calorimeter + water = gm.  
 4. Mass of the second calorimeter + liquid = gm.  
 5. Room temperature in the beginning = °C  
 6. Room temperature at the end of the experiment = °C

S. No	Time, in minutes	Temperature of water	Temperature of liquid
1			
2			
3			
4			
5			
6			

**Calculations**

Water equivalent of first calorimeter,  $W_1 = m_1 s_1 \approx$  gm.

" " second " ,  $W_2 = m_2 s_2 \approx$  gm.

( $s_1$  is the specific heat of the material of calorimeter)

Mass of water  $\approx (1 - 1) \approx$  gm.

Mass of liquid  $\approx (1 - 2) \approx$  gm.

Time taken by water cooling from  $\theta_1^{\circ}$  to  $\theta_2^{\circ}$  = minutes

" " " liquid " " = minutes

$$S = \frac{1}{m_2 t_1} \left[ \frac{t_2}{10} (m_1 + W) - W_1 \right]$$

$$= \frac{1}{20 \cdot 10} \left[ \frac{7}{10} (25.85 + 10.49 \times 0.1) - 10.26 \times 0.1 \right]$$

$$= \frac{1}{20 \cdot 10} \left[ \frac{7}{10} \times 26.90 - 1.026 \right]$$

$$= \frac{1}{20 \cdot 10} [ 18.83 - 1.026 ]$$

$$= \frac{17.80}{20 \cdot 10} \quad \begin{matrix} \log 17.80 = 1.2504 \\ \log 20 \cdot 10 = 1.3032 \end{matrix}$$

$$\text{Diff.} = \overline{T}^{\prime} 9472$$

$$\therefore S = \text{Antilog } \overline{T}^{\prime} 9472$$

$$= 0.8855$$

$$= 0.89$$

### Result

Specific heat of a given liquid =

Standard result =

Percentage error =

Precautions—Same as in experiment 8.1

### Oral Questions

1. State Newton's law of cooling. What are its limitations?
2. Explain the rate of cooling and how do you measure it?
3. What is radiation? What are the factors governing radiation?
4. Explain the nature of surface pertaining to radiation.
5. Define the terms specific heat and water equivalent.
6. What do you mean by identical calorimeters with respect to radiation?
7. Can you find specific heat of a solid by the method of Newton's law of cooling?

## COMPOUND MICROSCOPE

**Compound microscope**—It consists of a brass tube having an objective at one end and an eye-piece at another end. The eye-piece can be moved in and out of the microscope tube. Both, the objective and the eye-piece, are convex lenses or in case of superior instruments combination of the lenses behaving as convex lens where the defects like chromatic and spherical aberrations are eliminated or reduced considerably.

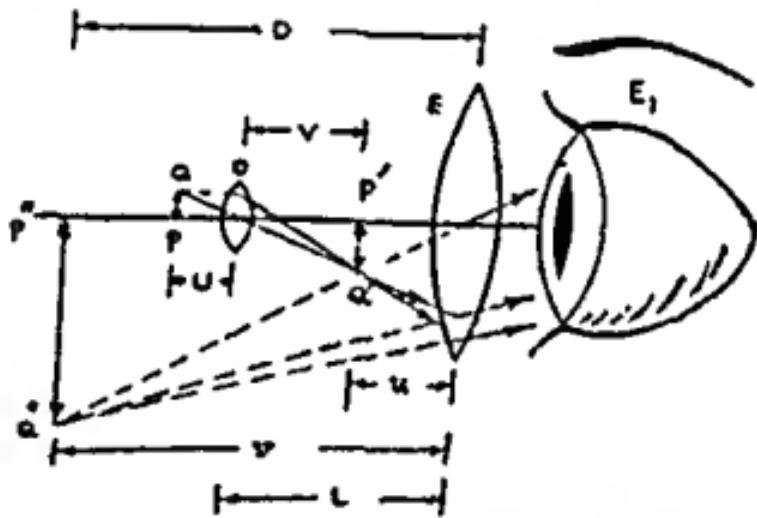


Fig. 9-1

As shown in the fig. 9-1  $PQ$  is an object in front of the objective  $O$  and its real, inverted and enlarged image is formed at  $P'Q'$ .  $P'Q'$  behaves as an object for the eye-piece and its virtual, upright and enlarged image is formed at  $E_1$ . The final image is magnified and inverted with respect to the object under observation.

**Magnifying power** of a microscope is defined as the ratio of the angle subtended by the image at the eye to the angle subtended by the object at the eye when the object is also at the least distance of distinct vision,  $D$ .

$$\begin{aligned} M &= \frac{P'Q'/D}{PQ/D} \\ &= \frac{P'Q'}{PQ} \\ &= \frac{P'Q'}{PQ} \times \frac{P'Q'}{PQ} \end{aligned}$$

Therefore  $M = \frac{v}{u} \times \frac{v}{u}$  (Because  $\frac{1}{D} = \frac{v}{u}$ ) .... .(1)

For a convex lens, we have

$$-\frac{1}{f} = \frac{1}{v} - \frac{1}{u}$$

Multiplying by  $v$  throughout, we get

$$-\frac{v}{f} = \frac{v}{v} - \frac{v}{u}$$

$$\text{or } \frac{v}{u} = 1 + \frac{v}{f} \quad \dots .(2)$$

Since  $v=D$ ,  $f=f_e$  (for eye-piece), and  $U$  is almost equal to the focal length of the objective, i.e.,  $f_o$ . Therefore (1) becomes

$$M = \frac{v}{f_e} \left( 1 + \frac{D}{f_e} \right) \quad \dots .(3)$$

### EXPERIMENT 9.1

**Object**—To determine the magnifying power of a microscope.

**Apparatus**—A compound microscope, scale, graph paper etc.

#### Theory

$$M = \frac{\text{Angle subtended by the image at the eye}}{\text{Angle subtended by the object when it is also at the distance } D}$$

$$= \frac{P'Q'/D}{PQ/D}$$

On a scale if  $P'Q' = N$  divisions

and  $PQ = n$  division

$$\text{Then } M = \frac{N}{n}$$

#### Procedure

- Take a graph paper and colour one of the small division with red or blue ink.

# 10

## ASTRONOMICAL TELESCOPE

### Astronomical telescope

It is used for observing heavenly bodies like planets and stars. It consists of a brass tube with an objective at one end and an eye-piece at the other end. The eye-piece can be moved in and out. Both the objective and the eye-piece are either convex lenses or combination of lenses behaving as convex lenses. Unlike the microscope the objective of a telescope is of larger focal length.

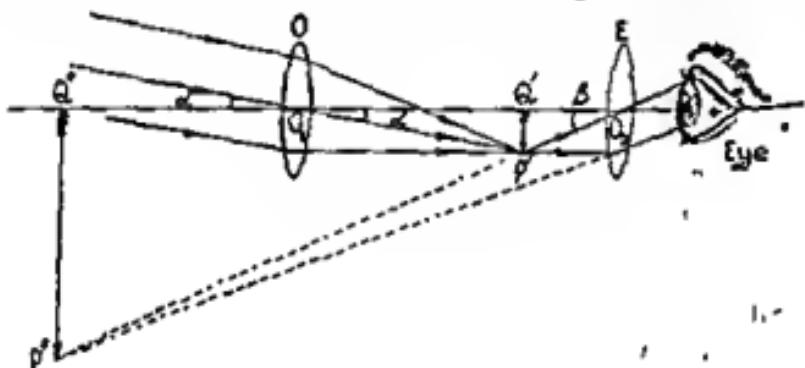


Fig: 10-1

As shown in the (fig. 10-1) O and E are the objective and the eye-piece coaxially mounted in a brass tube. The parallel beam of rays coming from the distant object forms an inverted, real and diminished image  $P'Q'$  in the focal plane of the objective O.  $P'Q'$  behaves as an object for the eye-piece E and its virtual, upright and magnified image is formed at  $P''Q''$ . The final image is inverted with respect to the object under observation.

**Magnifying power**--It is defined as the ratio of the angle subtended by the image at the eye to the angle subtended by the object at the eye. But the object is at such a great distance that the angle subtended by the object at the eye is almost equal to the angle subtended by the object at the objective.

According to the (fig. 10-1)  $\beta$  and  $\alpha$  are respectively the angle subtended by the image at the eye and the angle subtended by the object at the objective.

$$\therefore \text{Magnifying Power} = \frac{\angle \beta}{\angle \alpha}$$

since  $\beta$  and  $\alpha$  are very small angles

$$\therefore M = \frac{\tan \angle \beta}{\tan \angle \alpha}$$

$$\begin{aligned} &= \frac{P'Q'/Q'O_2}{P'Q/Q'O_1} \\ &= \frac{Q'O_1}{Q'O_2} \\ &= \frac{F}{f} \end{aligned}$$

Where  $F$  and  $f$  are the focal lengths of the objective and the eye-piece respectively.

### EXPERIMENT 10-1

**Object**—Determine the magnifying power of a telescope.

**Apparatus**—A telescope, a scale, measuring tape etc.

**Theory**—Let  $PQ$  be the object and the angle subtended by it at the objective is  $\alpha$ . The final image  $P''Q''$  subtends the angle  $\beta$  at the eye.

$$M = \frac{\angle \beta}{\angle \alpha}$$

As shown in the fig. (10-2) there is a telescope  $T$  mounted on a vertical stand and a vertical scale is fixed on a wall at a distance  $D$  from the telescope. Some divisions on the scale are observed with the help of the telescope with one eye and at the same time with the help of another eye. It is estimated that how many divisions are covered on the vertical scale by these magnified divisions.

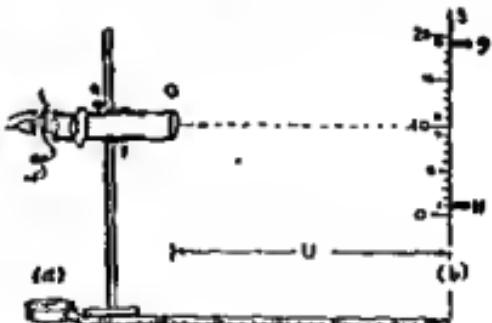


Fig. 10-2

Suppose the number of divisions observed through the telescope are  $n$  and the number of divisions covering them when observed directly are  $N$ . If  $d$  is the span of each division, then

$$\angle \beta = \frac{Nd}{D}$$

$$\text{and } \angle \alpha = \frac{nd}{D}$$

$$\text{Hence } M = \frac{N}{n}$$

#### Procedure

1. Place the telescope mounted on a vertical stand at a distance about 5 to 7 metres from a vertical scale fixed on a wall.
2. Adjust the eye-piece such that cross-wires are clearly visible.
3. Now see the scale with one eye through the telescope and concentrate on certain number of divisions, say  $n$ . With the other eye see the scale directly and count the number of divisions which coincide with the magnified  $n$  divisions. Suppose these are  $N$  in number.
4. Repeat the experiment with different number of  $n$  divisions.
5. Repeat the experiment with different distances from the scale.

#### Observations

S. No.	Distance of the scale from the telescope	No. of divisions seen through the telescope $n$	No. of divisions seen directly $N$	$M = \frac{N}{n}$
1	315 cm	1	8	8
2	"	2	14	7
3	"	3	23	7.6
4	535 cm	1	7	7
5	"	2	15	7.5
6	"	3	20	6.6
7	700 cm	1	6	6
8	"	2	13	6.5
9	"	3	21	7

**Calculations**

$$M = \frac{8}{1} = 8$$

**Result**

Magnifying power of a given telescope =

**Precautions**

1. The eye should be kept near the eye-piece.
2. The divisions marked on the scale must be clearly visible when seen directly with the naked eye.

**Oral Questions**

1. What is the construction of astronomical telescope ?
2. What are the different types of telescopes ?
3. Explain the working of an astronomical telescope. What is the nature of the image observed ?
4. Define the magnifying power of the telescope.
5. How do you differentiate a telescope from a microscope ?
6. Suggest how a telescope of larger magnifying power can be constructed.

# 11

## RESONANCE TUBE

**Object**—Determine the velocity of sound in air at  $0^{\circ}\text{C}$  by resonance tube and also determine the end correction of the resonance tube by finding the first and second resonance lengths.

**Apparatus**—Resonance tube, vernier callipers, A rubber pad, a thermometer, set squares, three tuning forks of frequencies 512,480,427 or any other combination.

**Theory**—(i) At resonance, i.e. when loud sound is heard, frequency of air column = frequency of tuning fork ( $n$ ).

(ii) Water level serves as a closed end of the tube and it serves two purposes—

(a) Reflection of waves takes place at the water level.

(b) Water level can be raised or lowered to adjust the length of air column to achieve resonance.

(iii) Antinode is formed above the open end at a distance  $x$ . If  $l_1$  and  $l_2$  are the first and second resonance lengths obtained with a fork of frequency  $n$ ,

$$l_1 + x = \frac{\lambda}{4}$$

$$\text{and } l_2 + x = \frac{3\lambda}{4}$$

$$(iv) \text{ Hence } x = \frac{l_2 - 3l_1}{2} \text{ (End correction)}$$

(v) The velocity  $v_t$  at room temperature ( ${}^{\circ}\text{C}$ ) is given by  $v_t = 2n(l_2 - l_1)$

(vi) If  $V_0$  = Velocity of sound at  $0^\circ\text{C}$ , then

$$\frac{V_1}{V_0} = \left(\frac{T}{T_0}\right)^{1/3} = \left(\frac{273+t}{273}\right)^{1/3}$$

$$\text{So that } V_0 = V_1 \left(\frac{273}{273+t}\right)^{\frac{3}{2}}$$

(vii) Also approximately  $x \approx 3D$ , where  $D$  is the inner diameter of the resonance tube.

#### Procedure--

1. Set the resonance tube vertical using a plumb line and the levelling screws at the base of the apparatus. Fill the reservoir and the resonance tube partly with water.
2. Place the thermometer bulb into the mouth of the tube

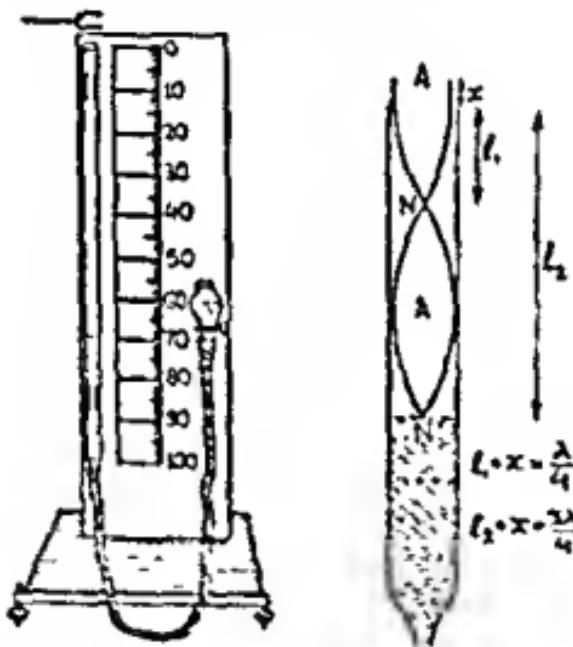


Fig. 111

and note the temperature. See that the bulb does not dip into water.

3. Holding the tuning fork by the stem, strike it gently on the rubber pad and place it horizontally just above the open end

of the tube so that the prongs vibrate in the vertical plane and do not touch the edge of the tube.

*Note:—The end A of the prong of the fork should be at the centre*

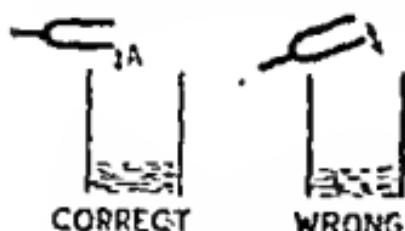


Fig. 11.2

*of the mouth of the tube. If the fork is not perfectly horizontal, the waves sent downwards by it will be reflected from the walls of the tube instead of from the water surface.*

4. Lower the reservoir and using the pinchcock, adjust the length of air column so that the maximum possible sound is heard. Now resonance has been achieved. Measure the length of air column. This is  $l_1$ . Measure  $l_1$  twice, once while lowering the level of water and again while raising the level of water.

5. Further lower the reservoir. Again maximum sound will be heard when length of air column becomes slightly greater than  $3l_1$ . This is  $l_2$ . Measure  $l_2$  twice, once while lowering the level of water and again while raising the level of water above the position obtained.

6. Repeat the experiment with the second and the third tuning forks. Calculate velocity of sound at  $t^\circ\text{C}$  and  $0^\circ\text{C}$  by eqns. (i) and (ii) respectively.

7. Calculate the end correction by eqn. (iv) and verify it by eqn. (viii). Measure the internal diameter of the tube with inside calipers in two positions at right angles.

S. No.	Frequency of fork	Upper resonance point			Lower resonance point			$I_2 - I_1$
		Reading of water level		Mean	Reading of water level		Mean	
		Falling level	Rising level	$h$	Falling level	Rising level	$I_2$	
1.	$n_1 = 512$ v/s	cm	cm	cm	cm	cm	cm	33.6 cm
2.	$n_2 = 480$ v/s	—	—	—	—	—	—	—
3.	$n_3$	—	—	—	—	—	—	—

V.C. of vernier scale =  $\frac{\text{The smallest division on main scale}}{\text{Total number of divisions on V. scale}}$

$$= \dots \dots \dots \text{cm}$$

$$\text{Zero error} = \dots \dots \dots \text{cm}$$

$$\text{Zero correction} = \dots \dots \dots \text{cm}$$

$$\text{Internal diameter of tube in one direction} = \dots \text{cm}$$

$$\text{", " ", " } \perp \text{ direction} = \dots \text{cm}$$

$$\text{Mean internal diameter of the tube D} = \dots \text{cm}$$

### Calculation for $V_t$

$$1. V_t = 2 \times 512 \times 33.6$$

$$= 1024 \times 33.6$$

$$= 34410 \text{ cm/sec}$$

$$\log 1024 = 3.0103$$

$$\log 33.6 = 1.5263$$

$$\text{antilog } 4.5366$$

$$= 34410$$

$$2. V_t = 2 \times 480 \times \dots$$

$$= \dots \text{cm/sec}$$

$$3. V_t = \dots \text{cm/sec}$$

$$\text{Mean } V_t =$$

$$273 - 2.4362$$

$$- 3 - 2.4698$$

$$\hline$$

$$1.9664$$

$$\log \left( \frac{273}{273-T} \right)^{\frac{1}{2}} = 7.9412$$

$\log 215.2 = 2.5161$

Antilog 2.5161

$V = 332.0 \text{ metres/sec}$

$= 332.0$

Calculations for  $\pi$  (End correction)

S.	Fork of fork	Mean	Mean	$3l_1$	$l_2$	$3l_2$	$\pi = \frac{l_2 - l_1}{2}$	Mean $\cdot 3D$
		$l_1$ cm	$l_2$ cm	cm	cm	cm	cm	cm
1.								
2.								
3.								

### Result

Velocity of sound at 0°C (by Experiment) = .... Metres/sec

Standard result = 332.0 Metres/sec

Error =

Percentage Error = %

End correction  $\pi$  = ... cm

$\cdot 3D$  = ... cm

Difference = ... cm

### Precautions

1. The resonance tube should be set vertical using levelling screws.
2. A pinch cock should be used and when the pinch cock is closed, water level should not change.
3. Temperature of air in the tube should be measured and not the temperature of water.
4. The inner diameter of the tube should be determined in two mutually perpendicular directions.
5. The tuning fork should be held only from its stem so that frequency may not get affected.

6. The vibrating fork should be held perfectly horizontal, just above the open end of the tube and without touching the edge of the tube. The end of the prong has got maximum amplitude of vibration, so the end should be at the centre of the mouth of the tube.

7. The resonance should be obtained both for water level falling and rising in the tube, while determining  $l_1$  or  $l_2$ . The water level should be raised or lowered in small steps lest the resonance position should get missed.

8. Tuning forks of high frequencies e.g. 512, 480, etc. should be used. With forks of low frequencies, the second position of resonance is not obtained because  $l_2$  in their case would become larger than the whole length of the resonance tube.

9. The tuning fork should be kept vibrating all the time when the water level is made to rise or fall for determining the correct position of maximum loudness.

#### Modifications

### EXPERIMENT 11·2

**Object**—Find the frequency of a given fork using resonance tube, given the velocity of sound at 0°C 332 meters/sec.

**Hint** : First Calculate  $V_t = V_0 \left( \frac{273+t}{273} \right)^{\frac{1}{3}}$  where  $t$  is the room temperature

Then using the eqn.  $V_t = 2n(l_2 - l_1)$

$$n = \frac{V_t}{2(l_2 - l_1)}$$

So  $n$  can be calculated by determining  $l_1$  and  $l_2$  experimentally.

### EXPERIMENT 11·3

**Object**—Compare the frequencies of the two given tuning forks by using resonance tube.

**Hint**:  $V_t = 2n_1(l_2 - l_1) = 2n_2(l_2' - l_1')$

$$\therefore \frac{n_1}{n_2} = \frac{l_2' - l_1'}{l_2 - l_1}$$

So by finding the first and second resonance lengths with both the forks, the ratio of their frequencies can be calculated.

## EXPERIMENT II-4

**Object**—Determine the temperature coefficient of the velocity of sound using resonance tube. Given velocity of sound at 0°C 332 metres/sec.

Hint  $V_t = V_0 + \alpha t$  where  $\alpha$  is the temperature coefficient.

$$30 \quad e = \frac{V_t - V_0}{t}$$

$V_0$  is given and  $V_t$  can be determined experimentally, using the formula  $V_t = 2\alpha (l_1 - l_2)$

## **Oral Operations**

1. Why the tube is called resonance tube ? What is resonance and what is end correction ?
2. Do you find the velocity of sound in air, or in water or in the material of the tuning fork ?
3. Why is water used ? Will the velocity of sound be affected if instead of water, oil or mercury is used in the tube ?
4. When first and second resonance lengths are obtained, are the frequencies of the air column in both the cases, the same ? Are they equal to the frequency of fork in both the cases ?
5. Are the fundamental frequencies the same when first and second resonance lengths are obtained.
6. Can you obtain the third resonance length also ? If so, how many times will it be 1, ?
7. If the room temperature increases, will the values of  $l_1$  or  $l_2$  also increase or decrease or remain the same ?
8. What kind of waves are present in the tube-progressive or stationary ? Are they longitudinal or transverse waves ?
9. When the fork vibrates, what type of vibrations are these ?
10. How do you select the tuning fork for this experiment ? Should it be of high frequency or low frequency ? and why ?
11. Can this method be used to find the frequency of a fork ? So, which method is better for the determination of Frequency - Resonance method ?

# 12

## SONOMETER

**Object**—Determine the frequency of a given tuning fork with the help of a sonometer.

**Apparatus**—Sonometer with a wire stretched on it, a hanger with slotted half-kilo weights, a tuning fork, a striking pad of rubber, a light V shaped paper rider, a metre rod.

**Theory**—Transverse stationary waves are produced in the stretched string by pressing the stem of the vibrating fork against the surface of the sonometer board. Then length of the vibrating wire between the bridges is adjusted till frequency of vibration of wire becomes equal to that of fork. So resonance occurs and therefore amplitude of vibration of the string becomes very large at the antinodes. So a paper rider placed at the position of the antinode falls off the wire.

$$n = \frac{1}{2l} \sqrt{\frac{T}{m}}$$

Where  $n$  = the frequency of length  $l$  of the wire.

= the frequency of fork, at resonance.

$l$  = length of the wire between the bridges in cms measured on achieving resonance.

$T$  = the tension in dynes under which the wire is stretched.

$T = Mg$  dynes where  $M$  is the weight in gms. of the hanger and the half kilo weight placed on the hanger.

$m$  = mass per unit length of the wire

= volume per unit length of the wire  $\times$  density.

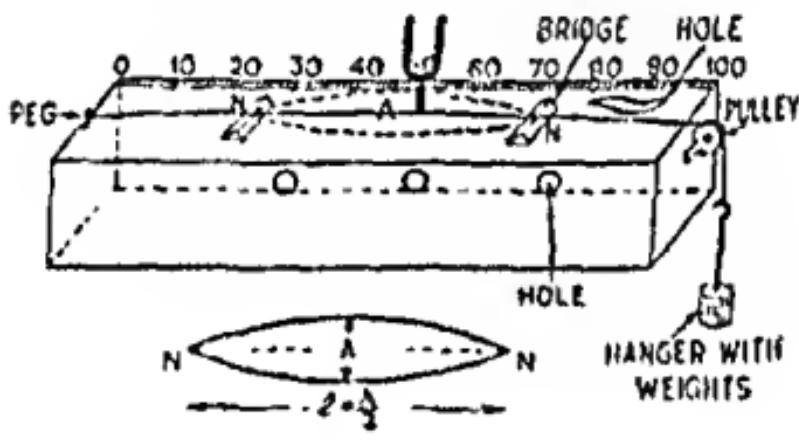
$m = \pi r^2 l \rho$  where  $r$  is the radius of the wire and  $\rho$  is the density.

$$\therefore n = \frac{1}{2l} \sqrt{\frac{T}{2\pi\rho}}$$

$n = \frac{1}{2lr} \sqrt{\frac{T}{\pi\rho}}$  But  $2r = D$ , the diameter.

$$\therefore n = \frac{1}{lD} \sqrt{\frac{T}{\pi\rho}}$$

Knowing  $D$ ,  $T$ , and  $\rho$ , and determining resonant length  $l$ , frequency  $n$ , can be calculated.



wire increases. The stem of the vibrating fork is to be kept pressed against the sonometer board all the time. For a particular length  $l$  of the wire between the bridges, the paper rider is thrown off the wire. It means now frequency of the wire has become equal to the frequency of the fork, so resonance has been achieved, as a result of which the amplitude of vibration at the antinode (middle of the wire) has become large and consequently the paper rider has been thrown off the wire. Now place a metre rod edge wise, along the wire and read the positions of the bridges, on this metre rod. So find the resonant length of the wire between the bridges.

5. Again find the resonant length of the wire, stretched under the same tension and with the same fork, but this time, the resonant length is to be obtained while decreasing the distance between the bridges.

6. Find the mean of the resonant lengths obtained in (4) and (5), for the same tension. Next change the tension in steps of 1 kgm each and every time find the mean of the resonant lengths obtained while first increasing the distance between the bridges and then while decreasing the distance between the bridges.

7. Then calculate, corresponding to every tension employed the frequency of the fork using the formula

$$n = \frac{1}{16} \sqrt{\frac{T}{\pi \rho}}$$

Then find the mean value of  $n$ .

Note:- 1. While recording the tension  $T$ , in the observation table, remember that weight of the hanger has been added to the weights, placed on the hanger, for the purpose of calculating  $T$ .

2. To read the resonant length of the wire, it would be advisable not to use the metre rod provided on the board. For accurate measurement, a metre rod may be placed edge wise along the wire and the position of the two bridges may be noted on this metre rod.

#### Observations

(a) Determination of diameter.

Outer diameter =  $\frac{D}{2} + \frac{t}{2}$  cm

Corrected diameter D = 51.4 cm (say)

#### (b) Determination of resonant lengths

Weight of mass of bridge, kg/cm	Increasing increasing			Distance decreasing			Mean resonant length (cm)
	Position of first bridge cm	Position of second bridge cm	Resonant length l' (cm)	Position of first bridge cm	Position of second bridge cm	Resonant length l" (cm)	
1. 15 kg/cm	...	...	...	...	...	...	...
2. 20 kg/cm	...	...	...	...	...	...	25.4 cm
3. 25 kg/cm	...	...	...	...	...	...	...

79

Material of the wire - Steel (say)

So density of the material of the wire = 7.8 gm per cc (for steel)  
(from tables)

### Calculations

1.

$$n = \frac{1}{ID} \sqrt{\frac{T}{\pi F}}$$

$$n = \frac{1}{25.1 \times 0.046} \cdot \left( \frac{2000 \times 980}{3.142 \times 7.8} \right)^{1/2}$$

$$n = \frac{1}{25.1 \times 0.046} \times (x)^{1/2}$$

$$\text{Where } x = \frac{2000 \times 980}{3.142 \times 7.8}$$

$$\text{So } n = 244.8 \text{ vib/sec.}$$

3.

4.

### Result

Mean  $n = \dots$  vib/sec.

Standard result = vib/sec.

Error = ... vib/sec.

% error =

$$\log 2000 = 3.3010$$

$$\log 980 = 2.9912$$

$$\text{Add } 6.2922$$

$$\log 3.142 = 0.4972$$

$$\log 7.8 = 0.8921$$

$$\text{Add } 1.3893$$

$$(1) - (2) = 4.9029$$

$$\text{i.e. } \log x = 4.9029$$

$$\text{and } \log x^{\frac{1}{2}} = \frac{4.9029}{2}$$

$$= 2.4514$$

$$\log 25.1 = 1.3997$$

$$\log 0.046 = \frac{2.6628}{0.0625}$$

$$(3) - (4) = 2.3889$$

$$\text{antilog } 2.3889 = 244.8$$

### Precautions

1. The wire should be uniform in diameter, free from links.

2. Start with a small length of the wire between the bridge and adjust it for unison by gradually increasing the length. This length should be checked by finding the resonant length again when the distance between the bridges is decreased.

3. Weight of the hanger must be included while calculating the tension.

4. The hanger should not be moving when resonant length is being determined.

5. The friction in the pulley should be the minimum possible, most negligible.

6. The paper rider must always be kept at the middle of the wire (i.e. at the position of the antinode), between the bridges.

7. Use a fork of smaller frequency. This would increase the accuracy by increasing the resonant length.

8. With large tension used, the resonant length will increase so the accuracy also increases. But tension applied must be within the elastic limit of the material of the wire.

#### Criticism of the method

There are many sources of error in the experiment.

1. The sonometer wire is not perfectly flexible. Due to its stiffness its frequency is greater if it were perfectly flexible.

2. The frequency of vibration of the wire may change due to the yielding of the supports, because yielding would then result in shifting the positions of nodes from the bridges.

3. The tension on both the sides of the bridge may not be the same.

4. The friction in the pulley causes  $T$  to be less than that actually applied. So the calculated frequency is more than the actual frequency.

#### Oral Questions

1. Define resonance, stationary waves, fundamental frequency and harmonics. What is sharp resonance and what is flat resonance?

2. Which method is better for determining the frequency of a fork—sonometer method or resonance tube method?

3. What type of vibrations are produced in a tuning fork? Where are the nodes and antinodes situated in a vibrating fork? On what factors does the frequency of a fork depends? What is the purpose of the stem? Of what materials the forks are made? Why are forks of frequencies 100, 200, ... not chosen for laboratory use?

4. Why is it better to have a thinner wire of lower Young's modulus and to stretch it with a large load? Is it necessary to stretch the wire horizontally? Which is better, horizontal or vertical arrangement? Can a rubber cord be used. Explain the principle of working in this experiment. What type of vibrations are produced in the string.

5. What is the function of the sounding board and of the bridges? Why the edges of the bridges should be sharp? Why is the box hollow and why holes are provided in it?

6. Explain the principle of the rider. Why should the rider be always kept at the middle of the wire between the bridges?

7. What are the sources of error in the experiment and what precautions are to be observed? What is the use of the sonometer?

8. On what factors does the frequency of a note emitted by a sonometer wire depend? How will the frequency change—

(i) if the tension is made four times?

(ii) if the area of cross-section of the wire increases four times?

(iii) if the radius of the wire increases four times, provided other factors remain the same in each case?

## EXPERIMENT 12·2

**Object**—Verify the laws of transverse vibrations of strings.

**(A) Verification of the law of length.**

**Apparatus**—Sonometer, hanger with weights, striking pad, paper rider, tuning forks of different frequencies say 256, 288, 320, 341, 384 etc. A metre rod to measure the resonant lengths.

### Theory

When  $T$  and  $m$  are const.

$$n \propto \frac{1}{l} \text{ or } n l = \text{constant}$$

Where  $T$ —the tension under which the wire is stretched.

$m$ —the mass per unit length of the wire.

$n$ —the frequency of vibration of length 1 cm of the wire.

### Procedure

1. Place suitable weights on the hanger so that the wire is stretched (use a load of 2·0 or 2·5 kgm).

2. Place a V-Shaped paper rider at the middle of the wire between the bridges.

3. Take the first fork of frequency  $n_1$ . Strike its tines against a rubber pad and press the stem of the vibrator against the sonometer board, simultaneously adjusting the length of the wire between the bridges till for a particular length, paper rider is thrown off the wire. Find this resonant length twice, first while increasing the distance between the bridges and then while decreasing the distance between the bridges. Find mean resonant length  $l_1$ .

4. Repeat the process with other tuning forks of frequencies  $n_2, n_3, \dots$  and find the mean resonant lengths  $l_2, l_3, \dots$  respectively. The tension is to be kept the same in all these observations and the wire is also not to be changed.

5. Calculate the products  $n_1 l_1, n_2 l_2, n_3 l_3, \dots$  etc. These would come out to be constant.

6. Draw a graph between  $n$  and  $\frac{1}{l}$ . It will be found to be a straight line passing through the origin.

#### Observations

Load including the hanger - 2 kgm (kept constant)

No. of forks	Frequency of the fork (n)	Resonant length obtained by		Mean resonant length (l)	from reciprocal tables $(\frac{1}{l})$
		increasing the distance between the bridges	decreasing the distance between the bridges		
1.	256 v/s				
2.	288 v/s				
3.	320 v/s				
4.	341 v/s				

#### Calculations

#### Result

- The product  $n l$  comes out to be constt.  
i.e.,  $n l = \text{constt.}$

2. The graph between  $n$  and  $\frac{1}{l}$  comes out to be a st. line. It also means that  $n \propto \frac{1}{l}$ , i.e., the frequency of vibration of a given wire ( $m = \text{constt.}$ ) stretched under constant tension ( $T = \text{constt.}$ ) is inversely proportional to its length. This is the law of length, which is verified.

### (B) The law of tension.

**Apparatus**—Sonometer with a wire stretched over it, hanger with weights, striking (rubber) pad, paper rider, a metre rod to measure the resonant lengths, one fork of a particular frequency, say 256.

### Theory

When  $l$  and  $m$  are constt.

$$n \propto \sqrt{T}$$

When  $n =$  the frequency of fixed length  $l$  of the given wire

$T =$  the tension in dynes under which the wire is stretched.

### Procedure

1. Take one fork only, of frequency,  $n_1$  (say). Start with 1 kgm load and under this tension  $T_1$ , find the mean resonant length  $l_1$  in unison with the fork.

2. Increase the tension in steps of  $\frac{1}{3}$  kgm, three or four times and thus find the resonant lengths  $l_2, l_3, l_4$  under tension  $T_2, T_3, T_4$  respectively, of the same wire and in unison with the same fork of frequency  $n_1$ . Then

$$n_1 = \frac{1}{2l_1} \sqrt{\frac{T_1}{m}} = \frac{1}{2l_2} \sqrt{\frac{T_2}{m}} = \frac{1}{2l_3} \sqrt{\frac{T_3}{m}} = \frac{1}{2l_4} \sqrt{\frac{T_4}{m}}$$

In second case, when the tension is  $T_2$ , if lengths were  $l_1$  instead of  $l_2$ , the frequency would have been  $n_1$  (say) instead of  $n_2$ . Using law of length,

$$n_2 l_1 = n_1 l_2$$

$$\text{i.e. } \boxed{n_2 = n_1 \times \frac{l_2}{l_1}}$$

$$\frac{n_1}{\sqrt{T_1}} = \frac{295.9}{35.73} = 7.640$$

$$\log 295.9 = 2.4711 \\ \log 35.73 = 1.5580 \\ \text{antilog } \overline{0.8831} \\ = 7.640$$

$$\frac{n_2}{\sqrt{T_2}} = \frac{337.2}{45.19} = 7.541$$

$$\log 337.2 = 2.5279 \\ \log 45.19 = 1.6505 \\ \text{antilog } \overline{0.8774} \\ = 7.541$$

### Result

Values of  $\frac{n}{\sqrt{T}}$  are found to be constt.

$$\text{So } \frac{n}{\sqrt{T}} = \text{constt. or } n \propto \sqrt{T}$$

Also graph between  $n \propto \sqrt{T}$  comes out to be a straight line. It also means  $n \propto \sqrt{\frac{l}{m}}$ , i.e., frequency of fixed length ( $l$ —constt.) of a given wire ( $m$ —constt.) is directly proportional to the square root of the tension under which the wire is stretched. This is the law of tension and it stands verified.

### (c) Verification of the Law of Mass

**Apparatus**—Spirrometer, hanger with slotted weights, a striking pad of rubber, a tuning fork of particular frequency (say) 256, a metre rod, three wires having different masses per unit length by virtue of their different materials or different diameters.

### Theory

$$n \propto \frac{1}{\sqrt{m}} \text{ when } T \text{ and } l \text{ are constt.}$$

where  $n$  is the frequency of vibration of fixed length  $l$  of the wire, whose mass per unit length is  $m$ .

$T$ —the tension under which the wire is stretched.

### Procedure

1. Stretch the first wire with a suitable load say  $T=2\text{kgm}$  and find its mean resonant length  $l_1$  which is in unison with a particular fork of frequency  $n_1$ . The wire is  $m_1$ .

2. Replace the first wire with the second one, whose mass per unit length is  $m_2$ . Find its length  $l_2$ , under the same tension  $T=2 \text{ kgm}$  and in unison with the same fork of frequency  $n_1$ . Similarly find the length  $l_3$  of the third wire (mass per unit length =  $m_3$ ), under the same tension  $T=2 \text{ kgm}$  and in unison with the same fork of frequency  $n_1$ .

$$\text{Then } n_1 = \frac{1}{2l_1} \sqrt{\frac{T}{m_1}} = \frac{1}{2l_2} \sqrt{\frac{T}{m_2}} = \frac{1}{2l_3} \sqrt{\frac{T}{m_3}}$$

length  $l_2$  of 2nd wire has got frequency =  $n_1$

its length  $l_1$ , under the same tension,  $T$ , would have

frequency =  $n_2$  (say)

Then applying law of length,  $n_2 l_1 = n_1 l_2$

$$\text{or } n_2 = n_1 \frac{l_2}{l_1}$$

$$\text{Similarly } n_2 = n_1 \frac{l_3}{l_2}$$

For  $n_1$ , substitute the frequency of the fork used. So  $n_2$ ,  $n_3$  are the frequencies of 2nd wire and 3rd wire respectively, calculated for fixed length  $l_1$ .

3. Next measure the radii of the wires used and knowing the densities of their materials, calculate the mass per unit length of each wire, using the formula

$$m = \pi r^2 \rho$$

Then calculate the products  $n_1 \sqrt{m_1}$ ,  $n_2 \sqrt{m_2}$ , and  $n_3 \sqrt{m_3}$

These are found to be constant.

4. Graph between  $n$  and  $\frac{1}{\sqrt{m}}$  will be a straight line.

#### Observations

Pitch of the screw gauge = cm

L. C. of the screw gauge = cm

## Measurement of diameters of the wires.

Density of Wire in gm/cc ( $\rho$ )	Diameter in cms										Mean diameter in cm (D)	Radius $r = \frac{D}{2}$	mass per unit length $m = \pi r^2 \rho$
1	2	3	4	5	6	7	8	9	10				
A	.....	.....	.....	.....	.....	.....	.....	.....	.....				$m_1 = \text{gm/cm}$
B	.....	.....	.....	.....	.....	.....	.....	.....	.....				$m_2 = \text{gm/cm}$
C	.....	.....	.....	.....	.....	.....	.....	.....	.....				$m_3 =$

## Measurement of resonant lengths of the wire

Load including the hanger = 2 kgm (kept constt.)

Frequency of the fork used =  $n_3 = 256$  vibrations/sec.

(kept constt.)

wire	$m$ in gm/cm	$\sqrt{m}$	$\frac{1}{\sqrt{m}}$	Resonant length with frequency $n_1$ increas. sing length	Decreas. sing length	Resonant length with frequency $n_2$ increas. sing length	Decreas. sing length	Mean resonant length (i) $l_1 = \dots \text{cm}$	Mean resonant length (ii) $l_2 = \dots \text{cm}$	frequency calcu- lated for $a \sqrt{m}$ $n_1 = \dots$	frequency calcu- lated for $a \sqrt{m}$ $n_2 = \dots$
A	$m_1$							$l_1 = \dots \text{cm}$	$l_2 = \dots \text{cm}$	$n_1 = \dots$	$n_2 = \dots$
B	$m_2$							$l_1 = \dots \text{cm}$	$l_2 = \dots \text{cm}$	$n_1 = \dots$	$n_2 = \dots$
C	$m_3$							$l_1 = \dots \text{cm}$	$l_2 = \dots \text{cm}$	$n_1 = \dots$	$n_2 = \dots$

## Calculations

## Result

The values of the product  $a \sqrt{m}$  have been found to be constant. It means  $a \sqrt{m} = \text{const.}$

$$\text{Or } n \propto \frac{1}{\sqrt{m}}$$

Also a graph between  $n$  and  $\frac{1}{\sqrt{m}}$  comes out to be a straight line.

It also shows that  $n \propto \frac{1}{\sqrt{m}}$ , i.e., the frequency of vibration

of fixed length of a wire stretched under constant tension is inversely proportional to the square root of the mass per unit length of the wire.

### Modifications

#### EXPERIMENT 12.3

Object—Determine the weight of the given brick. Given forks of different frequencies say 256, 288, 320 and 341.

$$\text{Hint: } n = \frac{1}{2l} \sqrt{\frac{T}{m}} \quad \dots(1)$$

Where  $T = Mg$  = the weight of the brick suspended

$$\text{So } n = \frac{1}{2l} \sqrt{\frac{Mg}{m}}$$

$$\text{Squaring } n^2 = \frac{1}{4l^2} \times \frac{Mg}{m}$$

$$\text{or } Mg = 4n^2 l^2 m \quad \dots(2)$$

With the tension due to the same brick, find the resonant lengths  $l_1, l_2, l_3, l_4$  with forks of frequencies  $n_1, n_2, n_3$  and  $n_4$ . Calculate  $m$ , the mass per unit length of the wire using the formula  $m = \pi r^2 \rho$  where  $r$  is the radius of the wire and  $\rho$  is the density of the material of the wire. Knowing  $m, l$  and  $m$ , find weight  $Mg$  of the brick, using relation.

#### EXPERIMENT 12.4

Object—Determine the density of the material of the sonometer wire. Given a fork of known frequency.

$$\text{Hint: } n = \frac{1}{2l} \sqrt{\frac{T}{m}} \quad \dots(1)$$

$$m = \pi r^2 \rho$$

$$\therefore n = \frac{1}{2l} \sqrt{\frac{T}{\pi r^2 \rho}}$$

$$\text{or } n = \frac{1}{2l} \sqrt{\frac{T}{\pi \rho}}$$

$$\text{or } n = \frac{1}{16} \sqrt{\frac{T}{\pi \rho}}$$

1. If  
m is known  
2. If T is known

$$\text{Squaring } n^2 = \frac{l^2}{D^2} \times \frac{T}{\rho}$$

$$\text{or } \rho = \frac{T}{l^2 D^2 \pi n^2} \quad \dots(2)$$

Where  $T$ —Mg dynes, Mg being the total load including that of the hanger. ( $M$  is in gms.)

$n$ —the frequency of the given fork used.

$D$ —Diameter of the sonometer wire in cms.

$l$ —resonance length of the wire in cms.

Resonant lengths at different tensions and for the same fork, are found out and then formula (2) used to determine  $\rho$ .

### EXPERIMENT 12.5

Object—Find the diameter of the sonometer wire and verify your result by measuring the diameter with screw gauge.

Hint : See Modification (2) above.

$$\text{From Equation (2), } D^2 = \frac{T}{\pi l^2 n^2 \rho}$$

$$\text{or } D = \frac{1}{nl} \sqrt{\frac{T}{\rho}}$$

Knowing  $n$ ,  $l$ ,  $T$ ,  $\rho$ , diameter  $D$  can be found out. For different sets, change the tension  $T$  and find the resonant length  $l$  every time for the same fork.

### EXPERIMENT 12.6

Object—Prove that  $\frac{T}{l^2} = \text{Constant}$ ,  $l$  being the length of the sonometer wire, always in unison with the same fork.

$$\text{Hint :— } n = \frac{l}{2l} \sqrt{\frac{T}{m}}$$

$$\text{Squaring } n^2 = \frac{1}{4l^2} \times \frac{T}{m}$$

or  $\frac{T}{l^2} = 4 n^2 m = \text{constt.}$  since  $n$  is constant if same fork is used and  $m$  is constant if wire is not changed. So find resonant lengths  $l_1$ ,  $l_2$ ,  $l_3$  or tensions  $T_1$ ,  $T_2$ , and  $T_3$  in unison

Show that  $\frac{T}{l_1^2} = \frac{T_2}{l_2^2} = \frac{T_3}{l_3^2} = \text{constt.}$

Also a graph between  $T$  and  $l^2$  will be a straight line.

### EXPERIMENT 12.7

Object—Compare the frequencies of two given tuning forks.  
Take at least three sets by taking three values of tension.

Hint :—  $n_1 = \frac{1}{2l_1} \sqrt{\frac{T}{m}}$  and  $n_2 = \frac{1}{2l_2} \sqrt{\frac{T}{m}}$

Dividing  $\left[ \frac{n_1}{n_2} = \frac{l_2}{l_1} \right]$ ;  $\frac{n_1}{n_2}$  has got no units it being a ratio.

## DEFLECTION MAGNETOMETER

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### EXPERIMENT 13.1

**Object**—Compare the magnetic moments of two magnets by setting the deflection magnetometer in Tan A position and using equal distance method (i.e. deflection method).

**Apparatus**—Deflection magnetometer, two given magnets, a metre rod.

#### Theory

When a magnetic needle is placed under the action of two perpendicular fields  $F$  and  $H$ , then in equilibrium the magnetic needle makes  $\angle A$  with one of them, say  $H$ , such that  $F \perp H$  (see  $\theta$  (tangent law)).

Let  $M_1$  and  $M_2$  be the magnetic moments of the two magnets whose half lengths are  $l_1$  &  $l_2$  respectively.  $F_1$  and  $F_2$  are the fields acting on the compass needle due to these magnets when they are successively placed at a distance  $d$  from the pivot of the compass needle, the position of the needle being end on with respect to the magnets.  $\theta_1$  and  $\theta_2$  are the mean deflections obtained in the needle due to the two magnets.

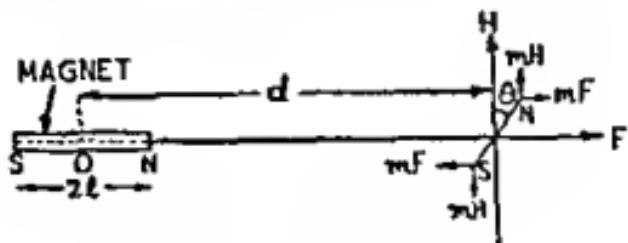
$$\text{Then } F_1 = \frac{2 M_1 d}{(d^2 + l_1^2)^{3/2}} = H \tan \theta_1$$

$$(u) F_2 = \frac{2 M_2 d}{(d^2 + l_2^2)^{3/2}} = H \tan \theta_2$$

$$\frac{F_1}{F_2} = \frac{(2 M_1 d)^2}{(2 M_2 d)^2} \times \frac{\tan \theta_1}{\tan \theta_2}$$

$$\therefore \frac{M_1}{M_2} = \frac{\tan \theta_1}{\tan \theta_2} \text{ if } l_1 = l_2 \text{ or the half lengths } l_1 \text{ & } l_2 \text{ of}$$

the magnets are so small that  $I_1$  &  $I_2$  are negligible compared with  $d^2$ .



Principle diagram  
Fig. 13·1

**Note—1.** In the principle diagram magnetic needle should be shown quite small in length compared with the magnet because only then fields acting on its poles can be taken as approximately equal to  $F$ , which is actually the field due to the magnet acting at the centre of the magnetic needle.

**2. The angle made by the magnetic needle with the field  $H$  should be marked as  $\theta$  in the principle diagram.**

#### Procedure

(a) **1<sup>st</sup> step**—First examine the apparatus given to you. See that the aluminium pointer is perpendicular to the magnetic needle and that the needle can rotate freely about its pivot. See that the magnets are not demagnetised and that their poles are correctly marked.

(b) **2<sup>nd</sup> step**—Setting the magnetometer in the A position.—Remove all magnets and magnetic substances and all conductors carrying electric current away from the apparatus. Place the magnetometer

with its arms along the East-West direction. To do so correctly place a metre rod (its edge should be perfectly straight) on top of the box and parallel to the metre rod fixed on the arms of the magnetometer. Then hold the magnetometer at the extreme ends of the arms and rotate it so that the aluminium pointer becomes parallel to the metre rod. This process may have to be repeated a number of times till, or looking from above downwards into the plane mirror of the box, it is found that all three, (i) the aluminium pointer (ii) the metre rod placed on top of the box, (iii) the metre rod fixed on the arms of the magnetometer, have become parallel among themselves.

Now rotate the compass box so that both the ends of the pointer read zero. Now the magnetometer is set in Tan A position.

3. Now place the magnet A on the East arm with its North pole pointing towards the needle. The magnetic axis of the magnet should be parallel to the metre rod fixed on the arm, i.e., it should be parallel to the arm and if the magnetic axis is produced, it should pass through the centre of the compass needle pivoted in the compass box. Distance of the magnet from the magnetic needle means the distance from the centre of the magnet to the centre of the magnetic needle. If distance of the end of the magnet from the magnetic needle is read, then to this distance, half the length of the magnet may be added to know the exact distance from the centre of the magnet to the centre of the needle. Adjust this distance so that the deflection is about  $40^\circ$ . Read both the ends of the pointer by keeping your eye vertically above the pointer so that the image of the pointer in the mirror below is covered by the pointer itself.

4. Now reverse the magnet pole to pole on the same arm so that South pole of the magnet points towards the needle. Keeping the mid. point of the magnet at same distance, read both ends of the pointer. This makes four readings.

5. Reverse the face of the magnet in the same very position id without changing the poles. Read both the ends of the pointer. This makes six readings.

6. Again reverse the poles having the same face above as in (5) and read both the ends of the pointer. This makes eight readings.

7. Now transfer the same magnet on the other arm, i.e., West arm and keeping the mid. point of the magnet at the same distance as on the East arm, repeat the above procedure and take eight readings. This makes sixteen readings for the same magnet A placed at the same distance d, for both the arms of the magnetometer. The mean  $\theta_1$  of these sixteen deflections gives the correct value of deflection.

8. Now remove the magnet A away from the apparatus. Place the magnet B in the same way and with its centre at the same distance and repeat the same procedure to note the sixteen deflections. Take the mean of these sixteen deflections. This is  $\theta_2$ . This forms one set of observation.

9. For the second set and the third set, change the distance and adjust it such that now the magnet A gives a deflection of  $45^\circ$  and  $50^\circ$  respectively in the second set and the third set, whereas it had given a deflection of  $40^\circ$  in the first set.

*Note—For the various sets, the distance should be either increased only or decreased only so that the deflections are recorded in some systematic order either in the decreasing order or in the increasing order. Also for various sets, changes in the distance should be uniform, so that uniform changes in the deflection of one magnet are obtained.*

10. Calculate  $\frac{M_1}{M_2}$  separately for each set and find the mean.

#### Observations

$$\text{Length of magnet A} = L \text{ cm. } l_1 = \frac{5}{12} L \text{ ... cm.}$$

$$\text{Length of magnet B} = L \text{ cm. } l_2 = \frac{5}{12} L \text{ ... cm.}$$

Since the pointer is permanently attached at right angles to the magnetic needle, therefore

Deflection of the pointer = Deflection of the magnetic needle

**Deflection of the pointer in degrees when the magnet is on the West Arm**

## Calculations

$$\frac{M_1}{M_2} = \frac{\tan \theta_1}{\tan \theta_2}$$

$$= \frac{\tan 48^\circ}{\tan 47^\circ} \quad \begin{matrix} \text{(use natural tangents)} \\ \text{tables} \end{matrix}$$

$$= \frac{1.1106}{1.0724}$$

$$\log 1.1106 = 0.0453$$

$$\log 1.0724 = 0.0302$$


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$$\frac{M_1}{M_2} = 1.035 \quad \text{Antilog } -0.0151$$

$$= 1.035$$

## Result

$$\text{Mean } \frac{M_1}{M_2} = \dots \dots \text{(Being a ratio, it has no units).}$$

## Precautions

1. The magnetometer should be placed on a rigid table preferably of stone so that it is not shaky and can not be disturbed by other experimenters working on other apparatus. Once set in the desired position, mark its boundary with a piece of chalk and do not hereafter disturb it during the experiment.
2. All magnetic substances and current carrying conductors should be removed away from the magnetometer before setting it and also these should be kept away, during the course of the experiment.
3. Do not measure the dimensions, e.g., length, breadth, etc. of the magnet during the experiment. The contact of vernier callipers, (being of steel) may change the magnetic moment of the magnet.
4. The magnet should be placed on the arms of the magnetometer such that its magnetic axis when produced, must pass through the centre of the magnetic needle.
5. The magnets should be labelled as A and B with ink. Also mark their mid-points and always measure the distances from the mid points of the magnets and NOT from their ends.
6. Tap the top of the compass box, with your finger gently and every time before taking a reading.
7. While reading the position of the pointer on the circular scale, the eye should be vertically above the pointer and in such a

position that the pointer covers its image in the plane mirror; otherwise an error will be made in noting the deflection. Deflection can be read correctly if you remember that it increases from the side of zero and not from the side of 90°.

8. The distance  $d$  should be so adjusted that the deflections are near about 45°, preferably the deflections obtained for a given magnet in the three sets should be nearly 40°, 45°, 50°. The central reading should be 45° and the other two should be equal and on either side of 45°.

9. Distance  $d$  should remain the same, for one set of observations, for both the magnets. Also  $d$  should be quite large so that the field due to the magnet, acting on the magnetic needle, may be more uniform.

#### Sources of error and their removal

1. The needle or the pointer may not be pivoted exactly at the centre of the circular scale. One end reads less and the other more, than the actual deflection. Hence read both the ends of the pointer and take the mean.

2. The poles of the magnet may not be symmetrically placed from the ends. So to eliminate the error on this account, turn the magnet from pole to pole and read both the ends of the pointer again.

3. The geometric axis and the magnetic axis of the magnet may not coincide. Hence the face of the magnet is reversed and the above readings repeated.

4. Zero of the metre-rod may not be coincident with the centre of the circular scale, i.e., where the needle is pivoted. So the readings are repeated on the other arm, with the magnet placed in similar position and at the same distance.

#### Criticisms of the method

1. The field  $F = \frac{2M d}{(d^2 + r^2)^{3/2}}$  due to the magnet acts only at the point, i.e., centre of the magnetic needle. The field acting on the North pole or the South pole can't be equal to  $F$ , the field at the centre, an assumption which we make in deriving the formula.

$F = \frac{2 \text{ Md}}{(d^2 - l^2)^2} - H \tan \theta$ . The needle being not a point needle, therefore does not rotate in an absolutely uniform magnetic field.

2. The main defect is that the distance  $2l$  between the poles of the magnet can not be measured accurately.

3. The needle being pivoted and also because it carries a long pointer, some frictional resistance does act against its movement.

4. The system of measuring deflection by reading the deflection of the pointer over a circular scale is also not very accurate. The accuracy in measuring deflection can be increased by fixing a plane mirror vertically at the centre of the needle and then measuring the deflection by lamp and scale arrangement. Kew magnetometer is more accurate and therefore should be used in place of ordinary deflection magnetometer.

#### Oral Questions

1. Why the instrument is called a deflection magnetometer ? Which one is the needle-the shorter one or the longer one ? Why the needle is enclosed in a box ? Why must there be two, a needle and a pointer ? Could not the circular scale be made of a smaller diameter or the needle made sufficiently long so that the needle itself could serve for the pointer as well ?

2. What are the requirements of an ideal pointer ? Can you suggest one ?

3. Why is the needle deflected when the magnet is placed on the arm of the magnetometer ? Why the magnet should be placed parallel to the arms in this setting ? What is the harm if the magnet is placed  $\perp$  to the arms ?

4. Why is the plane mirror fixed below the needle ? What are the sources of error in this experiment and how you proceed to remove them ?

5. Way the dial of the compass box is levelled ? What is the harm if it is not levelled.

6. What will be the nature of the graph, drawn between  $\frac{(d^2 - l^2)^2}{2d}$  and  $\cot \theta$  ?

Ans. It will be a straight line because

$$F = \frac{2Md}{(d^2 - l^2)^2} - H \tan \theta.$$

$$\text{i.e. } \frac{M}{H \tan \theta} = \frac{(d^2 - l^2)^2}{2d}$$

$$\frac{M}{H} = k, \text{ a const. and } \frac{l}{\tan \theta} = \cot \theta$$

$$\therefore \frac{(d^2 - l^2)^2}{2d} = k \cdot \cot \theta.$$

$$\text{i.e. } \frac{(d^2 - l^2)^2}{2d} \propto \cot \theta.$$

So a graph between  $\frac{(d^2 - l^2)^2}{2d}$  and  $\cot \theta$  will be a straight line. Remember that  $\cot \theta = \tan (90^\circ - \theta)$ , i.e., if you want to find the value of  $\cot 38^\circ$ , then subtract  $38^\circ$  from  $90^\circ$ . It gives you  $52^\circ$ . Then  $\tan$  of  $52^\circ$  will be the same as  $\cot$  of  $38^\circ$ .

### EXPERIMENT 13.2

**Object**—Compare the magnetic moments of two magnets setting the deflection magnetometer to Tan-B position and using Equal distance method.

#### Theory

$$(i) F = Il \tan \theta \text{ (tangent law)}$$

Where  $F$  and  $Il$  are the two perpendicular fields acting simultaneously on the magnetic needle.  $\angle \theta$  is the  $\angle$  made by the magnetic needle with the field  $Il$ , when it comes into equilibrium.

$$(ii) F_1 = \frac{M_1}{(l_1^2 + l_2^2)^{1/2}} = Il \tan \theta_1$$

$$F_2 = \frac{M_2}{(l_1^2 + l_2^2)^{1/2}} = Il \tan \theta_2$$

where  $F_1$  and  $F_2$  are the fields due to the two magnets acting on the magnetic needle which now lies on the equatorial bar of the magnet.  $\theta_1$  and  $\theta_2$  are the mean deflections produced in the needle, successively due to the two magnets  
 $\therefore \frac{F_1}{F_2} = \frac{\tan \theta_1}{\tan \theta_2}$

(iv)  $\frac{M_1}{M_2} = \frac{\tan \theta_1}{\tan \theta_2}$ , if  $l_1 = l_2$  or if the half lengths  $l_1$  and  $l_2$  of the magnets are so small and the distance  $d$  is so large that  $l_1^2$  and  $l_2^2$  can be neglected compared with  $d^2$ .

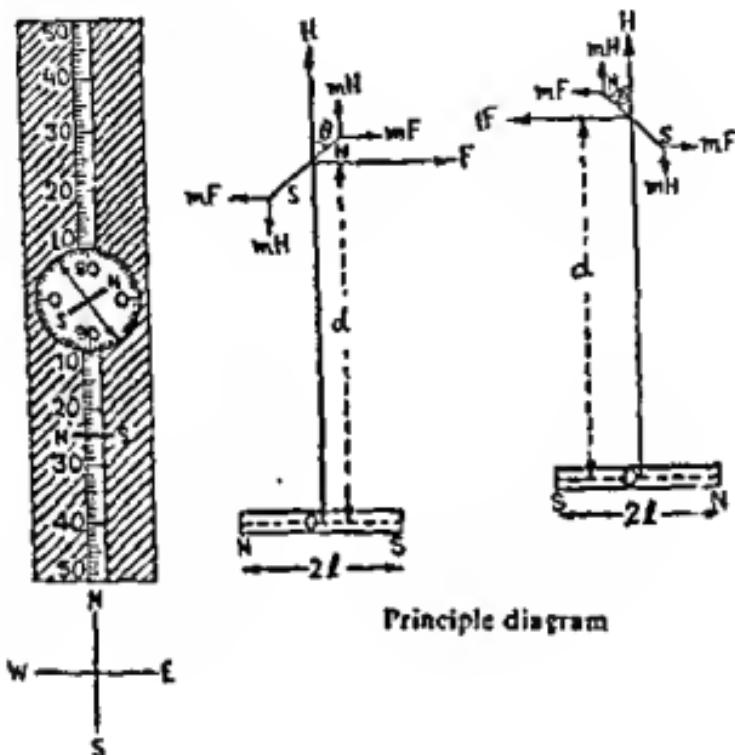


Fig. 13-2

**Note**—The magnetic needle should be shown quite small in length compared with the length of the magnet. Mark its poles and designate the angle made by the magnetic needle with the field  $H$ , as  $\theta$ . Remember that since the magnetic needle lies on the equatorial line of the magnet, so the field acting at the centre of the needle and through the centre is parallel to the magnetic axis of the magnet and in a direction from North pole side of the magnet towards the South pole side of the magnet.

### Procedure

1. Examine the apparatus and the working of its component very carefully.

2. Setting the magnetometer in Tan B position. Remove all magnets, magnetic materials and any other conductors carrying electric current away from the apparatus. First set the magnetometer in Tan-A position by the method described in the last Experiment and the pointer reads 0-0. Next hold the magnetometer from the extreme ends of its arms and rotate through  $90^{\circ}$  so that the pointer reads 90-90. It means now the arms are in the North-South direction, i.e., in magnetic meridian since the arms have been rotated through exactly  $90^{\circ}$  from their East-West position in Tan A position. Before starting work rotate the Compass box so that the pointer reads 0-0. Now the magnetometer is set in Tan B position.

3. Note the breadths of the magnets and mark their mid points. Distances are to be measured from the mid points of the magnet always. So if practically distance from the edge of the magnet is observed, then to this distance, half the breadth of the magnet should be added to know the exact distance from the centre of the magnet.

4. Place the magnet A, on the South arm of the magnetometer and with the axis of the magnet perpendicular to the arms and in such a way that the pivot of the needle lies on the equatorial line of the magnet. (In tangent A position, the axis of the magnet was along the arms and not perpendicular to the arms).

5. Suppose the north pole of the magnet is towards West. Adjust the distance of the magnet so that the deflection obtained is between  $30^{\circ}$  and  $60^{\circ}$ . Note the deflection by reading both the ends of the pointer and also record the distance of the centre of the magnet from the pivot of the needle. This gives two readings.

6. Reverse the poles of the magnet so that now the north pole of the magnet points towards East. Read both the ends of the pointer, keeping distance of the magnet the same, this makes four readings.

7. Next change the face of the magnet and repeat the four readings of steps (5) and (6), keeping distance of the magnet, the same. This makes 8 readings.

8. Transfer the same magnet on the other arm, i.e., North arm and keeping the centre of the magnet at the same distance as on South arm, repeat the above procedure and take 8 readings. This makes a total of sixteen readings for the same magnet A placed at the same distance  $d$ , on both the arms of the magnetometer. Take the mean of these sixteen deflections and say ( $\theta_1$ ).

9. Remove the magnet A away from the apparatus and place the magnet B in the same way and with its centre at the same distance. Repeat the same procedure to note the 16 deflections, the mean of which gives  $\theta_2$ . This forms one set of observation.

10. Take such three sets of observations by changing the distance of the magnets.

11. Find  $\frac{M_1}{M_2}$  separately for every set and take the mean.

### Observations

Length of magnet A =  $L$  ... cm.  $I_1 = \frac{5}{12} L$  ... cm

Length of magnet B =  $L$  ... cm.  $I_2 = \frac{5}{12} L$  ... cm

Deflection of the pointer - deflection of the magnetic needle

S. No.	Magnet	Distance of the centre of the magnet from the centre of the coil	Deflection of the pointer in degrees when the magnet is on the South Arm	North Arm		Max deflection	$\tan \theta$
				Face A up	Face B up		
1	A	1	1	2	3	4	(6)
2	B	1	1	2	3	4	
3	A	1	1	2	3	4	
4	B	1	1	2	3	4	
5	A	1	1	2	3	4	
6	B	1	1	2	3	4	
7	A	1	1	2	3	4	
8	B	1	1	2	3	4	
9	A	1	1	2	3	4	
10	B	1	1	2	3	4	
11	A	1	1	2	3	4	
12	B	1	1	2	3	4	
13	A	1	1	2	3	4	
14	B	1	1	2	3	4	
15	A	1	1	2	3	4	
16	B	1	1	2	3	4	

**Calculations**

$$\frac{M_1}{M_2} =$$

**Result**

Mean  $\frac{M_1}{M_2} = \dots \dots \text{ (Being a ratio it has no units)}$

**Precautions.** Same as in the last experiment.

**EXPERIMENT 13·3**

**Object**—Compare the magnetic moments of two magnets by setting the deflection magnetometer in  $Tan A$  position of Gauss and using Null method.

**Apparatus**—Deflection magnetometer, two magnets and a metre rod.

**Theory**

The field  $F_A$  at the needle due to magnet A is counterbalanced by the field  $F_B$  due to the second magnet B, (the deflection being zero), So we have

$$(i) \quad F_A = F_B$$

The magnetic needle lies on the magnetic axis of both the magnets, therefore

$$(ii) \quad F_A = \frac{2M_1d_1}{(d_1^2 - l_1^2)^2}$$

$$F_B = \frac{2M_2d_2}{(d_2^2 - l_2^2)^2}$$

$$\therefore \frac{2M_1d_1}{(d_1^2 - l_1^2)^2} = \frac{2M_2d_2}{(d_2^2 - l_2^2)^2}$$

$$\text{or} \quad \frac{M_1}{M_2} = \frac{(d_1^2 - l_1^2)^2}{(d_2^2 - l_2^2)^2} \times \frac{d_2}{d_1}$$

$$(iii) \quad \frac{M_1}{M_2} = \frac{d_1^3}{d_2^3} \text{ if the magnets are so small that } l_1^2 \text{ and } l_2^2 \text{ are negligible compared with } d_1^2 \text{ and } d_2^2 \text{ respectively.}$$

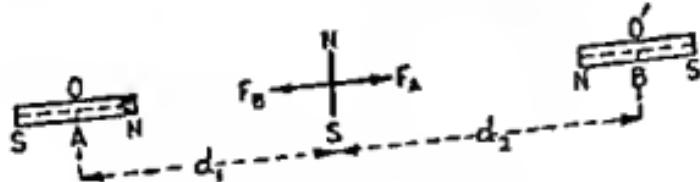


Fig. 13.3

**Procedure**

1. Mark the magnets as A and B, measure their lengths and mark their mid points.
2. Set the magnetometer in the Tan A position as discussed earlier. The arms are therefore in the East-West direction and the pointer reads 0-0.
3. Place the magnet A with its mid point at a distance  $d_1$  (kept fixed always) on the East arm of the magnetometer and with its North pole towards the needle. Deflection should not be very small. Then place the other magnet B on the West arm of the magnetometer and with its north pole towards the needle. This magnet deflects the needle in the opposite direction. Move the magnet B along the arm and find a position for which the magnetic needle stands at 0-0 again. It means deflection produced by B is exactly equal and opposite to the deflection produced by A so that the net deflection is zero. This is so because the couple on the needle due to one magnet is exactly equal and opposite to the couple due to the other. Note the distance of the centre of the magnet B.
4. Now reverse the poles of the magnet A on the same East arm so that its south pole now points towards the needle, the distance of its mid point from the needle being kept the same, equal to  $d_1$  as before.

You will have to reverse the poles of the magnet B also, on the same position to get zero deflection.

Note the distance of the centre of the magnet B, from the needle. This makes two readings.

5. Turn the magnet B upside down and reverse its face. Adjust its distance to get zero deflection again. Note the distance of the centre of the magnet. This makes three readings.

6. Reverse the poles of A. Then the poles of B will also have to be reversed and again the distance of B, adjusted to get zero deflection. Note the distance of B again. This makes four readings.

7. Now place the magnet A first with its N-pole and then S-pole towards the needle, on the West arm of the magnetometer, keeping the distance  $d_1$  of its centre from the needle, the same as on the East Arm. Note the corresponding distances of the centre of the magnet B, which is now placed on the East Arm and whose position is adjusted to get zero deflection. These two readings along with four, already taken make six readings.

Next reverse the face of magnet B and note its distances first when N-pole of both the magnets A and B are towards the needle and again when S-poles of both the magnets A and B are towards the needle. This makes 8 readings. Let mean of these eight readings be  $d_2$ . This forms one set.

8. Repeat the experiment by placing magnet A, at two more fixed distances. Thus three sets of observations are obtained.

9. Calculate  $\frac{M_1}{M_2}$  separately for every set and then calculate the mean  $\frac{M_1}{M_2}$ .

#### Observations

$$\text{Length of magnet A} = L \dots \text{cm}, \quad l_1 = \frac{5}{12} L = \dots \text{cm}$$

$$\text{Length of magnet B} = L \dots \text{cm}, \quad l_2 = \frac{5}{12} L = \dots \text{cm}$$

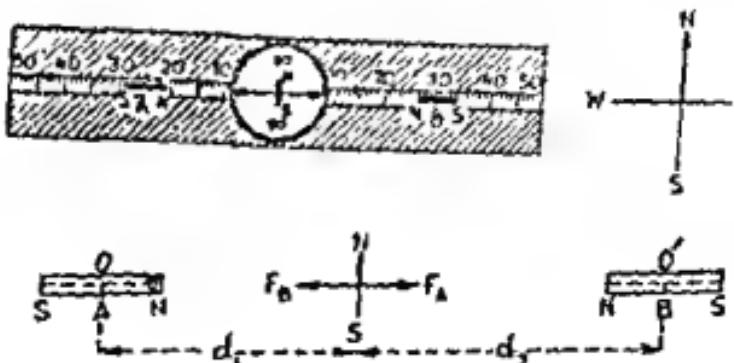


Fig. 13.3

**Procedure**

1. Mark the magnets as A and B, measure their length and mark their mid points.
2. Set the magnetometer in the Tan A position as discussed earlier. The arms are therefore in the East-West direction and the pointer reads 0-0.
3. Place the magnet A with its mid point at a distance  $d_1$  (to be kept fixed always) on the East arm of the magnetometer with its North pole towards the needle. Deflection should now be very small. Then place the other magnet B on the West arm of the magnetometer and with its north pole towards the needle. This magnet deflects the needle in the opposite direction. Move the magnet B along the arm and find a position for which the magnetic needle stands at 0-0 again. It means deflection produced by B is exactly equal and opposite to the deflection produced by A so that the net deflection is zero. This is so because the couple on the needle due to one magnet is exactly equal and opposite to the couple due to the other. Note the distance of the centre of the magnet B from the needle.
4. Now reverse the poles of the magnet A on the same East arm so that its south pole now points towards the needle. Find the distance of its mid point from the needle which is equal to  $d_2$  as before.
- You will have to reverse the poles of the magnet B on the same West arm and adjust its position to

Calculations—(i)  $\frac{M_1}{M_2}$ —

Result

Mean  $\frac{M_1}{M_2}$ —... (Being a ratio, it has no units).

**Precautions**—In addition to the general precautions to be observed with a deflection magnetometer, the following precautions are noteworthy.

- Both the ends of the pointer may not read zero before starting the experiment. Hence while setting the instrument, make only one end read zero. Do not bother about the other. Then in all subsequent readings in the experiment, the same end is to be brought to zero always by adjusting the distance of magnet B.
- Similar poles of both the magnets should point towards the needle so that their fields may be opposite otherwise zero deflection will not be obtained.
- In one particular set, distance of one magnet (A) is to be kept fixed and distance of only the other magnet (B) is to be adjusted in the eight readings to be obtained, to get zero deflection every time.

#### Oral Questions

- Which setting for the magnetometer you prefer ? Tan A or Tan B.

**Ans**—Tan A position is preferred because the field due to the same magnet placed at the same distance is twice in Tan A position than in Tan B position. Therefore the same magnet and for the same distance, the deflection produced in Tan-A setting will be more. Consequently the accuracy in measuring deflection will be more.

- Which method do you prefer for comparing the magnetic moments of two magnets, deflection method or null method and why ?

**Ans**. Null method is preferred because the deflection in this method is zero, always. So deflection is not to be measured and therefore the errors which could be committed in measuring the deflection, are eliminated.

Distance of the mid pt of the magnet B from the needle when B is on

Fixed distance of the mid pt. of magnet A (d <sub>1</sub> )	West Arm		East Arm		$\frac{N_1}{N_2} = ?$
	Face A up	Face B up	Face A up	Face B up	
1 cm	N-pole towards needle	S-pole towards needle	N-pole towards needle	S-pole towards needle	-
2 cm	N-pole towards needle	S-pole towards needle	N-pole towards needle	S-pole towards needle	-
3 cm	N-pole towards needle	S-pole towards needle	N-pole towards needle	S-pole towards needle	-

Calculations—(1)  $\frac{M_1}{M_2} -$

### Result

Mean  $\frac{M_1}{M_2} = \dots$  (Being a ratio, it has no units).

**Precantions**—In addition to the general precautions to be observed with a deflection magnetometer, the following precautions are note worthy.

- Both the ends of the pointer may not read zero before starting the experiment. Hence while setting the instrument, make only one end read zero. Do not bother about the other. Then in all subsequent readings in the experiment, the same end is to be brought to zero always by adjusting the distance of magnet B.

- Similar poles of both the magnets should point towards the needle so that their fields may be opposite otherwise zero deflection will not be obtained.

- In one particular set, distance of one magnet (A) is to be kept fixed and distance of only the other magnet (B) is to be adjusted in the eight readings to be obtained, to get zero deflection every time.

### Oral Questions

- Which setting for the magnetometer you prefer ? Tan A or Tan B.

**Ans**—Tan A position is preferred because the field due to the same magnet placed at the same distance is twice in Tan A position than in Tan B position. Therefor the same magnet and for the same distance, the deflection produced in Tan-A setting will be more. Consequently the accuracy in measuring deflection will be more.

- Which method do you prefer for comparing the magnetic moments of two magnets, deflection method or null method and why ?

**Ans**. Null method is preferred because the deflection in this method is zero, always. So deflection is not to be measured and therefore the errors which could be committed in measuring the deflection, are eliminated.

stance of centre of the magnet B, each time. This makes eight readings.

6. Then transfer the magnet A on to the North Arm and magnet B on to the South arm. Keeping the distance of the magnet A, the same, i.e.,  $d_1$  as on the South arm, repeat the above process and take the four readings of the distance of the magnet B, when B is placed on the other arm, i.e., North arm. So eight readings of the distance of magnet B have been obtained corresponding to fixed distance  $d_1$  of magnet A. Let the mean of these eight readings be  $d_2$ . This forms one set.

7. Repeat the experiment by placing magnet A, at two fixed distances. Thus three sets of observations are obtained.

8. Calculate  $\frac{M_2}{M_1}$  separately for every set and find mean.

#### Observations

Length of magnet A = L ..... cm,  $l_1 = \frac{5}{12} L -$

4

.....

**Q1:** The mid point of magnet B from the needle when B is on

**Calculations**

$$(1) \quad \frac{M_1}{M_2} =$$

**Result**

$$\text{Mean } \frac{M_1}{M_2} = \dots \text{ (Being a ratio, it has no units).}$$

**Precations :—** Same as in the previous experiment.**Modifications****EXPERIMENT 13.5**

**Object**—Plot a graph between  $\frac{(d^2 - l^2)^2}{2d}$  and  $\cot \theta$  for different values of  $d$  and mean  $\theta$  in Tan A setting of the deflection magnetometer. Interpret this graph. (R. U. 1966)

**Hint****Theory**

$$F = \frac{2Md}{(d^2 - l^2)^2} = H \tan \theta \text{ (for Tan A position)}$$

$$\text{So } \frac{M}{H} = \frac{(d^2 - l^2)^2}{2d} \tan \theta$$

$$\text{Now } \frac{M}{H} = \text{const. (K) for a magnet and for a particular place}$$

$$\therefore \frac{K}{\tan \theta} = \frac{(d^2 - l^2)^2}{2d}$$

$$\text{or } \frac{(d^2 - l^2)^2}{2d} = K \cot \theta \text{ if } \frac{1}{\tan \theta} = \cot \theta$$

$$\text{i.e. } \frac{(d^2 - l^2)^2}{2d} \propto \cot \theta$$

Hence graph between  $\frac{(d^2 - l^2)^2}{2d}$  and  $\cot \theta$  will be a straight line.

Remember that  $\cot \theta = \tan (90^\circ - \theta)$

$$\text{Examples } \cot 33^\circ = \tan (90^\circ - 33^\circ) = \tan 57^\circ$$

$$\cot 60^\circ = \tan 30^\circ$$

So it is easier to calculate  $\cot$  of an angle by consulting natural tangent tables. The value of  $\tan 30^\circ$  will be the same as that of  $\cot 60^\circ$ .

## EXPERIMENT 13.6

**Object - Verify Inverse square law of magnetism with the help of deflection magnetometer.**

**Theory**

A magnet of magnetic moment  $M$  and length  $2l$  is placed at a distance  $d$  from the magnetic needle. Let  $\theta$  and  $\phi$  be the mean deflections obtained when the magnetometer is set in Tan A and Tan B positions respectively.  $F_A$  and  $F_B$  are the fields due to the same magnet, acting on the needle when magnetometer is set in Tan A and Tan B positions respectively.

$$F_A = \frac{2Md}{(d^2-l^2)^{3/2}} = H \tan \theta \quad \dots\dots(1)$$

$$F_B = \frac{M}{(d^2+l^2)^{3/2}} = H \tan \phi \quad \dots\dots(2)$$

$$\text{Dividing } \frac{2d(d^2+l^2)^{3/2}}{(d^2-l^2)^{3/2}} = \frac{\tan \theta}{\tan \phi} \quad \dots\dots(3)$$

**Procedure**

Place a magnet at a distance  $d$  on the arm of a magnetometer set in Tan A position and find the mean  $\theta$  of the 16 deflections obtained.

Then set the magnetometer in Tan B position. Place the same magnet at the same distance  $d$  on its arm and find the mean  $\phi$  of the 16 deflections obtained. Then show that equation (3) is true. Equation (3) has been deduced from equations which were derived on the basis of inverse square law. So if practically, equation (3) is verified to be true, it means inverse square law has been indirectly verified to be true.

## VIBRATIONAL MAGNETOMETER

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### EXPERIMENT 14.1

**Object—** Compare the magnetic moments of two magnets vibration magnetometer using moment of inertia method.

**Apparatus—** Vibration magnetometer, two magnets, spirit level, compass needle, a brass bar, stop watch, vernier calliper or metre rod, physical balance and weight box.

#### Theory

When a magnet suspended freely from its centre of gravity is displaced through an  $\angle \theta$  from its natural position in the magnetic meridian, a couple  $MH \sin \theta$  acts on the magnet and the magnet begins to oscillate with a small amplitude in a horizontal plane about the vertical axis passing through its centre of gravity. Its time period is given by

$$(i) \quad T_1 = 2\pi \sqrt{\frac{I_1}{M_1 H}}$$

Where  $H$  = the horizontal component of Earth's field.

$I_1$  = the moment of inertia of the magnet about its axis of oscillation,

and  $T_1$  = the time period of first magnet.

$$(ii) \quad T_2 = 2\pi \sqrt{\frac{I_2}{M_2 H}} \text{ for the second magnet.}$$

$$(iii) \quad \frac{M_1}{M_2} = \frac{I_1}{I_2} \times \frac{T_2^2}{T_1^2}$$

$$(iv) \quad I = \text{Mass} \times \left[ \frac{(\text{Length})^2 + (\text{Breadth})^2}{12} \right]$$

i.e.,  $I = m \left[ \frac{L^2 + B^2}{12} \right]$  for a rectangular bar magnet

and  $I = m \left[ \frac{L^2}{12} + \frac{R^2}{4} \right]$  for a cylindrical magnet

when  $R$  = the radius of the cylindrical magnet  
 $m$  = its mass

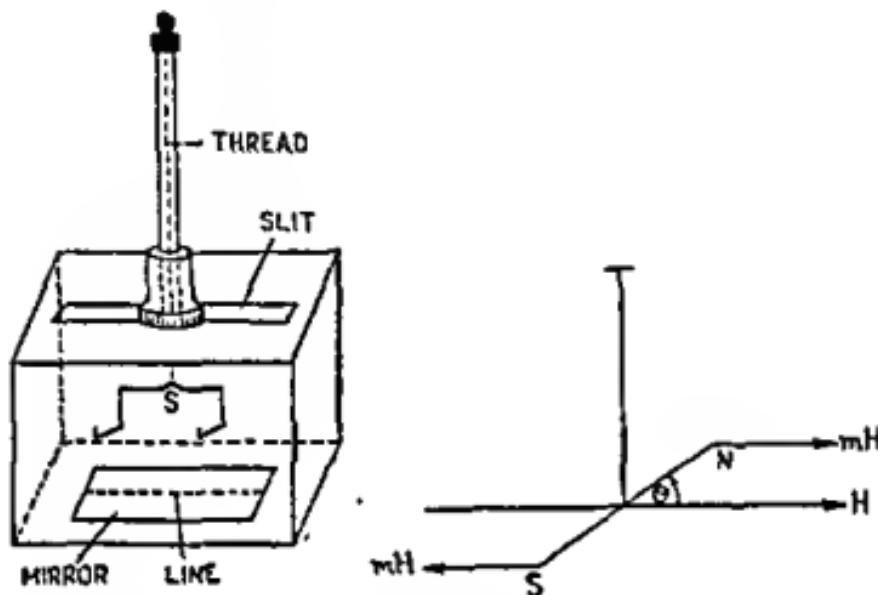


Fig. 14-1

$$\text{Couple} = MH \sin \theta$$

#### Procedure

1. Level the vibration magnetometer with the help of a spirit level by adjusting the levelling screws. When levelled, the suspension thread will not touch the sides. It will pass through the centre of the hole.

2. To set the magnetometer in the magnetic meridian. A line is already marked on the plane mirror fixed to the floor of the magnetometer. The line is parallel to the slit. Place a compass needle on this line and rotate the box till the compass needle becomes parallel to the line. Mark the boundary line around the box which now lies in the magnetic meridian.

$$3. I_1 = m_1 \left[ \frac{L_1^2 + B_1^2}{I_2} \right] \\ = \dots \text{gm cm}^3$$

$$4. I_2 = m_2 \left[ \frac{L_2^2 + B_2^2}{I_1} \right] \\ = \dots \text{gm cm}^3$$

$$5. \frac{M_1}{M_2} = \frac{I_1}{I_2} \times \frac{T_2^2}{T_1^2}$$

i.e.,  $\frac{M_1}{M_2} = \dots$  Being a ratio, it has got no units.

### Precautions

1. The suspension fibre should be carefully chosen; it should be free from twist. Unspun silken thread serves best.
2. No magnetic substance should be present in the neighbourhood of the magnetometer.
3. No metal should be present in its vicinity because this vibrating magnet would cause the flow of eddy currents in that metal, due to the variation of magnetic flux in the metal. Consequently the vibrations will get damped and the time period will be affected.
4. The formula holds good only for small amplitudes (i.e. in which  $\sin \theta = \theta$ ). So see that the amplitude does not exceed  $5^\circ$ .
5. Before starting the experiment, the magnetometer should be set in the magnetic meridian and twist in the thread, if any, should be removed according to step 3 of the procedure given above.
6. The axis of suspension should pass through the centre of gravity of the magnet.
7. When the magnet is placed in the stirrup, see that the plane containing the length and the breadth of the magnet remains horizontal. This is necessary so that the horizontal component of earth's field alone should act on the magnet.
8. The magnet should be small so that it vibrates in a uniform field. Its north pole should point towards geographical north of the earth. So before starting the experiment check the poles of the magnets and see that the magnets are not demagnetised.

9. For counting the number of vibrations, count ZERO and not ONE, when the magnet passes through the magnetic meridian and simultaneously the stop watch is started.

10. Remember length and breadth of the magnet are those dimensions of the magnet, which are perpendicular to the suspension thread and thickness is parallel to the axis of suspension. Don't confuse breadth with thickness.

11. Note the time very carefully, twice for the same number of vibrations. In the table, record the time in minutes and seconds as read on the stop watch. Then convert minutes into seconds.

#### Sources of error

1. The suspension thread is not completely free from twist. So a couple due to twist acts and causes an error.

2. When the magnet is set to be horizontal, (so that only the field II acts on the magnet), the centre of gravity of the magnet is NOT exactly below the point of suspension. The reason for this is, that the moment of the couple due to vertical component of earth's field, acting on the magnet has to be balanced by the moment due to weight of the magnet, when magnet is horizontal. Hence there occurs an error in the measurement of radius of gyration and hence in the measurement of moment of inertia.

3. Damping also affects the time period.

4. Amplitude can not be decreased very much, practically but theoretically it is required to be small.

#### Oral Questions

1. Why the apparatus is made of wood ? Are there no iron coils fixed in it ? What is the use of the mirror fixed to its floor ? Why above the apparatus, the tube, through which the thread passes, is of glass ? Why the sides of the magnetometer box have glass sheets ?

2. Will you prefer a magnetometer box of long glass tube or small tube ?

**Ans.—**The time period of oscillation is independent of the length of the suspension thread. Still we prefer a long vertical glass tube to have a greater length of suspension thread. The effect of torsion in the suspension, if any, will become negligible, if the suspension is long.

3. In which direction a freely suspended magnet would point ? On being deflected, why this freely suspended magnet vibrates ? What is the nature of these vibrations ?

4. Upon what factors does the time period depend ? How the time period of the magnet changes, when we go from the equator to the poles ?

5. Will you chose a magnet of large magnetic moment ? Of what material, the magnets are made ?

6. What is the principle of this experiment ?

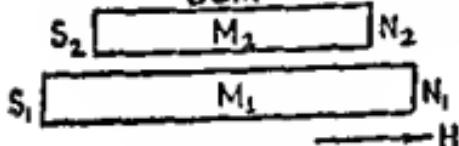
7. What is the use of the stirrup ?

8. What is moment of inertia and what are its units ?

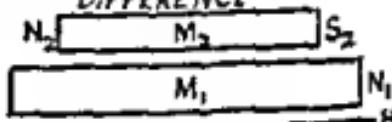
### EXPERIMENT 14.2

Object--Using vibration magnetometer, compare the magnetic moments of two magnets by sum and difference method.

SUM



DIFFERENCE



$$M = M_1 + M_2$$

$$I = I_1 + I_2$$

time period  $\sim T_1$

$$M = M_1 - M_2$$

$$I = I_1 - I_2$$

time period  $\sim T_2$

## Theory and formula

$T_1$  is the time period in the sum reading, i.e., when N-poles of both the magnets point towards geographical north of the earth.

$T_2$  is the time period in the difference reading, i.e., when N-pole of the stronger magnet is towards North of the earth and N-pole of the weaker magnet is towards South of the earth.

The moment of inertia  $I = I_1 + I_2$ , of the combination remains the same in the sum reading and also the difference reading. The total magnetic moment  $M = M_1 + M_2$ , in the sum reading and  $M = M_1 - M_2$ , in the difference reading.

$$T_1 = 2\pi \sqrt{\frac{I_1 + I_2}{(M_1 + M_2)H}} \quad \dots(1)$$

$$T_2 = 2\pi \sqrt{\frac{I_1 + I_2}{(M_1 - M_2)H}} \quad \dots(2)$$

Squaring (1) and (2) we get

$$T_1^2 = 4\pi^2 \frac{I_1 + I_2}{(M_1 + M_2)H} \quad \dots(3)$$

$$T_2^2 = 4\pi^2 \frac{I_1 + I_2}{(M_1 - M_2)H} \quad \dots(4)$$

Dividing (4) by (3)

$$\frac{M_1 + M_2}{M_1 - M_2} = \frac{T_2^2}{T_1^2}$$

Apply componendo and dividendo.

$$\frac{M_1}{M_2} = \frac{T_2^2 + T_1^2}{T_2^2 - T_1^2} \quad \dots(5)$$

## Procedure

Steps 1 to 3 are exactly the same as described in experiment No. 14.1 above.

4. First of all check the poles of the two given magnets. Be sure that neither of the two magnets is demagnetised. If one magnet is demagnetised,  $T_3$  will be the same as  $T_1$  and the denominator in (5) will become zero and  $\frac{M_1}{M_2}$  will come out to be  $\infty$ , which is NOT possible.

5. Test which of the magnets is stronger. For this, place the magnets by turn, on the arm of a deflection magnetometer, at the same distance. The one which produces a greater deflection is the needle of the deflection magnetometer, is stronger.

6. Place in the stirrup the two magnets symmetrically one above the other, with similar poles pointing towards north of the earth. A piece of paper or cardboard is inserted between two magnets so that they do not induce polarity on each other. If two pairs of hooks are provided in the stirrup, then one magnet should be placed in the upper hook and the other magnet in the lower hook. Since now they are a good distance apart, they won't induce polarity and hence there is no need of placing any cardboard between them.

The combination is ready for sum-observation. Its time period  $T_1$  is observed.

7. For the difference reading, shift the north pole of the weaker magnet from north towards south of the earth. Keep the North pole of the stronger magnet toward North of the earth, otherwise the combination of the magnets will rotate through  $180^\circ$ . Note the time period of this combination. It is  $T_2$ .

8. Calculate  $\frac{M_1}{M_2}$  using formula (5) above.

### Observations

No. S.	Number of vibrations	Sum Reading			Difference reading		
		Time in Minutes and seconds	Time in secs.	Time Period $T_1$ (sec.)	Time in Min. and sec.	Time in secs.	Time Period $T_2$ (sec.)
1	20						
2	20						
3	25						
4	25						
5	30						
6	30						

$$\text{Mean } T_1 = 14.7 \text{ seconds (say)}$$

$$\text{Mean } T_2 = 35.3 \text{ seconds (say)}$$

### Calculations

$$\frac{M_1}{M_2} = \frac{T_2^2 + T_1^2}{T_2^2 - T_1^2}$$

$$= \frac{(35.3)^2 + (14.7)^2}{(35.3)^2 - (14.7)^2}$$

$$\log 35.3 = 1.5478$$

$$\text{antilog } \frac{3.0956}{2}$$

$$-1247$$

$$- \frac{1247.0 + 216.1}{1247.0 - 216.1}$$

$$\log 14.7 = 1.1673$$

$$\text{antilog } \frac{2.3346}{2}$$

$$-216.1$$

$$- \frac{1463.1}{1030.9}$$

$$\log 1463 = 3.1653$$

$$\log 1030 = 3.0133$$

$$\text{antilog } \frac{0.1520}{2}$$

$$-1.419$$

$$\text{Result } \frac{M_1}{M_2} = 1.419$$

Being a ratio,  $\frac{M_1}{M_2}$  has no units.

### Additional Precautions

1. Don't allow the magnets to touch each other. They will induce polarity on each other and thus cause error. So either place cardboard between them or use such an apparatus in which they can be placed one above the other, 1 or 2 cm. apart.
2. If in the difference reading, the combination rotates through  $180^\circ$ , it means the North pole of the stronger magnet has been placed towards South of the earth. So change the poles of the magnets end to end.
3. The magnetic moments should not be nearly equal, because  $M_1 - M_2$  will become very small in difference reading and hence period  $T_2$  will become very large. If  $M_1 = M_2$ ,  $M_1 - M_2 = 0$ , then  $T_2 = \infty$ . So it will be impossible to record any time period.
4. While changing from sum to difference reading, only the weaker magnet has to be reversed.

### Sources of errors

1. Magnetic induction acting mutually on the two magnets will change the values of  $M_1$  and  $M_2$ .
2. The geometrical axis and the magnetic axis of the magnets may not coincide.

### Oral Questions

1. Why is this method called the sum and difference method? What is its importance and is this method better than inertia method? If so, why?
2. Why should the magnetic axis of the two magnets be parallel?
3. What is the necessity of the stirrup? Can't its use be avoided?
4. Should the stirrup be heavy or light?

Ans. It should be light, (1) If it is a heavy metallic stirrup the magnetic field of the earth will cause the flow of induced currents in the stirrup. This will damp the vibrations of the magnets and increase on using a heavy

## MEASUREMENT OF RESISTANCE

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An unknown resistance can be determined by making use of Ohm's Law  $R = \frac{V}{C}$ . Thus the unknown resistance will be equal to the ratio of deflections obtained in the voltmeter and the ammeter. These deflections can not be determined accurately. Hence the value of R will not be accurate. If a method is evolved in which deflection remains zero and some other quantities are measured with a greater accuracy, such a method will be a NULL METHOD and hence preferable to the deflection method. Such a null method is based upon Wheatstone's bridge principle.

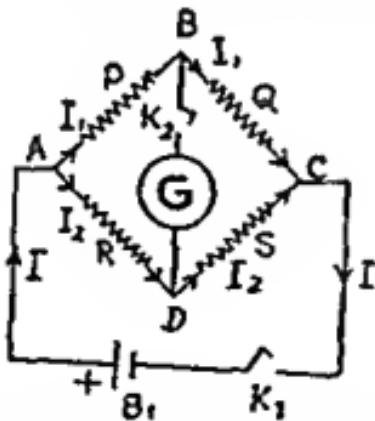


Fig. 15.1

A Wheatstone's bridge consists of four resistances P, Q, R and S connected as shown in the fig. 15.1. Between the points A and C, a cell along with a key  $K_1$  is connected and between the points B

and D, a galvanometer along with a key  $K_1$  is connected. On closing key  $K_1$ , current begins to flow through all the four resistances P, Q, R and S. Then on pressing key  $K_2$ , if galvanometer gives zero deflection, i.e., if no current flows in the branch BD, it means the resistances P, Q, R and S are such that potential at B = potential at D. This is possible when  $\frac{P}{Q} = \frac{R}{S}$ . Then bridge is said to be balanced.

### Conclusion

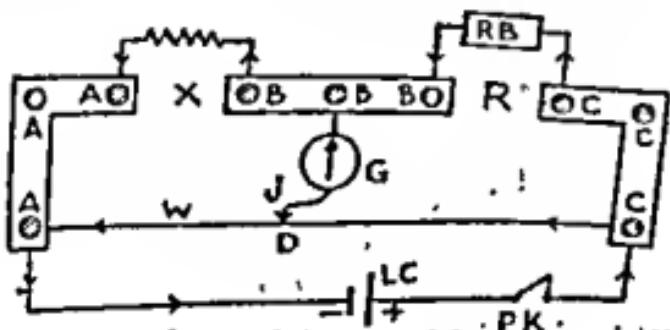
If the resistances P, Q, R and S are adjusted in such a way that on pressing first key  $K_1$  and then key  $K_2$ , galvanometer gives zero deflection, it means the bridge is balanced and the condition  $\frac{P}{Q} = \frac{R}{S}$  is being satisfied. Metre bridge and P. O. box are the practical examples of Wheatstone's bridge.

### EXPERIMENT 15.1

**Object**—Using metre bridge, determine the resistance of the given wire and thus calculate the specific resistance of the material of the wire.

#### Apparatus

Metre bridge, decimal Ohm Resistance box, Leclanche cell, galvanometer, Screw gauge, Metre scale, plug key, connecting wires etc.



X—Unknown resistance, R. B—a decimal Ohm resistance box,  
 LC—Leclanche cell, J—Jockey PK—plug key, G—Galvanometer,  
 W—Metre bridge wire 100 cm long—AC

$l$ —Balancing length corresponding to unknown resistance X.

$\rho$ =resistance per cm length of the wire.

### Theory and Formula

If galvanometer gives zero deflection when the jockey J is touched at the point D, it means the metre bridge is balanced and hence from equivalent Wheatstone's bridge diagram, we have

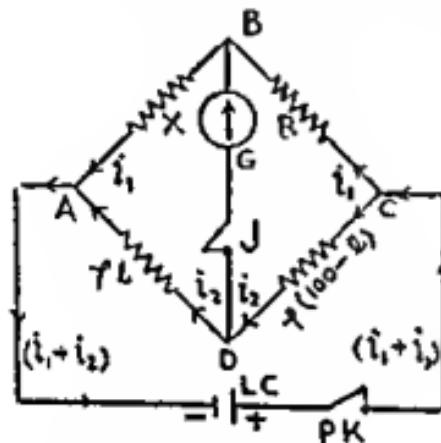


Fig. 15.3

$$\frac{X}{R} = \frac{2\rho}{(100-l)\rho}$$

$$\text{i.e., } \frac{X}{R} = \frac{1}{(100-l)}$$

$$\text{(i) or } X = R \cdot \frac{1}{100-l}$$

Where l is the distance of the null point from the left end A of the wire, when unknown resistance X is in the left gap.

$$\text{(ii) } \rho = \frac{X \cdot \pi r^2}{L}$$

Where  $\rho$ —Specific resistance of the material of the given wire.

$r$ —radius of the given wire

L—the effective length of the wire, i.e., total length of the wire minus the length under the screws.

### Procedure

1. Make the connections as shown in the figure 15.2. If there are four gaps in the apparatus, two of these may be closed by inserting two thick metal plates.

2. Start the current in the circuit by closing the plug key. Take out one or two ohm plug from the resistance box. Place the jockey J at one end A of the wire and note the galvanometer deflection. Then place the jockey J at the other end C of the wire and again note the deflection. If these deflections are in opposite directions, it means the connections are correct. For further confirmation, place the jockey J at the middle of the wire and note the deflections by making  $R=0$  and  $R=\infty$ . The two deflections in opposite directions would mean the connections are correct.

3. Using resistances even up to first place of decimal, adjust the resistance R in the R. B. in such a way that the null point is obtained nearly at the middle of the wire. If null point is obtained exactly at the middle of the wire, i.e., if the jockey J divides the wire AC into two exactly equal halves, it would mean that the unknown resistance X is equal to the resistance R in the R. B. So without making calculations, it would give you an idea about the exact magnitude of X, which would be equal to R.

4. With unknown resistance X in the left gap, find the distance l' of the null point from the left end A of the wire. Interchange the resistances R and X, so that unknown resistance X is now in the right gap. Measure the distance l'' of the null point, from the right end C of the wire. Take the mean of l' and l''. It is l. Use the formula  $X = R \frac{l}{100-l}$  to calculate the unknown resistance X. This is one set.

Note—1. Note that l' and l'' correspond to X, i.e., these are the lengths measured on the side of X, always.

2. l' and l'' should not differ by more than 1 cm. Your observations will be considered better if l' and l'' are quite close to each other. So while interchanging the resistances, see that the portion of the wire under the screws

remains the same in the left gap as well as in the right gap. Also the pressure of connections should not change.

5. To take more sets, change R in R. B. in steps of 1 ohm or 2 ohm, i.e., take resistance in R Box—R-2, R-1, R, R + 1 and R + 2. So for these resistances used I should very preferably from 45 cm to 55 cm. In no case I should be less than 40 cm and more than 60 cm. So calculate X separately for these observations and then find the mean.

6. Disconnect the resistance wire and measure its length with the metre scale. As the portion of the wire under the screws does not contribute to resistance in the gap, hence exclude that portion while measuring length L of the wire.

7. With the help of a screw gauge, measure the diameter of the wire at six different points along the length of the wire and at every point in perpendicular directions. Find mean diameter D and then calculate its radius  $r = \frac{D}{2}$ .

8. Using the formula  $\rho = X \frac{\pi r^2}{L}$ , calculate the specific resistance  $\rho$  of the material of the given wire.  
Observations

S. No.	Resistance in R Box R (in ohms)	Distance of the null point		$\frac{I - I' + I''}{2}$ (in cm)	$\frac{R}{(100 - I)}$ (ohms)	$X = R \frac{I}{(100 - I)}$ (ohms)
1.		from end A when X is in left gap	from end C when X is in right gap			
2.						
3.						
4.						

Mean value of X = ..... ohms.

Length L of the resistance wire = ..... cms

Least count of the screw gauge = ..... mm = ..... cm

Zero error in screw gauge = ..... mm = ..... cm

S.	Main scale reading (in cms)	Circular scale reading		Total read (in cm)
		in divisions	in cm	
1	(a) in one direction			
2	(b) in $\perp$ direction			
3				
4				
5				
6				

Mean diameter = ..... cm

Corrected diameter =  $D - \frac{z}{2} = D - \frac{0.01}{2} = D - 0.005$

Radius  $r = \frac{D}{2} - 0.0025$

### Calculation

$$\rho = \sqrt{\frac{\pi r^2}{L}}$$

### Result

$$\rho = \dots \text{ ohm cms}$$

2. Do not press the jockey on the wire, because it will make the cross-section of the wire non uniform. Although meter bridge is called slide wire bridge also yet do not slide the jockey by pressing it on the wire.

3. First press the plug key and then press the jockey j. If you press these keys in the reverse order, you are likely to miss the actual null point because galvanometer may give deflection due to the flow of induced current in it, even when the bridge is balanced.

4. To begin with, galvanometer may be shunted to avoid damage to its coil. Then near the null point the shunt may be removed.

5. The plugs in the resistance box should be tight. They should not be hammered down, but they should be rotated to make them tight. Whenever a particular plug is taken out, the plugs on either side of it get loose. So they should be tightened. Use decimal ohm box.

6. Allow the current to flow only for small time, because otherwise wire will get hot and its resistance may change. For the same reason, do not use a lead accumulator, as it will send a large current and thus heat the wire. So use Laclanche cell.

7. When the unknown resistance and the resistance box are interchanged, the distance of the null point should be measured from the other end of the wire.

8. Observations should be repeated after reversing the direction of current in the wire A C. So errors due to Peltier's effect will get eliminated.

9. X and R must be interchanged and while doing so the pressure of connections should not change. Do not include the wire that has come under the screws while measuring length L of the wire.

#### Sources of error

1. Due to non uniformity of the one metre long wire stretched on the metre bridge.

2. Due to end resistances.

3. Due to large least count equal to one mm for measuring length.

4. Due to Peltier's effect.

### Oral Questions

1. Why connecting wires are of copper and why are they wrapped with thread ?

2. Define resistance, specific resistance, current, potential difference and also name their units.

3. Why resistance wires are doubled on themselves before they are made into coils ?

4. Why resistance box is closed from all sides ? How the resistance coils are joined in it and what is there below the plug of infinite resistance.

5. Why galvanometer gives deflection on passing current and why its needle stops at a particular division when a particular current passed ?

6. What are other methods for determining the resistance and out of them which one is the best ?

7. Why metre bridge is called a metre bridge ? Can't the wire stretched on it be of copper. If not, why so ?

8. What are end resistances and how do they come into picture ?

9. Why the metallic plates joined in two gaps, so polished ?

10. What are conjugate arms ? When will the bridge be most sensitive ?

11. Can the metre bridge wire be taken very long or very short ?

### EXPERIMENT 152

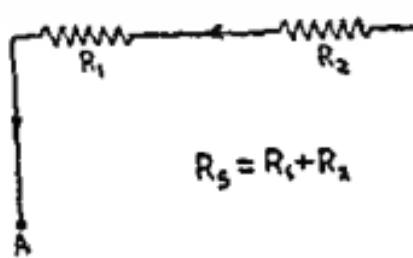
**Object—Verify the laws of resistances in series and in parallel using metre bridge.**

## Formula

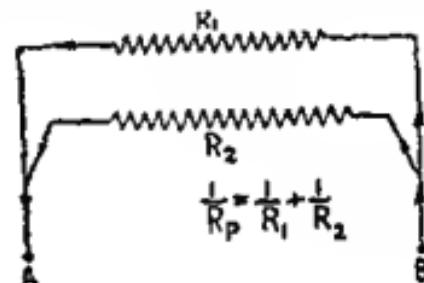
$$R_S = R_1 + R_2 \quad \dots\dots(1)$$

$$\frac{1}{R_P} = \frac{1}{R_1} + \frac{1}{R_2} \quad \dots\dots(2)$$

When the resistances are joined in series, their equivalent resistance is equal to the sum of the individual resistances. When the resistances are joined in parallel, the reciprocal of their equivalent resistance is equal to the sum of the reciprocals of the individual resistances.



Series combination



Parallel combination

Fig. 15.3

## Procedure

- Find the resistances  $R_1$  and  $R_2$  of the two resistance wires separately, according to the procedure given in experiment 15.1
- Join  $R_1$  and  $R_2$  in series and connect this series combination in the left gap AB of the metre-bridge and find their equivalent resistance  $R_S$ . Disconnect them and again connect them, this time in parallel combination, in the gap AB of the metre bridge and determine their equivalent resistance  $R_P$ .
- Then make a table as given on next page and show that is  $R_S$  very nearly equal to  $R_1 + R_2$  and  $\frac{1}{R_P}$  is equal to  $\frac{1}{R_1} + \frac{1}{R_2}$ .

perimentally  
recorded values

$$\frac{1}{R_p} = \frac{1}{R_1} + \frac{1}{R_2}$$

$$\frac{1}{R_p} = \frac{1}{R_1 + R_2}$$

$$\frac{R_p}{R_1 + R_2} = \frac{1}{1} = \frac{R_p}{R_S}$$

$$R_S = (R_1 + R_2)$$

volt

$R_S = (R_1 + R_2)$  - a very small quantity (negligible)

So  $R_S = R_1 + R_2$  so law of resistances in series is verified. Again  $\frac{1}{R_p} = \frac{1}{R_1} + \frac{1}{R_2}$  - a very small quantity negligible

So  $\frac{1}{R_p} = \frac{1}{R_1} + \frac{1}{R_2}$ . So law of resistances in parallel is verified.

#### cautions

Don't take wires of very small resistances because in parallel combination, the resistance will further decrease and hence the current will increase.

#### Oral Questions

- What is the characteristic of series combination ?  
Ans. The same current passes through both the wires.
- What is the characteristic of parallel combination ?  
Ans. The same potential difference exists between the ends of both the wires.
- Where is series combination used ?  
Ans. (i) When it is desired to decrease the current in the

4. Where is parallel combination used ?

Ans. (i) When we want to increase the current in the circuit.

(ii) When the addition of one resistance is not desired to change the current in the other resistance.

Example—Electric bulbs are connected in parallel.

Note—The Equivalent resistance of a number of resistances connected in parallel is always less than the least of all of them.

### Modifications

#### EXPERIMENT 15.3

Object—Study the variation of resistance of a wire of a given material with length.

Hint :  $R \propto l$

Take three lengths  $l_1$ ,  $l_2$  and  $l_3$  of the same wire, i. e., wire of the same material and the same diameter and find their resistances  $R_1$ ,  $R_2$  and  $R_3$ .

Then show that  $\frac{R_1}{l_1} = \frac{R_2}{l_2} = \frac{R_3}{l_3}$  , const.

$$\text{i. e., } \frac{R}{l} = \text{const.}$$

$$\text{or } R \propto l$$

Hence a graph between resistance and length will be a straight line.

#### EXPERIMENT 15.4

Object—Study the variation of resistance with diameter, by taking wires of the same material, and same length but of different diameters.

Hint :  $R \propto \frac{1}{A}$  where  $A$  = area of cross-section of wire.

$$\text{So } R \propto \frac{1}{D^2}, \quad \therefore R = \frac{\pi D^2}{4}$$

Hence show that  $R_1 D_1^2 = R_2 D_2^2 = R_3 D_3^2 = \text{const.}$   
i.e.,  $R D^2 = \text{const.}$

Also draw a graph between  $R$  and  $\frac{1}{D^2}$ . It will be a straight

line.

### EXPERIMENT 15·5

Object—Determine the resistance of one cm length of the given wire by metre bridge.

$$\rho = \frac{R}{l} \text{ ohm per cm.}$$

Divide the resistance of a wire as determined by the help of metre bridge, by its length. It will be  $\rho$ , the resistance per cm length of the wire. You may take two or three different lengths and then calculate the mean value of  $\rho$ .

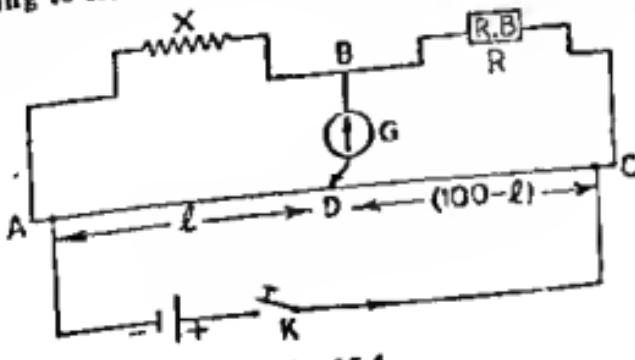
### EXPERIMENT 15·6

Object—Determine the length of the given wire required to construct a five ohm coil.

Let  $R$  be the resistance of length 1 cm of the wire determined as above in experiment 15·1. Then required length  $L = \frac{1}{R} \times 5 \text{ cms.}$

### EXPERIMENT 15·7

Object—Connect the unknown resistance  $X$  in one gap and a resistance box in the other gap. Then study a relation between resistance  $R$  to the resistance box and the reciprocal of the length corresponding to  $X$ .



$$R = \frac{(100 - I)}{I} \cdot X$$

$$R = \frac{100X}{I} - X$$

...(1)

X the unknown resistance is constant.

$$\text{Hence } R \propto \frac{1}{I}$$

...(2)

Hence a graph between resistance R in the R box and reciprocal of the length I (corresponding to unknown resistance X), will be a straight line.

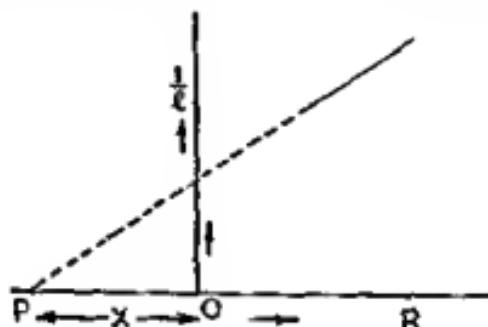


Fig. 15.5

Further on putting  $\frac{1}{I} = 0$  in equation (1) we get,

$$R = 0 - X$$

$$\text{i. e., } X = -R$$

Hence if the straight line graph is produced, it will meet the axis of R, on its negative side at a point P whose distance from O, the origin would measure the unknown resistance X. So the unknown resistance X can be determined from this graph but since you have to find its absolute value, see that you take zero of  $\frac{1}{I}$  and zero of R as the origin itself.

# 16

## POST OFFICE BOX

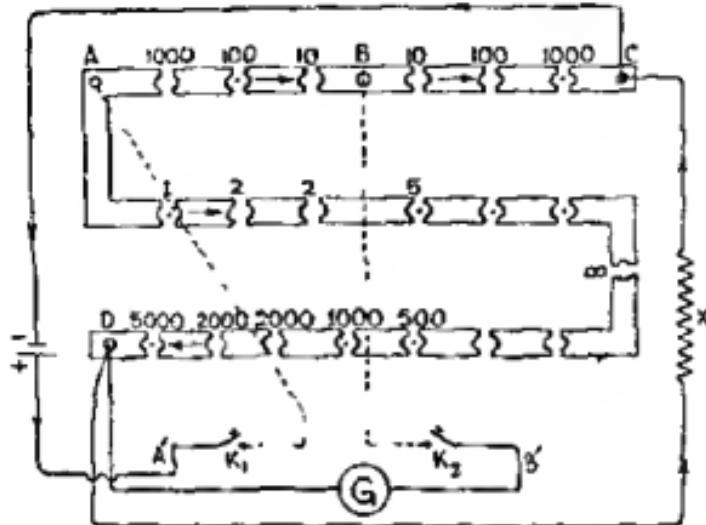
Post office box, like metre bridge is based on Wheatstone's bridge principle. Three arms P, Q and R of Wheatstone's bridge principle are permanently provided in the Post Office box itself. The fourth arm S is provided from outside by the unknown resistance. Arms P and Q in the Post Office box are called ratio arms and each arm contains resistance coils of 10, 100 and 1000 ohms joined in series. The third arm R is called the variable resistance arm or the rheostat arm. It contains resistance coils of one ohm, 2 ohms.....and 5000 ohms, all joined in series. The total resistance of all the coils in this arm R is 11110 ohms and the resistance in this arm can be varied in steps of one ohm, from one ohm to 11110 ohms. The points A and B have been brought out of A' and B' through tapping keys by making connection internally as shown by dots.

For the measurement of resistance, metre bridge can cause an error up to 5% and the P. O. box can measure resistances up to second place of decimal and with error less than 1%. For very small resistances, it is not a good instrument but for ordinary resistances, it gives quick and accurate results. The resistance coils used in it are made of manganin which has a high specific resistance and low temperature coefficient of resistance. To avoid the effect of water vapours present in air, the coils are sealed in a closed box.

### EXPERIMENT 16 I

Object—Using Post Office box, determine the resistance of the given wire and then calculate the specific resistance of the

Apparatus—Post office box, Leclanche cell, Galvanometer, Screw gauge, Metrescale, Connecting wires, Sand paper etc.



Post Office Box diagram

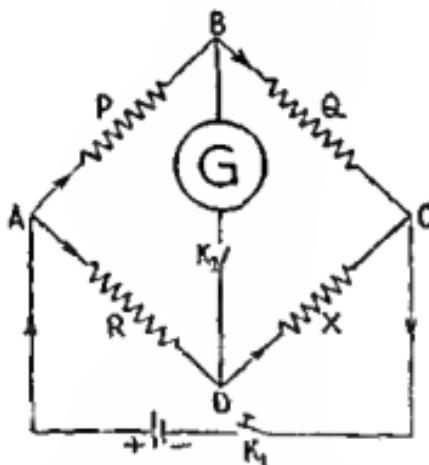


Fig. 16-1  
Equivalent Wheatstone's bridge diagram

#### Theory and formula

If on pressing key  $K_1$  and then key  $K_2$ , galvanometer gives zero deflection, it means the bridge is balanced and hence the condition

$$\frac{P}{Q} = \frac{R}{X} , \text{ } k \text{ being satisfied and from}$$

$$\text{which } X = R \frac{Q}{P}$$

Knowing P, Q and R, value of X, the unknown resistance can be calculated. The ratio  $\frac{Q}{P}$  can be kept as 1.01 or 1.

$$\rho = \frac{X \pi r^2}{L} \text{ ohm cm}$$

where  $\rho$  = specific resistance of the material of wire.

$r$  = radius of the wire measured in cms,

L = Total length of the wire between the screws measured in cms.

### Procedure

1. Note carefully which points are internally connected in the Post office box and locate the points A, B, C and D. Make the connections as shown in the figure, i. e., insert the galvanometer between B and D via the tapping key B'. Connect the cell between A and C via the tapping key A'. Connect the unknown resistance between C and D, i. e., between the free ends of arms Q and R.

2. First of all take out 10 ohms plug from each of the arms P and Q.

*Note :—If you do not do so, you won't get any deflection at all in the galvanometer. See that all the remaining plugs in the arms P, Q and R are tight.*

To test whether the connections are correct or not, keep R=0 and first press the cell key K<sub>1</sub> and then the galvanometer key K<sub>2</sub>. Note the deflection. Next make R=∞, and repeat the above process. If now the deflection is in a direction opposite to that obtained by keeping R=0, it means, the connections are correct. If the deflection is in the same direction again, check up the connections and see that the one sided deflection is not due to loose plugs.

note the deflection. Go on increasing R in steps of one ohm, and note the direction of deflection every time. Thus find consecutive resistances (say 3 and 4 ohm) in arm R, for which deflections are obtained in opposite directions. Note these observations in the proper columns in the observation table. Since P and Q are equal. So the unknown resistance X is also equal to the resistance in third arm R, i.e., X lies somewhere between 3 and 4 ohms. (Don't say X is equal to the mean of 3 and 4 ohm).

4. Next make P = 100  $\Omega$ s, keeping Q = 10  $\Omega$ . Don't forget to introduce the 10  $\Omega$ s plug in P, because otherwise it will make  $P = 110 \Omega$ s. Now since P is ten times Q, from the formula  $X = R \frac{Q}{P}$ , it is clear that R will also have to be increased ten times, in order to get the null point. Hence search for consecutive resistances between 30  $\Omega$ s and 40  $\Omega$ s in R, for which galvanometer gives deflections in opposite directions. Let these be 37  $\Omega$ s and 38  $\Omega$ s. Unknown resistance X is now  $\frac{1}{10}$  of the resistance in R, i.e., X lies somewhere between 3.7  $\Omega$ s and 3.8  $\Omega$ s (Don't say that X is equal to the mean of 3.7 and 3.8  $\Omega$ s). Record these observations in the table.

5. First insert 100  $\Omega$ s plug in P and then take out 1000  $\Omega$ s plug out of it, keeping Q = 10  $\Omega$ s as before so that the ratio Q:P becomes 10:1000. Now null point will be expected for obvious reasons, for some resistance lying between ten times the values of R obtained in step 4, i.e., between 370 and 380  $\Omega$ s.

6. At this stage the bridge usually becomes insensitive. Due to high resistance in the circuit, the current becomes very weak and so it does not produce any detectable deflection in the galvanometer. Therefore not down the range of all such resistances in R for which deflections remains zero. You MUST find two resistances, one on either side of this range, for which the galvanometer JUST gives deflections in opposite directions. Then the correct value of R is the mean of these values of R, which cause opposite deflections. This mean value of R divided by 100 gives the value of the unknown resistance X.

7. Measure the effective length L of the wire, (i.e., by excluding the portion of the wire under the screw). Measure the d.s.

## PRACTICAL PHYSICS

meter of the wire at six different points all along the length of the wire and at every point in perpendicular directions. Find the mean diameter and hence the radius of the wire.

8. Calculate the specific resistance  $\rho$ , by using the formula  
 $X = \frac{\pi r^2}{L}$ .

**Observations**

	Ratio arms		Resistance in Rheostat arm R (ohm)	Deflection is towards	Inference
	P (ohms)	Q (ohms)			
1.	10	10	3	Right	Connections are correct.
			∞	Left	
2.	10	10	3	Right	$X = R \cdot \frac{Q}{P} = R \cdot \frac{10}{10} = R$
			4	Left	So X lies somewhere between 3 and 4.
3.	100	10	37	Right	$X = R \cdot \frac{10}{100} = \frac{R}{10}$ . Then
			38	Left	so X lies somewhere between 3 and 3.8.
4.	1000	10	374	Right	$R = \frac{374 + 378}{2} = 376$
			375 to 377	No deflection	$X = R \cdot \frac{Q}{P} = R \cdot \frac{10}{100}$
			378	Left	$= \frac{R}{10}$
					$\therefore X = 3.76 \text{ ohms.}$

So unknown resistance  $X = 3.76 \text{ ohms}$

(The values obtained in your experiment will naturally be different from those recorded in the above table).  
 Length of the resistance wire  $L = \dots \text{cm.}$

No.		Main Scale reading (cms)	Circular scale reading		Total reading in cms
			in Divi- sion	in cms	
1	(a) in one direction (b) in $\perp$ direction				
2					
3					
4					
5					
6					

$$\text{Mean diameter} = \frac{\Sigma D}{6} = \dots \text{cm}$$

$$\text{Corrected diameter} = D = \dots \text{cm}$$

$$\text{radius } r = \frac{D}{2} = \dots \text{cm}$$

### Calculations

$$r = \frac{\Sigma x_{\text{corr}}}{L}$$

### Result

$$r = \dots \text{cm}$$

$$\text{Standard result } r = \dots \text{cm}$$

$$\% \text{ age error} = \dots$$

### Precautions

1. All connections should be tight, neat and clean. Rub the connecting wires and the terminals with sand paper to make them clean.

2. When a plug is taken out, the plug on either side of it get loose. Make them tight by slightly twisting. Repeat it every time when a plug is taken out. Do not hammer the plug from above.

3. Never use an ammeter in this experiment. It will set a large current and then test the resistance and change their value. Use a Leclanche cell.

4. Always press the cell key first so that current grows to its invariant value. Then press the galvanometer key. If galvanometer key is pressed first, then on pressing cell key, current grows in the circuit and consequently an induced current begins to flow in the circuit. This induced current may flow through the galvanometer and cause deflection in it even when the bridge is balanced. Then you are likely to miss the actual null point.

5. Before testing the correctness of the connections, don't forget to take out 10 ohms plugs from each of the arms P and Q, because otherwise you won't get deflection at all in the galvanometer.

6. Remember that Q is kept fixed at  $10\ \Omega$  and only the value of P is changed from 10 to 100 and then to 1000 ohms. While changing the value of P, see that only one plug is out, at a time.

7. When P : Q is 10 : 10, start with R = 0, 1, 2, 3...etc. Sometimes when the unknown resistance X is less than one, i. e., it lies between 0 and 1, you will get one sided deflection if you try R = 1, 2, 3...upwards and if you do not record the deflection for R = 0. In this case on making P : Q as 100 : 10, the null point will be expected for some resistance R lying between 0 and 10 ( $0 \times 10 = 0$ , and  $1 \times 10 = 10$ ).

8. The values of R recorded for opposite deflections MUST be opposite when P : Q is 10 : 10 or 100 : 10.

9. Remember that the unknown resistance X is obtained only from the third set. The first two sets, i. e., when P : Q is 10 : 10 or 100 : 10 only gives us an approximate value.

3. In what respect the metre bridge method and post office box method, for the measurement of resistances are ( i ) similar ( ii ) different ?

Ans : ( ii ) In Post office box, ratio arms are kept fixed and resistance in third arm R is adjusted to get the null point. In Metre bridge, the ratio arms are themselves adjusted to get the null point.

4. When is the bridge most sensitive ? What are conjugate arms ? Explain.

5. Why in the last set, the bridge becomes so insensitive ?

6. Can't you keep P fixed at 10 ohms and change Q to 100 or 1000  $\Omega$ .

7. Is this the best method for determining the resistance ? To which place of decimal, the post office box can determine the unknown resistance ?

#### Modifications

1. Using Post Office Box, verify the laws of resistances in series and in parallel.

2. Study the variation of resistance of a wire of a given material and given diameter, with length.

3. Study the variation of resistance with diameter, by taking wires of the same material and the same length.

4. Determine the resistance per cm length of the given wire.

5. Determine the length of the given wire required to construct a one ohm cell. For the hints and solutions, consult the modifications on Metre bridge experiment, already discussed.

---

Potentiometer means the arrangement which measures potential difference.

Potentiometer is an ideal voltmeter. To cause deflection a voltmeter, current must pass through it. So when a voltmeter connected across two points to measure the potential difference between them, it draws same current. Hence the main current between the two points decreases and consequently the potential difference between the two points to be measured, also decreases. Hence theoretically speaking, a voltmeter never reads the actual potential difference or the actual e. m. f. of a cell. Potentiometer is an arrangement in which no deflection is to be read. It is a NULL method and hence preferable. It measures the actual potential difference between two points and the actual e. m. f. of a cell.

#### EXPERIMENT 17·1

**Object**—Compare the e.m.f.s. of two cells using potentiometer. Also find the minimum and the maximum potential gradients you have used in your experiment.

**Apparatus**—Potentiometer, Lead accumulator, Rheostate,

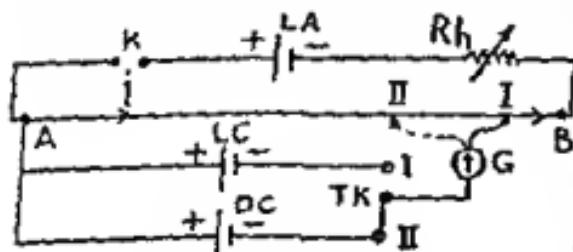


Fig. 17·1

plug key, two way key, galvanometer, the two cells say Leclanche cell and Daniel cell whose e. m. fs. are to be compared, connecting wires and jockey.

PK=Plug key, LA=Lead Accumulator, Rh=Rheostat, LC=Leclanche cell; DC=Daniel cell. G=galvanometer. J=Jockey. TK=Two way key; AB=Potentiometer wire 1000 cm

long. It actually consists of ten wires joined in series and of 100 cm length each. D and D' are the null points obtained, after taking Leclanche cell and Daniel cell into the circuit respectively.

**Theory and Formula—**Lead accumulator sends a constant current C (say) through the potentiometer wire A B, whose resistance per cm length of the wire is  $\rho$ .  $l_1$  and  $l_2$  are the balancing lengths obtained with Leclanche cell and Daniel cell taken into the circuit respectively. Then if  $E_1$  and  $E_2$  are the e.m.f.'s of Leclanche cell and Daniel cell, we have

$$E_1 = \text{Potential difference between A and D} = C l_1 \rho$$

$$E_2 = \text{Potential difference between A and D'} = C l_2 \rho$$

$$\text{so } \frac{E_1}{E_2} = \frac{C l_1 \rho}{C l_2 \rho} \text{ i.e. } \frac{E_1}{E_2} = \frac{l_1}{l_2} \quad \dots (1)$$

i. e., e. m. fs. of the two cells are directly proportional to their balancing lengths provided constant current is passed through the potentiometer wire.

Potential gradient  $\sigma$  is the potential difference per unit length of the potentiometer wire

$$\text{i. e. } \sigma = \frac{E_1}{l_1} = \frac{E_2}{l_2} = C \rho \quad \dots (2)$$

Since e.m.f. of Daniel cell is taken as a standard e.m.f. = 1.08 volts, so

$$\text{Minimum potential gradient} = \sigma_{\min} = \frac{\text{E. m. f. of Daniel cell}}{\text{Max. value of } l_2 \text{ out of all sets of observations}}$$

$$\text{Maximum potential gradient} = \sigma_{\max} = \frac{\text{E. m. f. of Daniel cell}}{\text{Min. value of } l_2 \text{ out of all sets of observations}}$$

- Units of potential gradient are volts per cm.

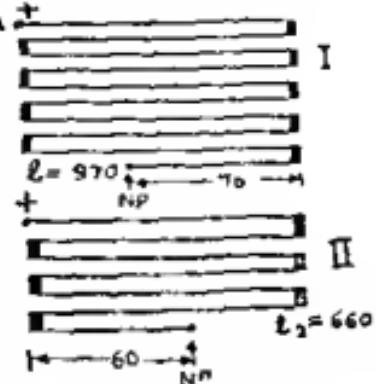


Fig. 17.2

**Procedure—1.** Make the connections as shown in the fig 17-1 i.e., first join in series the plug key, the lead accumulator & the rheostat between the ends A and B of the potentiometer so that a current begins to flow through A B. Next connect positive electrodes of both the given cells at the same end where positive pole of the lead accumulator has already been connected. The negative electrodes of the two given cells are joined to the end terminals of the two way key whose central terminal is connected to one terminal of the galvanometer. The other terminal of the galvanometer is connected to the jockey J sliding over the potentiometer wire.

**2. Testing the connections—** Start the current in wire A B by inserting a plug in the plug key. Next being Leclanche cell (i. e. cell of higher e.m.f.) into the circuit by inserting the plug I in the two way key. Place the jockey J on the first wire and then on the last wire. If galvanometer gives deflections in opposite directions in these two cases, it means the connections are correct. If the deflection remains one sided, check up the connections and see that the positive pole of the lead accumulator, and positive electrodes of Leclanche cell and Daniel cell are all connected to the common point A. If the connections are correct and still one sided deflection is obtained on the first wire and on the last wire, it means the potential difference between A and B is less than the e.m. f.  $E_1$  of the cell, so to increase the potential difference between A and B, increase the current C flowing in the potentiometer wire A B.

(i) by decreasing the resistance in the primary circuit with the help of rheostat

: or (ii) by inserting another lead accumulator in series with the first in the primary circuit.

Again check and see that deflections in opposite directions are obtained on the first wire and on the last wire.

**3. After testing the connections and after the necessary adjustment, explained in step 2, search for the null point and preferably get the null point on the last wire, by adjusting the resistance with the help of rheostat, if necessary. This is done so, because greater the balancing length obtained, smaller will be the**

percentage error. Note the balancing length, i.e., measure the distance of null point D from end A of the wire.

*Note—Distances of null points are to be measured always from the end A, i.e., where positive pole of the battery and positive electrodes of the cells are all connected. Note these distances very carefully. The students usually read 970 as 930 and 660 as 640 (See the figure 17-2).*

4. Next take out plug 1 and insert plug 2 in the two way key so that the other cell (Daniel cell) comes into the circuit. Without disturbing the rheostat (otherwise current C will change), balance the e.m.f.  $E_2$  of this cell against length  $l_2$  of the potentiometer wire.

These values of  $l_1$ ,  $l_2$  constitute one set of observations. Calculate  $\frac{E_1}{E_2}$

5. Next change  $e$ , the potential gradient by adjusting the rheostat and take another set of  $l_1$  and  $l_2$ . In all, 12 to 15 sets may be taken.

*Note:- In a particular set, while determining  $l_1$  and  $l_2$ , the rheostat should not be disturbed.*

Calculate  $\frac{E_1}{E_2}$  separately for every set and then take the mean.

#### Observations and calculations

No. S.	Balancing Length for Leclanche cell $l_1$ in cms.	Balancing length for Daniel cell $l_2$ in cms.	$\log l_1$	$\log l_2$	$x - \log l_1$	$\frac{E_1}{E_2} = \frac{l_1}{l_2}$ —Antilog $x$
1	992.7	675.4				
2	970.0	660.0				
...	...	...				
15	...	432.8				

Mean  $\frac{f_1}{f_2}$  ..... Being a ratio of two similar quantities  
 $\frac{f_1}{f_2}$  has got no units.

Maximum value of Balancing length used for Daniel cell  
 $\approx 675.4$  cm.

Minimum " " " used for Daniel cell  
 $\approx 432.8$  cm.

and e. m. f of Daniel cell = 1.08 volts (given)

So Minimum potential gradient used =  $\frac{1.08}{675.4}$  .... volts/cm.

Maximum " " " " =  $\frac{1.08}{432.8}$  .... volts/cm.

#### Precautions:

1. The positive electrodes of the two cells and the positive pole of the Lead accumulator, all the three must be connected at one point A
2. Choose the lead accumulator of large capacity (in ampere hours) so that current through the potentiometer wire remains steady throughout the experiment.
3. The galvanometer should be shunted to begin with and when the null point is reached, the shunt should be removed.
4. As soon as the null point is determined, open the plug key PK, so that the potentiometer wire does not get unnecessarily heated up.
5. The potential difference between the ends A and B of the wire must be greater than the taken individually otherwise deflection will remain one : first check up the connection increase the current through increase the number of lead :
6. Better get the null point cell in circuit, because greater error.

7. First balance the cell of higher e. m. f. (Leclanche cell). If you balance the cell of lower e.m.f. (Daniel cell) first and get the balancing length—950 cm (say), then with Leclanche cell in the circuit, the balancing length required will be more than 1000 cm, which is not available.

8. Do not disturb the position of the slider on the rheostat i. e., do not change the current through the wire for one set of  $l_1$  and  $l_2$ .

9. Starting with balancing length more than 900 cm for the Leclanche cell control the experiment in such a way that balancing length for Leclanche cell in the succeeding sets is obtained in the decreasing order at a spacing of about 15 to 20 cm. For this, you will have to slide the slider on the rheostat only in ONE direction.

10. Distance of the null point MUST always be measured from the point A where all +ive terminals have been connected. If the null point is obtained on an odd number of wire (3, 5, 7, 9), the reading of the jockey on the scale should be added as such to the full metre lengths (2, 4, 6, and 8 respectively) of wire from A. If null point occurs on an even number of wire (2, 4, 6, 8, 10), the reading of the jockey on the scale should be first subtracted from 100 and then difference added to the full metre lengths (1, 3, 5, 7, 9 respectively) of wire from A.

Sources of error can be due to—

1. Non uniform radius of the potentiometer wire.
2. End resistances.
3. Any variation in the e.m.f. of the lead accumulator which is sending current through the wire.

#### Oral Questions

1. Why potentiometer is so called? Define potential gradient. What are its units?

2. Both the potentiometer and the voltmeter are used to measure the potential difference between two points; which instrument is better and why? Explain the principle of the potentiometer.

3. Why potentiometer is called an ideal voltmeter? Will you choose a voltmeter of higher resistance or lower resistance? Give reasons for your answer.

4. Why is it necessary to connect all the positive terminals at one point? Can't the experiment be performed by connecting all the negative terminals at one point.

5. Why the e.m.f. of lead accumulator should be greater than the individual e.m.f.s. of the two cells? Why the cell of higher e.m.f. should be balanced first?

6. If the jockey J is touched at a point to the left or to the right of the actual null point, the galvanometer gives deflection. Trace the direction of current through the galvanometer in each such case.

7. Why rheostat is not disturbed while taking one set of  $I_1$  and  $I_2$ .

8. Why the potentiometer consists of so many wires, i.e., ten wires? Are these joined in series or in parallel.

9. What will you do, if for the same cell, you want to

" (i) increase the balancing length,

" (ii) decrease the balancing length ?

10. What are the uses of potentiometer?

### Modification

### EXPERIMENT 17·2

Object-Determine the e.m.f. of Leclanche cell after standardising the potentiometer wire with the help of Daniel cell. Also set up a potential gradient of 2 milli volts per cm along the wire and then find the balancing length for the Leclanche cell. Given e.m.f. of Daniel cell = 1·08 volts. (Raj. Univ. 1966)

**Hint:** Proceed for the experimental details exactly in the same manner as under Expt. 17·1, i.e., first balance the Leclanche cell with Daniel cell. Take

## Theory

(a) If a Leclanche cell of e.m.f.  $E_1$  and Daniel cell of e.m.f.  $E_2 = 1.08$  volts (given) are balanced against lengths  $l_1$  and  $l_2$  respectively of the potentiometer wire carrying a constant current,

$$\frac{E_1}{E_2} = \frac{l_1}{l_2}$$

$$\text{i.e., } E_2 = \frac{E_1}{l_1} \times l_2 \quad \dots(1)$$

$\therefore \frac{E_2}{l_2} = \frac{1.08}{l_2} = \epsilon$ , the potential gradient obtained along the wire

$$\text{So } E_1 = \epsilon l_1, \quad \dots(2)$$

where  $l_1$  is measured in cms,  $\epsilon$  in volts-cm and therefore  $E_1$  is given in volts.

(b) How to set up a potential gradient of 2 millivolts/cm?

$$\epsilon = \frac{E_2}{l_2}$$

$$\text{i.e., } 2 \times 10^{-3} = \frac{1.08}{l_2}$$

$$\text{or } l_2 = \frac{1.08}{2 \times 10^{-3}}$$

$$\text{i.e., } l_2 = \frac{1080}{2} = 540 \text{ cm}$$

So current flowing through the potentiometer wire should be so adjusted that the Daniel cell is balanced against length 540 cm of the potentiometer wire.

## Observations and Calculations

$\frac{S}{\Sigma}$	Balancing length for Leclanche cell $l_1$ in cms	Balancing length for Daniel cell $l_2$ (in cms)	Potential gradient obtained $\therefore \frac{E_2}{l_2} = \frac{1.08}{l_2}$	e.m.f. of Leclanche cell $E_1 = ?$
1.			..... Volts/cm	
2.				
...				
...				
...				
...				
10				

Mean e.m.f. of Leclanche cell = ..... volts

To set up a potential gradient of 2 millivolts/cm, place the jockey at a distance of 540 cm (as calculated above in theory) from the end A of the wire and adjust the position of the slider on the rheostat so that galvanometer reads zero deflection. After this setting is made, do not disturb the rheostat and find the balancing length for Leclanche cell. See that this balancing length multiplied by  $2 \times 10^{-4}$  gives a result equal to the mean value of e.m.f. of Leclanche cell already determined.

## Modifications

## EXPERIMENT 17.3

Object—Using potentiometer, determine the internal resistance of a primary cell (say Leclanche cell).

## Apparatus

Potentiometer, an accumulator, a rheostat, two one way plug ....... bat. Leclanche cell, connecting wires.

## Theory and formula

Let  $C$  be the constant current flowing through the potentiometer wire whose resistance per cm length is  $\rho$ . When key  $K_2$  is open i. e., cell is not shunted, its e.m.f.  $E$  is balanced against length  $l_1$  of the potentiometer wire, so that

$$E = Cl_1 \rho \quad \dots(1)$$

Next key  $K_2$  is closed and a plug of  $R$  ohms taken out from the  $R$ . Box. It means the cell is shunted with resistance  $R$  and a

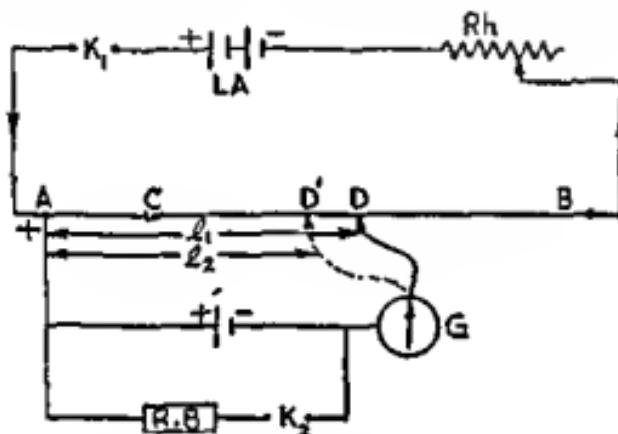


Fig 17.3

current  $i$  begins to flow through  $R$  and the cell. Consequently the p. d. between the electrodes of the cell falls from  $E$  to  $V$ . This p.d.  $= V$ , is balanced against length  $l_2$  of the potentiometer wire.

$$\text{So } V = Cl_2 \rho \quad \dots(2)$$

$$\text{Dividing } \frac{E}{V} = \frac{Cl_1 \rho}{Cl_2 \rho}$$

$$\text{i. e. } \frac{E}{V} = \frac{l_1}{l_2} \quad \dots(3)$$

$$\text{Also } E = i(R + r)$$

$$\text{and } V = iR$$

$$\text{Dividing } \frac{E}{V} = \frac{R + r}{R}$$

$$\text{i. e., } \frac{E}{V} = 1 + \frac{r}{R}$$

Substituting for  $\frac{E}{V}$  from (3)

$$\frac{l_1}{l_1} = 1 + \frac{r}{R}$$

$$\text{i. e., } \frac{r}{R} = \frac{l_1}{l_2} - 1$$

$$\text{or } \frac{r}{R} = \frac{l_1 - l_2}{l_2}$$

$$\text{i. e., } r = R \cdot \frac{l_1 - l_2}{l_2}$$

Knowing  $R$ ,  $l_1$  and  $l_2$ , the value of  $r$  can be calculated.  $l_1$  is the balancing length when cell is not shunted with any resistance and  $l_2$  is the balancing length when the cell is shunted with resistance  $R$  ohms from the resistance box.

### Procedure

1. Make the connections as shown in the figure 17-3.

2. Close plug key  $K_1$  so that the lead accumulator starts sending current through the potentiometer wire (keep  $K_2$  open). Test the connections by pressing the jockey on the first wire and on the last wire. Deflections obtained in opposite directions in these two cases would mean the connections are correct. If deflection remains one sided, check the connections and if the connections are also correct, then increase current through the potentiometer wire by adjusting the rheostat so that galvanometer gives deflections in opposite directions on the first and on the last wire.

3. After testing the connections as above, place the jockey on the last wire, preferably near the other end  $B$  of the wire and adjust the position of the slider on the rheostat so that galvanometer gives zero deflection. Measure the distance of the null point from the end  $A$ , of the wire. This is  $l_1$ , corresponding to e. m. f.  $E$  of the cell.

*Note:—The above adjustment for having maximum value of  $l_1$  is essential and preferable because then sufficient length of the wire will be available to us, for having different values*

of  $l_2$ , to be obtained subsequently ( $l_3$  is to be less than  $l_1$  always provided constant current is passed through the wire.)

4. Next close plug key  $K_2$  also, and take out a plug of resistance  $R$  ohms— $5\Omega$  (say) from the resistance box, so that a current begins to flow through  $R$  and the cell and therefore p.d. between the electrodes falls from  $E$  to  $V$ . Balancing length  $l_2$  corresponding to  $V$  is obtained and measured.

5. Knowing  $R$ ,  $l_1$  and  $l_2$ , value of  $r$ , the internal resistance of the cell can be determined using the formula

$$r = R \left( \frac{l_1 - l_2}{l_2} \right)$$

6. For obtaining different sets, shunt the cell with different resistances ( $R$  may be changed in steps of one or two ohms). Find balancing length  $l_2$  everytime and thus calculate  $r$  separately for every set. Its value will be different for different sets.

*Note:—Value of  $l_1$  should be checked everytime when  $l_2$  is measured, although  $l_3$  is expected to be constant if rheostat is not disturbed.*

#### Observations and Calculations

$\Sigma$ $n$	Resistance in R. Box, $R$ (ohms)	Balancing length when cell is NOT shunted with $R$ . $l_1$ in cm	Balancing length when cell is shun- ted with $R$ . $l_2$ in cm	$l_1 - l_2$	$r = R \cdot \frac{l_1 - l_2}{l_2}$
1.	Ohm	cm	cm	cm	Ohm
2.					
3.					
4.					
5.					
6.					

Mean value of  $r = \dots \text{ ohms}$

But we see that value of  $r$ , the internal resistance of the cell

it NOT a constant quantity. It increases with the current drawn from the cell.

### **Additional Precautions**

1. Basically the formula for internal resistance is  $r = R - \frac{E-V}{I_2}$ .

Here  $E$  is constant, so for taking different sets  $V$  must be changed by changing the value of  $R$ . In other words, different values of  $I_2$  should be obtained by shunting the cell with different resistances. Of course,  $I_2$  could be changed by changing the current through potentiometer wire also but that would NOT be preferable, because that would not amount to changing the value of  $V$ .

2. First balance the cell without shunting it and then balance the same cell after shunting it with resistance  $R$ . If shunted cell is balanced first, then on balancing the cell on open circuit, the required balancing length may not possibly be available.

3. In no case, disturb the rheostat for one set of  $I_1$  and  $I_2$ . It would be advisable NOT to disturb it for other sets also because in other sets,  $I_2$  can be varied by using different values of  $R$ .

### **Oral Questions**

1. What do you mean by the internal resistance of a cell?

Ans—It is the resistance offered by the electrolyte to the flow of current inside the cell.

2. Upon what factors does the internal resistance depend?

3. What is the physical effect of internal resistance of a cell? Should the internal resistance of a cell be high or low?

4. Why is the internal resistance of a lead accumulator so low as '01 ohms, whereas the internal resistance of a Leclanche cell is 4 to 5 ohms?

5. Can this method be used in case of a cell having a very low internal resistance?

6. Can or should  $I_1$  be kept constant in all the observations?

7. What is the difference between e.m.f. and potential?

8. Will the internal resistance of a cell increase or decrease if—

- The distance between the electrodes is increased ?
- More electrolyte is added ?
- The electrodes are raised vertically upwards so that their length dipping in the electrolyte decreases ?
- More current is drawn from the cell ?
- The temperature of the electrolyte is increased ?

#### EXPERIMENT 17·4

Using potentiometer—

- Compare to given resistances.
- Determine a given low resistance.

**Hint :** Consult a book on theory or consult your teacher in-charge and try to do the experiment, independently.

#### EXPERIMENT 17·5

**Object—** Compare the e. m. f.'s. of two cells by sum and difference method using potentiometer.

**Hint—** Let  $E_1$  and  $E_2$  be the e.m.f.s. of the two given cells,  $E_1$  being higher than  $E_2$ .

If the negative pole of the cell of e. m. f.  $E_1$  is joined to the positive pole of the cell e. m. f.  $E_2$ , the e. m. f. of the combination is equal to their sum  $E_1 + E_2$ . Let the e.m.f. of this combination be balanced against length  $l_1$  of the potentiometer wire, through which constant current  $C$  is flowing.

$$\text{Then } E_1 + E_2 = C l_1 P \quad \dots(1)$$

If the negative pole of the cell of e. m. f.  $E_1$  is joined to the negative pole of the cell of e.m.f.  $E_2$ , the e.m.f. of the combination is equal to their difference  $E_1 - E_2$ . Let the e.m.f. of this combination be balanced against length  $l_2$  of the wire.

$$\text{Then } E_1 - E_2 = C l_2 P \quad \dots(2)$$

$$\text{Dividing } \frac{E_1 + E_2}{E_1 - E_2} = \frac{l_1}{l_2}$$

Apply component law and divide by  
 $\frac{R_1 + R_2 + R_3}{R_1 + R_2} = \frac{I_1 + I_2}{I_1 - I_2}$

$$\frac{E_1 + E_2 + E_3}{E_1 + E_2} = \frac{I_1 + I_2}{I_1 - I_2}$$

$$\text{Le., } \frac{E_1}{E_2} = \frac{I_1 + I_2}{I_1 - I_2}$$

So knowing  $I_1$  and  $I_2$ , the e.m.f.s. of the two cells can be

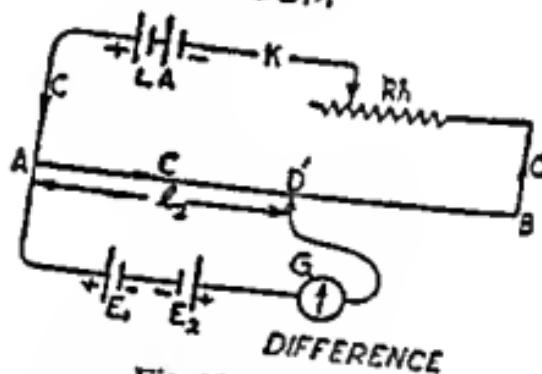
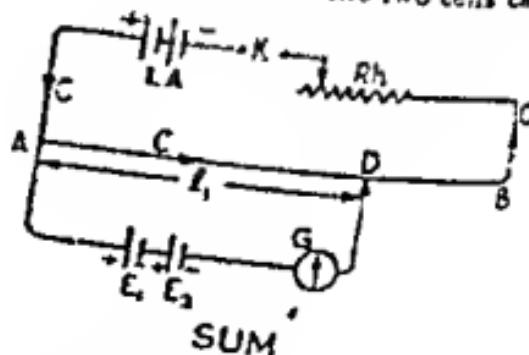


Fig. 17.4

Note:—In both the combinations, the positive pole of the e.m.f. of higher e.m.f. ( $E$ ) is to be connected at A i.e. where positive pole of the battery of the primary circuit is connected.

## ELECTROLYSIS AND VOLTAMETER

The process of decomposition of a liquid or a solution into ions, on passing electric current through it, is called electrolysis. The liquid or solution is called the electrolyte and the plates placed in the electrolyte are called electrodes. The plates connected to the positive and the negative pole of the battery are called the anode and the cathode respectively. The vessel containing the electrolyte and electrodes is known as voltameter.

(Note :—The difference between voltameter and voltmeter.)

As a matter of fact, the ions are already present in the solution itself. The passage of electric current simply helps the ions to move to opposite electrodes.

∴ The voltameter can be used for the following purposes.

- (1) Preparing gramophone records and printing blocks.
- (2) Polishing metals.
- (3) Comparing the equivalent weights.
- (4) Determining Avogadro's Number.

A copper voltameter consists of a glass vessel containing  $\text{CuSO}_4$  solution and three copper plates dipping into the solution. The two outer plates are placed parallel, a suitable distance apart and joined together by metallic strips to a common terminal. These are connected to the positive pole of the battery and hence constitute the anode. The cathode is constituted by the third copper plate placed parallel to and between the two outer plates, having its own binding terminal, which is connected to negative pole of the battery. (directly or indirectly through other apparatuses).

## EXPERIMENT 18.1

**Object**—Determine the electrochemical equivalent of copper using copper voltameter.

Employ a tangent galvanometer as a current measuring instrument.

**Apparatus**—A copper voltameter, a lead accumulator, rheostat, a tangent galvanometer having coils of different turns, a plug key, a reversing key, a physical balance and a weight box containing fractional weights of superior quality. A large beaker containing water, an air blower, connecting wires, sand paper etc.

**Theory and Formulae** :—

According to Faraday's first law of electrolysis, the mass of ions deposited on the cathode is

(i) directly proportional to the current  $c$  passed through the electrolyte,

(ii) the time  $t$  for which the current is passed.

$$\text{So } m \propto c$$

$$\text{and } m \propto t$$

$$\text{i.e., } m \propto c t$$

or  $m = Z c t$ , where  $Z$ , the constant of proportionality is known as the electro chemical equivalent of the metal used as anode.

$$\text{So } Z = \frac{m}{ct} \quad \dots(1)$$

$ct = q$ , the charge for which the unit is coulomb.

Hence units of  $Z$  will be gms per coulomb.

The magnetic field  $F$  acting on the magnetic needle pivoted at the centre of a coil, due to current  $c$  amperes flowing in the coil is  $F = \frac{2\pi n e}{10 r}$

If the tangent galvanometer is set in the magnetic meridian and the magnetic needle makes  $\angle \theta$  with the field  $H$ , due to earth, passing current through it, then

$$\begin{aligned} F &= H \tan \theta \\ \frac{2\pi n c}{10 r} &= H \tan \theta \\ \text{i.e. } c &= \frac{10 r H}{2\pi n} \tan \theta \end{aligned} \quad \dots (2)$$

Substituting the value of  $c$  from equ (2) in equ (1).

$$Z = \frac{m}{t} + \frac{2\pi n}{10 r l \tan \theta} \quad \dots (3)$$

$m$ —mass (in grams) of copper deposited on the cathode plate.

$t$ —the (in secs) time for which the current is passed.

$n$ —the number of turns of the coil in tangent galvanometer used.

$r$ —radius (in cms) of the coil of the tangent galvanometer.

$H$ —the horizontal component of Earth's field, at the place of experiment, (measured in Oersteds)

$\theta$ —the mean deflection of the magnetic needle pivoted at the centre of the tangent galvanometer coil.

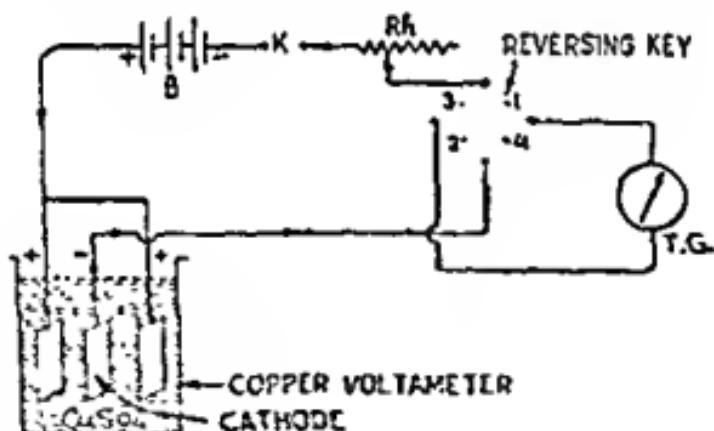


Fig. 18-1

#### Procedure

1. Make the connections as shown in the figure 18-1. See that you have connected the tangent galvanometer between the opposite terminals of the reversing key and NOT between the

neighbouring terminals. In case of these connections made between the neighbouring terminals, the current through the tangent galvanometer will NOT get reversed when subsequently desired to do so. Between the other pair of opposite terminals the reversing key, an electrical circuit is developed through voltameter as shown in the figure IS-I.

2. See that the rheostat and the tangent galvanometer are placed close to each other, because in that case magnetic field due to current flowing through the rheostat will affect the deflection of the tangent galvanometer. There should be no magnetic substance placed near the tangent galvanometer. To keep the galvanometer and the rheostat far removed from each other, a long one piece connecting wire. Do not join two wires in air.

3. Remove the cathode plate from the voltameter and rub on both sides with sand paper to remove any spots present on it. Wash it with water, dry it and then weigh it in an accurate balance, keep this weighed plate in reserve to be used subsequently in the actual experiment. For testing the connections and adjusting the current, a rough plate (dummy plate) is used as cathode in place of this weighed plate.

4. Preparing the electrolyte—Dissolve 30 gms of copper sulphate crystals in 600 ccs of distilled water (mass = 600 gm). Specific gravity of the solution =  $\frac{630}{600} = 1.05$ . Make the solution slightly acidic to make it conducting.

Calculate the area on both sides of the cathode plate dipping into the electrolyte. (NOT the total area but only the area inside the solution). To get a smooth and firm deposit, the current required is one ampere for 100 sq. cm area, of the cathode plate calculated above, provided the solution of specific gravity = 1.05, as prepared above is used.

5. Setting the tangent galvanometer—Take the compass box of the tangent galvanometer horizontal with the help of a spirit level. By looking from above with one eye closed, make the galvanometer coil parallel to the magnetic needle pivoted at the centre of the coil. Rotate the compass box to make the pointer read 0-0.

Next close key K and then insert opposite plugs 1 and 2 in the reversing key. Read both the ends of the pointer. Then take out plugs 1 and 2 and insert these in positions of 3 and 4 so that the current through the galvanometer coil gets reversed. Again read both the ends of the pointer. These readings should be the same as those recorded before reversing the current, and if the readings differ, they should differ slightly to  $1^\circ$  or  $2^\circ$ . If the difference is more, it means the coil has not been set properly in the magnetic meridian. So adjust its position and check that the deflection remains numerically the same before and after reversing the current. This is ONLY TEST of ensuring that the galvanometer coil has been set in the magnetic meridian.

6. Determining the radius of the coil—Pass a thread around the coil a number of times, say six times completely. Find its length and divide it by 6. This is the mean circumference  $2\pi r$ , from which  $r$ , can be calculated.

7. Choosing the proper number of turns of the coil and adjusting the current—Adjust the current with the help of rheostat so that with a 5 turn coil used, the deflection is in the vicinity of  $45^\circ$  (because for a deflection of  $45^\circ$ , the sensitivity is maximum.) Substituting these values of  $n$  and deflection  $\theta$ , in the formula  $C = 10 \frac{r H \tan \theta}{2 \pi n}$ , roughly. Calculate the current C and see that it is approximately the same as desired in step 4.

*Note:—A proper co-ordination of  $n$  and  $\theta$  to have the desired value of C is essential. Sometimes when a large number of turns is used, resulting in a large deflection, the current C is so small that a detectable deposit is not obtained.*

*Sometimes when a small number of turns is used, then even for a small deflection, the current will be so large that the large deposit obtained will not be firm.*

8. Testing the connections—Allow the current to flow for about five minutes with the dummy plate used as cathode. If after five minutes, on stopping current and taking out the plate, a deposit is observed on it, it means the connections are correct.

*Note:—Sometimes, by mistake, the students connect the central plate to the positive pole of the battery and the outer plates to the negative pole. They discover to their surprise, at the end of the experiment, that no deposit has been obtained on the central plate, whose mass instead of having increased, has decreased. This is because deposit has been obtained on the outer plate due to the movement of ions from the central plate.*

9. After setting the tangent galvanometer, adjusting the current and testing the connections, proceed with the actual experiment by replacing the dummy plate by the experimental plate weighed already. Start the current and the stop watch simultaneously. Read the ends of the pointer. If the deflection tends to change, keep it constant by adjusting the rheostat. Allow the current to flow for 15 minutes.

10. After 15 minutes, reverse the current through the tangent galvanometer. Pass the same constant current for another 15 minutes, noting the deflection again. After a total of 30 minutes, stop the current, remove the cathode plate, and immediately dip it into a beaker containing water. Move the plate to and fro in water so that any trace of  $\text{CuSO}_4$  solution on the plate is removed. Dry the plate in the sun or by blowing on it hot air from an air blower. Weigh the plate again and thus find the mass of copper deposited on it.

11. The value of  $H$  for that place, where the experiment has been performed, can be consulted from tables. Calculate  $Z$  using the formula (3) given above.

#### Observations

1. Mass of the cathode plate before passing current— $m_1$ ...gm
2. " " " after deposition of copper— $m_2$ ...gm
3. Mean circumference of the coil,  $2\pi r$  .....cm  
radius of the coil  $r$  .....cm
4. The value of  $H$  at the place (given) .....gauss/cm
5. The number of turns of the coil used .....—

For deflection of the tangent galvanometer

No. S.	Time for which current is passed	Direction of current through T. G.	Deflection at one end	Deflection at the other end
1	15 minutes	One direction	.....	....
2	15 minutes	opposite direction	.....	.....
3				

$$\text{Mean deflection } \theta = \frac{\theta_1 + \theta_2}{2} = \dots$$

$$\begin{aligned}\text{Total time for which current has been passed} &= t = 30 \text{ minutes} \\ &\approx 1800 \text{ seconds}\end{aligned}$$

### Calculations

$$\text{Mass of copper deposited} = m_2 - m_1 = m = \dots \text{gms}$$

$$Z = \frac{m}{t} \cdot \frac{2\pi n}{(0.91 \tan \theta)}$$

$$\approx \dots \text{gms/coulomb}$$

Standard result of

$$Z = 0.00329 \text{ gms per coulomb (For copper)}$$

% age error =

### Precautions

1. Before starting the experiment, check the setting of the tangent galvanometer by passing current through it in one direction and then in the opposite direction. The readings of the ends of the pointer should be the same numerically in both the cases and should not differ by more than 2°. In that case reset the galvanometer and recheck.

2. Read the ends of the pointer very carefully. Note that one division on the circular scale = 1° and NOT 0.1°. Sometimes when the correct reading is 47° (say), the students wrongly read it as 53° or as 40.7°. Avoid such mistakes.

3. The actual experimental plate should be rubbed weighed accurately and placed separately. In its place (dummy plate) is used for the purpose of setting the meter, adjusting the current and testing the connections.
4. The outer plates should be made the anode by connecting their common terminal to the positive pole of the battery. The central plate should be connected to the negative pole. Connections should be tested by passing the current for a few minutes. If a deposit occurs on the cathode plate, then connections are correct.
5. The number of turns of the coil used should be neither less nor too large. A 5-turns coil will best serve the purpose.
6. The rheostat should be far removed from the galvanometer, otherwise on passing current, the rheostat will become a solenoid and affect the deflection of the galvanometer if they are placed near to each other.
7. Current should be kept constant throughout the experiment with the help of rheostat.
8. At the end of the experiment, the cathode plate on which deposit has been made, should be placed under running water so that traces of  $\text{CuSO}_4$  solution present on the plate may be removed.
9. The electrolyte should be made slightly acidic to make it non-conducting.

#### Oral Questions

1. What is a voltmeter? Is it different from voltmeter?
2. What is electrolysis? State Faraday's law of electrolysis.
3. Define electro-chemical equivalent. What is chemical equivalent?
4. How current flows through the electrolyte?

6. What precautions will you take to get a good deposit ? Why is it necessary to clean the cathode plate before starting the experiment ?

7. Could not the current be measured by an ammeter ? Why the tangent galvanometer is used ?

8. Why the current is reversed ? Does the current get reversed through the voltameter also.

9. Could A. C. be used in this experiment ? Give reasons for your answer.

10. Why two anode plates are used ? Couldn't the experiment be performed by using single anode and a single cathode ?

11. In the formula used,  $m$  is the mass of copper deposited on the cathode, and  $m$  is thus found out by determining the increase in the mass of the cathode. Could not  $m$  be determined by finding the decrease in mass of the anode.

#### Modifications

#### EXPERIMENT 18.2

**Object**—Using copper voltameter, determine the reduction factor of the five turn coil of a tangent galvanometer. Verify the result by direct calculations. Given E. C. E. of copper = 0.000329 gms per coulomb.

**Hint :** The procedure of performing the experiment is exactly the same as that of the experiment 18.1.

$$Z = \frac{m}{ct}$$

$$\text{and } C = 10 K \tan \theta$$

where  $K$  is the reduction factor of the T. G.

$$\text{So } Z = \frac{m}{10 K \tan \theta \cdot t}$$

$$\text{or } K = \frac{m}{10 Z \tan \theta \times t} \quad \dots(1)$$

Knowing  $m$ ,  $t$  and  $\theta$ , value of  $K$  can be determined,  $Z$  being known to us.

By direct calculations,

$$K = \frac{IH}{2\pi a} \quad \dots(2)$$

Where  $r$  is the radius of the coil,  
 $n$  is the number of turns of the coil used,  
and  $H$ —the horizontal component of Earth's field at the place of experiment.

So knowing these quantities,  $K$  can be directly calculated from equation (2) and then its value compared with that determined from Equation (1).

### Result

Experimental value of  $K$  determined from Equation (1)=.....  
amperes.

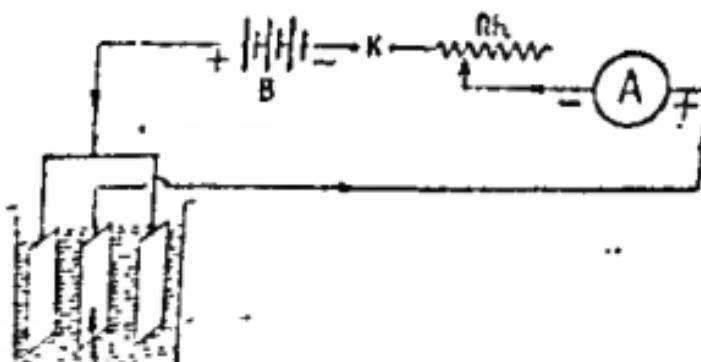
Value of  $K$  by direct calculations using Equation (2)=.....  
amperes.

Difference of the two values=.....

### EXPERIMENT 18.3

**Object**—Using copper voltameter and an ammeter, determine the E. C. E. of copper. Using the value of E. C. E. determined by you calculate the charge in coulombs required to  
deposit (1) One gm of copper.  
(2) One gm-equivalent of copper.

### Circuit diagram



## Apparatus

A copper voltameter with an extra test plate of copper, a battery, key, a rheostat, an ammeter of range 1.5 ampere and with a small least count, a physical balance and a weight box, sand paper and connecting wires etc.

## Theory and formulae

$$\text{or } \boxed{\tau = \frac{m}{ct}} \quad \dots(1)$$

## Procedure

The experiment is performed on the same lines as described in experiment No. 18.1 the only difference is that instead of a tangent galvanometer, an ammeter is used for measuring the current and thus the current is directly known to us. Noting the time for which current is passed and finding the mass of copper deposited on the cathode, the value of  $Z$  can be calculated from equation. (1)

Suppose the value of Z determined by you

Is  $Z = 0.0003182$  gms/coulomb. It means,

for depositing 0.0003182 gms of copper, charge required = 1 Coulomb

$$\text{So } \dots \quad 1 \quad \dots \quad \dots \quad \dots \quad -\frac{1}{0.003182} \text{ Coulomb}$$

We know At. wt. of copper = 63.5

### **Valency of copper - 2**

So Equivalent weight =  $\frac{\text{At. wt.}}{\text{Valency}}$ :

$$-\frac{63.5}{2} = -31.75$$

So gm equivalent of copper = 31.75 gms of copper. Therefore depositing one gm equivalent of copper to ...

31.75 gms of copper, the charge required =  $\frac{31.75}{0.0003182}$  coulomb  
 = 99790 coulombs

## MECHANICAL EQUIVALENT OF HEAT

According to first law of thermodynamics, heat and work are inter convertible and work done is always proportional to the heat i. e.  $W \propto Q$

or  $W = J H$ , where  $J$ , the constant of proportionality is called Mechanical Equivalent of heat.

$$J = \frac{w}{H}$$

J and Joule's calorimeter have been named after Joule, the scientist.

## **EXPERIMENT 19-1**

**Object**--Determine the value of  $J$ , the mechanical equivalent of heat, using Joule's calorimeter.

**Apparatus**—Joule's calorimeter, a 6 volt battery, a rheostat, a voltmeter of 6 volts range and an ammeter of 3 amperes range, a thermometer of least count =  $\frac{1}{10}$  °C., a physical balance and a weight box, stop watch, a plug key, connecting wires, sand paper etc.

### Theory and formula

**Work done by current—P. D.** between two points is defined as the work done to carry unit charge from one point to another. If p. d. between two points is  $V$ ,  
the work done to carry unit charge between those points— $V$

$$\text{so } " " " \text{ so work done } W = Q V = QV$$

$$\text{So } W = VCt$$

$$\text{Ohm's Law gives } V = CR$$

$$\text{So } W = CR \cdot Ct = C^2 R t$$

So if  $V$ ,  $C$  and  $R$  are measured in c. m. u.

$$W = VCt = C^2 R t$$

if  $V$ ,  $C$  and  $R$  are measured in practical units, i.e. in volts, amperes and ohms respectively

$$W = VCt \times 10^7 = C^2 R t \times 10^7 \text{ ergs} \quad \dots(2)$$

$$\text{Heat produced } H = (M + ms)(\theta_2 - \theta_1) \quad \dots(3)$$

Where  $M$ —mass of water contained in the calorimeter,

$m$ —mass of calorimeter.

$s$ —specific heat of the material of the calorimeter.

$\theta_1$ —the initial temperature.

$\theta_2$ —the final temperature.

$$I = \frac{W}{H} = \frac{VCt \times 10^7}{(M + ms)(\theta_2 - \theta_1)} \text{ ergs/calorie} \quad \dots(4)$$

#### Procedure

1. Remove the ebonite knob of the stirrer and weigh the stirrer along with Joule's calorimeter, after properly cleaning the calorimeter. Note this mass  $m$ .

2. Pour water into the calorimeter, sufficient enough to immerse the heating coil in it. Filling half of the calorimeter would serve the purpose. Weight the calorimeter, and the stirrer along with the contents (water) and out of this mass, subtract  $m$ , the mass of calorimeter and stirrer. This will be  $M$ , the mass of water.

3. Replace the lid of the calorimeter and pass the stirrer through one hole of the lid. Also replace the knob of the stirrer. Pass the thermometer through the piece of rubber which fits into the

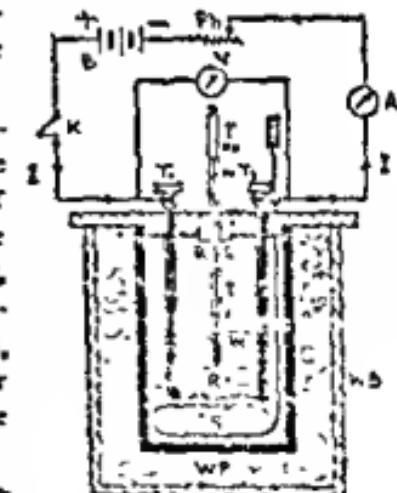


Fig. 19-1

central hole of the lid. By giving a screw type motion to the thermometer, adjust the height of the thermometer bulb so that bulb dips into water and at the same time it does not touch heating coil.

4. Make the connections as shown in the figure 19-1. It will require a battery of three or four lead accumulators joined in series. See that positive terminal of the voltmeter and of ammeter are connected directly or indirectly through other instruments to the positive pole of the battery.

*Note—1. If positive terminal of the ammeter is joined to negative pole of the battery, the needle will be deflected towards the left beyond the zero division of the scale of the ammeter.*

2. Sometimes when the voltmeter DOES give the reading but the ammeter reads zero, it usually indicates that the heating coil is broken and thus circuit is not being completed so check the coil.

3. Close the plug key and adjust the rheostat so that voltmeter reads between 4 to 6 volts. Do not apply more than 6 volt because then electrolysis will set in and which is not desired. So after setting the current in this way, open the plug key.

6. Stir water in the calorimeter and note its initial temperature  $\theta_1$ . Start current in the circuit by closing the plug key and at the same time start the stop watch also.

7. Go on stirring the liquid with the stirrer and see that the current remains constant. If current tends to change, keep it constant by adjusting the rheostat.

8. When temperature has risen by about 5 or 6°C, stop the current and simultaneously note the time  $t$  (in seconds) for which the current has been passed. Record the highest temperature reached. Let it be  $\theta_2$  °C.

#### Applying the radiation correction

9. After the highest temperature has been reached, it will start falling. Go on stirring and note the fall in temperature  $\Delta\theta$  in the same time  $t$ , for which the current had earlier been

**Observations**

1. Mass of the calorimeter and stirrer  $m = \dots \text{gms.}$
2. Mass of the calorimeter + stirrer + liquid (water)  $= M_1 = \dots \text{gms.}$
3. So mass of water  $= M = M_1 - m = \dots \text{gms.}$
4. Specific heat of the material of the calorimeter  $s = \dots$
5. Initial temperature of water  $\theta_1 = \dots ^\circ\text{C}$
6. P. D. applied, i. e., voltmeter reading  $V = \dots \text{volts}$
7. Current passed, i. e., ammeter reading  $I = \dots$   
amperes.
8. Time for which current is passed  $= t = \dots \text{minutes}$
9. Apparent final temperature  $\theta_2' = \dots ^\circ\text{C.}$
10. Fall in temperature of water recorded in the  
same time  $t$  is  $\Delta\theta = \dots ^\circ\text{C.}$
11. Corrected final temperature  $\theta_2 = \theta_2' + \frac{\Delta\theta}{2}$

$$J = \frac{Vct \times 10^7}{(M + ms)(\theta_2 - \theta_1)} \text{ ergs per calorie}$$

**Results**

$$J = \dots \text{ergs per calorie}$$

Standard result  $J = \dots \text{ergs per calorie}$

% error =

**Precautions**

1. The thermometer should be so adjusted that its thermometer bulb remains immersed in the liquid and at the same time, it does not touch the heating coil.
2. Don't take much time in adjusting the initial potential difference and the current.
3. Don't set the potential difference to a value greater than 6 volts because as a higher potential difference electrolysis will set in. So the work done by current will not be wholly utilized in raising the temperature of the liquid.

4. Use a very sensitive thermometer, of least count equal to  $\frac{1}{10}$ °C,

5. Throughout the experiment current in the circuit should be kept constant. If the current tends to change, keep it constant by adjusting the rheostat. Use lead accumulators of large ampere-hour capacities so that a constant supply of current is obtained for a long time.

6. Radiation correction must be applied to account for the loss of heat due to radiation. For this purpose, after the current is switched off, allow the liquid to cool, (while stirring it all the time) for the same time  $t$ , during which the current was passed. Note the fall in temperature. Then corrected rise in temperature = observed rise in temperature plus half of this fall in temperature

7. Stop the current as soon as the temperature rises by 5 or 6°C. A greater rise of temperature is not desirable because it will cause large radiation and for which the radiation correction explained in step 6 will not be applicable.

8. Sometimes when the heating coil is broken, the voltmeter DOES give deflection but the ammeter reads zero. In such a situation, check the heating coil and replace it or solder its snapped ends.

9. Current more than the rated capacity of the lead accumulator should not be drawn because large current drawn would produce large heat and so the lead plates in the accumulator will buckle and get spoiled.

#### Sources of error

1. The masses involved can not be determined very accurately.

2. The temperature throughout the mass of the liquid does not remain uniform.

3. Different parts of the apparatus possess different specific

precautions is only an approximation. It does NOT exactly account for the loss of heat due to radiation.

5. The thermometer also absorbs some heat and it is not taken into account.

6. The whole of the current as read by the ammeter does NOT pass through the heating coil. A part of it (through very small) passes through the voltmeter to cause deflection in it.

7. Some cooling is caused due to evaporation of the liquid from its surface.

8. The resistance of the heating coil changes when its temperature rises on passing current.

9. It is difficult to read exactly the temperatures which are not constant. A changing temperature involves some error in its measurement.

### Oral Questions

1. State first law of thermo dynamics and derive Joule's mechanical equivalent of heat.

2. What are the important precautions to be observed in this experiment and what are the sources of error ?

3. What is radiation loss ? How is it reduced and how a correction is applied to account for the radiation loss ?

4. Is there any upper limit for the potential difference applied ?

**Ans.** Yes, about eight volts. A large p. d. applied will cause electrolysis and so the work done by current will not wholly get converted into heat.

5. Can you determine the specific heat of a liquid by this method.

**Ans.** Yes, if  $J$  is given to us.

6. What is the material of the heating coil used ?

**Ans.** In principle the wire should be of manganin so that its resistance remains constant with increase in temperature. However, since the ammeter and the voltmeter used are not sensitive, these

can't detect any such change in resistance. So a wire of nichrome is used, nichrome being cheap and possessing a high specific resistance also.

7. Is this an accurate method of determining  $J$ ? If not, why not?

8. Enumerate other methods of determining  $J$ . Which one is the best and why?

9. Name the liquid you will prefer to use in this experiment.  
Modifications

### EXPERIMENT 19.2

**Object**—Determine the water equivalent of Joules' calorimeter and determine your result by direct calculations also. Given  $J = 4.18 \times 10^3$  ergs per calorie  
(R. U., 1966, 1967)

$$\text{Hint: } J = \frac{W}{t}$$

$$\text{or } J = \frac{Vct \times 10^3}{(M + w)(\theta_2 - \theta_1)}$$

$$M + w = \frac{Vct \times 10^3}{J(\theta_2 - \theta_1)}$$

$$\text{or } w = \frac{Vct \times 10^3}{4.18 \times 10^3 (\theta_2 - \theta_1)} - M$$

$$w = \frac{Vct}{4.18 (\theta_2 - \theta_1)} - M \quad \text{and}$$

$w$ , is the water equivalent of the calorimeter, and  $M$  is the mass of water contained in the calorimeter,  $t$  is the time in seconds for which the current is passed. The procedure is the same as in experiment No. 19.1.

**By direct calculations**

determined from equation (1) can come out to be negative also. Think why it can be so?

### EXPERIMENT 19·3

Object—With the help of Joule's calorimeter, find the specific heat of the given liquid. Given  $J=4.2 \times 10^7$  ergs per calorie.

(R. U. 1966, 69)

Hint : Use the given liquid in place of water and perform the experiment according to the details of experiment 19·1

Let  $M$  be the mass of the given liquid whose specific heat is  $S$ . Then

$$J = \frac{Vct \times 10^7}{(MS + w)(\theta_2 - \theta_1)}$$

$$MS + w = \frac{Vct \times 10^7}{J(\theta_2 - \theta_1)}$$

$$MS = \frac{Vct \times 10^7}{4.2 \times 10^7 (\theta_2 - \theta_1)} - w$$

$$S = \frac{Vct}{4.2(\theta_2 - \theta_1) M} - \frac{w}{M}$$

$$S = \frac{Vct}{4.2(\theta_2 - \theta_1) m} - \frac{ws}{M}$$

where  $m$  is the mass of calorimeter and stirrer and  $s$  is the specific heat of the material of the calorimeter ( $w=ms$ )

**Modification**

### EXPERIMENT 19·4

Object—Without using voltmeter, determine the resistance of the heating coil of Joule's calorimeter. Verify your result by Post Office Box. Given  $J=4.2 \times 10^7$  erg/calorie (R. U. 1966, 69)

$$J = \frac{W}{H} = \frac{Vct \times 10^7}{(M+w)\theta_2 - \theta_1} = \frac{e^2 R t \times 10^7}{(M+w) \times 6 \times 60}$$

$$\therefore R = \frac{J(M+w)(\theta_2 - \theta_1)}{e^2 \times 10^7}$$

$$\text{I.e., } R = \frac{4.2(M+w)(\theta_2 - \theta_1)}{e^2} \text{ ohms}$$

Where the symbols have their usual meaning. For verification, connect the ends of heating coil through its thick metallic rods, and connecting wires, infinite, fourth arm of Post Office Box and find out the resistance as usual. Then compare the two values.

**Modification**

### EXPERIMENT 19.5

**Object** - Determine  $J$  with Joule's calorimeter using copper voltameter.

Given E. C. E. of copper = 0.000329 gm/coulomb

$$\text{Hint : } J = \frac{W}{H} = \frac{Vct \times 10^7}{(M+w)(\theta_2-\theta_1)}$$

$$\text{mass of copper deposited } m = Zct \quad \text{or} \quad ct = \frac{m}{Z}$$

$$J = \frac{Vm}{Z(M+w)(\theta_2-\theta_1)} \times 10^7 \text{ ergs/calorie}$$

Join copper voltameter and Joule's calorimeter in series so that the same current passes through both for the same time  $t$ , in which (1)  $m$  gms of copper is deposited on the cathode of voltameter and (2)  $M$  gms of water contained in Joule's calorimeter of water equivalent  $w$ , gets heated up from  $\theta_1$  to  $\theta_2$  °C. Substituting all these values,  $J$  can be calculated.

---

**APPENDIX**  
**Some useful Physical constants**

Table I Properties of solids

Solid	Young's modulus of elasticity Y Dynes/sq. cm.	Density d gm./c.c.	Specific heat s per °C	coefficient of Linear expansion L per °C	Thermal conductivity k cal. sec <sup>-1</sup> cm <sup>-1</sup> (deg. °C) <sup>-1</sup>
Aluminium	$7.0 \times 10^{11}$	2.7	0.212	$22 \times 10^{-6}$	0.50
Copper	$(10.5-13.2) \times 10^{11}$	8.69	0.093	17.0 "	0.1
Iron (cast)	$(10-13) \times 10^{11}$	7.60	0.118	10.2 "	0.11
Iron (rough)	$(19-21) \times 10^{11}$	7.85	0.115	11.9 "	0.17
Steel	$(19.5-21.5) \times 10^{11}$	7.7	0.119	11.9 "	0.11
Gold	$8.2 \times 10^{11}$	19.3	0.03	14.0 "	0.70
Silver	$7.8 \times 10^{11}$	10.5	0.056	19.2 "	0.970
Zinc	$(8-11) \times 10^{11}$	7.1	0.093	28.0 "	0.265
Lead	$1.6 \times 10^{11}$	11.34	0.031	29.1 "	0.081
Bronze	$(9.7-10.2) \times 10^{11}$	8.1	0.094	19.0 "	0.26
Glass (flint)	$6.8 \times 10^{11}$	2.9	0.16	8.4 "	0.042
Germanium (Goreka)	$16.1 \times 10^{11}$	5.88	0.98	16.0 "	0.06
Wax (Paraffin)	" " "	0.9	0.49	" "	"
Cork	" " "	2.24	" "	" "	0.12

Table-II Properties of Liquids

Liquid	Density $d$ at $0^{\circ}\text{C}$	Temp. $^{\circ}\text{C}$	Coefficient of volume expansion		Thermal conductiv- ity $K$	
			Cal. per. gm	per $^{\circ}\text{C}$	Cal. sec $^{-1}$ cm $^{-1}$ (deg. $\text{C}^{-1}$ )	Cal. sec $^{-1}$ cm $^{-1}$ (deg. $\text{C}^{-1}$ )
Water	1.0	13.6	-38.8	337	0.013	$1.82 \times 10^{-1}$
Mercury	1.26	17	290	0.310	68	$1.97 \times 10^{-1}$
Gasoline	0.87	-10	159	0.42	70	5.5
Linseed oil	0.80	0	100	0.52	9.4	"
Castor oil	0.9998	0.0	100	1.00	536	9.1
Oil	[1.00 at $44^{\circ}\text{C}$ ]				2.0	"
Ice					1.4	3.6
Mercury (O.H.)	0.79	-113	78	0.58	205	11.6
Mercury (at $15^{\circ}\text{C}$ )	0.89	55	80	0.41	93	12.4
					"	4.2
					"	3.2

Table III-Refractive index  $\mu$  and critical angle (For sodium light)

Material	Refractive Index $\mu$	Critical Angle	Material	Refractive Index $\mu$	Critical Angle
Glass (Flint)	1.65-1.96	37°	Water	1.33	48° 30'
Glass(crown)	1.58-1.56	41°	Alcohol (C <sub>2</sub> H <sub>5</sub> OH)	1.36	...
Ice	1.301	...	Benzene	1.50	...
Diamond	2.24	24°	ether	1.35	...
Glycerine	1.47	44° 39'	Chloro-form	1.41	...
Turpentine	1.48	...	carbon-di-sulphide	1.63	...
Kerosine oil	1.44	44° 12'	Any gas	1	...

Table IV-Specific resistance and temperature coefficients

Material	Specific resistance (at 0°C)		Temperature coefficient
	Ohm cm	per °C	
Aluminium	2.82 × 10 <sup>-6</sup>		.0039
Copper	1.71 "		.0040
Iron	8.8 "		.0062
Zinc	5.7 "		.0040
Lead	20.9 "		.0043
Platinum	11.0 "		.0037
German silver	16.4 "		.0023
Brass (Cu 70%, Zn 30%)	6.0 "		.0010
Manganin (Cu 84%, Ni 4% and Mn 12%)	44.0 "		.00002
Constantan (Eureka) (Cu 60%, Ni 40%)	49.2 "		.00001
Nichrome (Ni 75%, Fe 12% or W% and Mn 2%)	113 "		.00017

Table-V Velocity of sound

Medium (Gaseous)	Velocity at 0°C	Medium (Liquid)	Velocity at 28°C	Medium (solid)	Velocity at 20°C
Oxygen	316	Water	1447	Aluminium	5100
Hydrogen	1262	Metres/sec	Metres/sec	Iron	5130
Nitrogen	338	Turpen-	"	Steel	4990
Carbon-di-	259	Alcohol	1275	Copper	3560
oxide	"	"	"	Brass	3400
Air	332	Mercury	1047	Glass	5000
Water vapour	401	"	"		"

Table VI-Electro-motive-force (E. M. F.) of cells and their internal resistance

Cell	E. M. F.	Internal Resistance
Daniel cell	1.03 Volts	1 to 5 ohms
Leclanche cell	1.5 "	1 to 5 "
Weston Cadmium cell	1.143 " (at 20°C)	very high (900 ohms)
Bichromate cell	2.0 "	very low
Lead accumulator	2.1 "	0.01 to 0.1 ohms
Edison cell (Ni-Fe cell)	1.4 "	0.01 to 0.1 ohms

VII Electro-chemical equivalents (E. C. E.)

Gold	0006400 gms per coulomb
Silver	0011180 "
Copper	0001295 "
Nickel	0003643 "
Lead	0010731 "
Zinc	0003314 "
Manganese	00021011 "
Oxygen	0024037 "

..... mechanical equivalent of heat

**IX Some useful formulae**

Circumference of a circle

$\pi = \text{Diameter of the circle} (2r)$

Circumference of a circle  $= 2\pi r$

Area of a circle  $= \pi r^2$  ( $r$  = radius)

Surface area of a sphere  $= 4\pi r^2$  ( $r$  = radius)

Area of the curved surface of a cylinder of length l and radius r

$= 2\pi rl$

Volume of a sphere  $= \frac{4}{3} \pi r^3$

Volume of a cylinder  $= \pi r^2 l$

**X Conversion Table**

F. P. S.	C. G. S.	F. P. S.	C. G. S.
1 Inch	$= 2.54$ cm	1 Pound	$= 453.6$ gm
1 Foot	$= 30.48$ cm	1 Ounce	$= 28.35$ gm
1 sq. Inch	$= 6.451$ sq. cm.	1 Poundal	$= 13825$ dynes
1 sq. foot	$= 0.0929$ sq. metre	1 Foot poundal	$= 1.356 \times 10^7$ ergs
1 cubic Inch	$= 16.39$ c. c.	1 Horse power	$= 1.356$ Joules
1 cubic foot	$= 28.32$ Litre	(550 foot pound per second)	$= 746$ watts

## LOGARITHMS

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
0	10	0000	0043	0086	0128	0170					59 13	77 21 26	30 34 38							
11	0414	0453	0492	0531	0569		0212	0253	0294	0334	0374	48 12	66 20 24	25 32 36						
12	0792	0833	0864	0895	0934		0607	0645	0683	0719	0755	47 11	55 18 22	26 39 33						
13	1139	1173	1206	1239	1272		1303	1335	1367	1399	1430	37 11	14 18 21	25 23 32						
14	1462	1492	1523	1553	1584		1614	1644	1673	1703	1732	36 9	13 15 19	22 25 29						
15	1761	1790	1818	1847	1875		1903	1931	1959	1987	2014	36 6	11 14 17	20 23 26						
16	2042	2068	2095	2122	2148		2175	2201	2227	2253	2279	36 8	11 14 17	19 22 25						
17	2304	2330	2355	2380	2405		2430	2455	2480	2504	2529	35 8	10 13 13	13 20 23						
18	2553	2577	2601	2625	2645		2672	2695	2713	2743	2765	25 7	9 12 14	17 19 21						
19	2783	2810	2833	2856	2873		2900	2923	2945	2967	2989	24 6	9 11 13	16 18 20						
20	3010	3032	3054	3075	3096	3118	3139	3160	3181	3201	34 6	8 11 13	15 17 19							
21	3222	3243	3263	3284	3304	3324	3345	3365	3385	3404	34 6	8 10 12	14 16 18							
22	3424	3444	3464	3483	3502	3522	3541	3560	3579	3593	34 6	8 10 12	14 15 17							
23	3617	3636	3655	3674	3692	3711	3729	3747	3766	3784	34 6	7 9 11	15 17 17							
24	3802	3820	3839	3858	3874	3893	3909	3927	3945	3963	34 3	7 9 11	12 14 16							
25	3979	3997	4014	4031	4048	4065	4082	4099	4116	4133	33 5	18 14 15								
26	4150	4166	4183	4200	4216	4232	4249	4265	4281	4298	22 5	7 8 10	11 13 15							
27	4314	4330	4346	4362	4378	4393	4409	4425	4440	4456	13 5	6 8 9	11 13 14							
28	4472	4487	4503	4518	4533	4545	4560	4579	4594	4609	23 5	6 8 9	11 12 14							
29	4624	4639	4654	4669	4683	4698	4713	4729	4744	4757	13 4	6 7 8	10 12 13							
30	4771	4786	4800	4814	4829	4843	4857	4871	4886	4900	13 4	6 7 8	10 11 13							
31	4916	4932	4948	4963	4979	4997	5011	5024	5037	5051	13 4	6 7 8	10 12 12							
32	5051	5065	5079	5092	5105	5119	5133	5145	5159	5172	13 4	5 7 8	9 11 12							
33	5153	5169	5184	5200	5217	5232	5248	5263	5276	5289	13 4	5 6 8	9 10 12							
34	5315	5328	5340	5353	5366	5379	5391	5403	5416	5428	13 4	5 6 8	9 10 12							
35	5411	5433	5453	5473	5490	5503	5514	5527	5539	5551	12 4	3 5 7	9 10 11							
36	5563	5575	5597	5619	5632	5653	5675	5697	5718	5720	13 4	5 6 7	9 10 11							
37	5652	5664	5676	5689	5701	5717	5729	5740	5752	5763	13 3	5 6 7	2 9 10							
38	5708	5720	5733	5743	5755	5766	5777	5789	5799	5801	13 3	4 5 6	2 8 9							
39	5911	5923	5933	5944	5953	5966	5977	5989	5999	6001	13 3	4 5 6	2 8 9							
40	6021	6033	6042	6053	6064	6076	6085	6096	6107	6117	12 3	4 5 6	2 8 9							
41	6125	6137	6147	6160	6170	6180	6191	6202	6212	6222	12 3	4 5 6	2 8 9							
42	6232	6243	6253	6263	6274	6284	6294	6304	6314	6324	12 3	4 5 6	2 8 9							
43	6335	6343	6353	6365	6375	6385	6395	6405	6415	6421	12 3	4 5 6	2 8 9							
44	6435	6444	6454	6464	6474	6484	6493	6503	6513	6523	12 3	4 5 6	2 8 9							
45	6532	6542	6551	6563	6575	6585	6595	6606	6618	6628	12 3	4 5 6	2 8 9							
46	6637	6640	6650	6663	6675	6686	6695	6705	6712	6722	12 3	4 5 6	2 8 9							
47	6738	6739	6740	6743	6745	6747	6749	6751	6753	6755	12 3	4 5 6	2 8 9							
48	6812	6814	6816	6819	6820	6823	6825	6828	6831	6833	12 3	4 5 6	2 8 9							
49	6902	6911	6912	6915	6917	6920	6925	6928	6931	6933	12 3	4 5 6	2 8 9							

## LOGARITHMS

	0	1	2	3	4	5	6	7	8	9	123	168	789
50	6990	6998	7007	7016	7024	7033	7042	7050	7059	7067	123	345	678
51	7076	7084	7093	7101	7110	7118	7126	7135	7143	7152	125	345	678
52	7160	7168	7177	7185	7193	7202	7210	7218	7226	7235	122	345	677
53	7243	7251	7259	7267	7275	7284	7293	7300	7308	7316	122	345	667
54	7324	7332	7340	7348	7356	7364	7372	7380	7388	7396	122	345	667
55	7404	7413	7419	7427	7435	7443	7451	7459	7466	7474	122	345	567
56	7482	7490	7497	7505	7513	7520	7528	7536	7543	7551	122	345	567
57	7559	7566	7574	7582	7589	7597	7604	7612	7619	7627	122	345	567
58	7634	7642	7649	7657	7664	7672	7679	7686	7694	7701	122	344	567
59	7709	7716	7723	7731	7738	7745	7752	7760	7767	7774	122	344	567
60	7782	7789	7796	7803	7810	7813	7815	7822	7829	7836	122	344	566
61	7853	7860	7868	7875	7882	7889	7896	7903	7910	7917	122	344	566
62	7934	7931	7938	7945	7952	7959	7966	7973	7980	7987	122	354	566
63	7993	8000	8007	8014	8021	8028	8035	8041	8048	8055	122	354	556
64	8063	8069	8075	8082	8089	8096	8103	8109	8116	8122	122	354	556
65	8129	8136	8142	8149	8156	8163	8169	8176	8183	8189	122	354	556
66	8195	8203	8209	8215	8223	8230	8235	8241	8248	8254	122	354	556
67	8261	8267	8274	8280	8287	8293	8299	8306	8312	8319	122	354	556
68	8335	8332	8338	8344	8351	8357	8363	8370	8376	8382	122	354	456
69	8393	8393	8401	8407	8414	8420	8426	8432	8439	8445	122	344	456
70	8451	8457	8463	8470	8476	8482	8488	8494	8500	8506	122	354	456
71	8533	8539	8535	8531	8537	8545	8549	8555	8561	8567	122	344	455
72	8573	8579	8585	8591	8597	8603	8609	8615	8621	8627	122	344	465
73	8633	8637	8643	8649	8655	8657	8663	8669	8675	8681	122	354	465
74	8692	8694	8704	8710	8716	8722	8727	8733	8739	8745	122	354	465
75	8751	8756	8762	8768	8774	8779	8785	8791	8797	8802	122	354	455
76	8803	8814	8820	8825	8831	8837	8843	8848	8854	8859	122	354	455
77	8865	8871	8876	8882	8887	8893	8899	8904	8910	8915	122	353	445
78	8921	8927	8933	8938	8943	8949	8954	8960	8965	8971	122	353	445
79	8976	8983	8987	8993	8997	9004	9009	9015	9020	9025	122	353	445
80	9031	9035	9042	9047	9053	9058	9063	9069	9074	9079	122	353	445
81	9085	9090	9096	9101	9106	9112	9117	9122	9128	9133	122	353	445
82	9133	9143	9149	9154	9159	9165	9170	9175	9180	9186	122	353	445
83	9191	9196	9201	9206	9212	9217	9223	9227	9233	9238	122	353	445
84	9243	9243	9253	9258	9263	9269	9274	9279	9284	9289	122	353	445
85	9294	9299	9304	9309	9315	9320	9325	9330	9335	9340	122	353	445
86	9345	9350	9355	9360	9365	9370	9375	9380	9385	9390	122	353	445
87	9375	9400	9405	9410	9415	9420	9425	9430	9435	9440	122	353	344
88	9445	9450	9455	9460	9465	9469	9474	9479	9484	9489	122	353	344
89	9494	9499	9504	9509	9513	9515	9523	9528	9533	9538	122	353	344
90	9542	9547	9552	9557	9562	9566	9571	9576	9581	9586	122	353	344
91	9590	9595	9600	9605	9609	9614	9619	9624	9629	9634	122	353	344
92	9635	9643	9647	9651	9657	9662	9666	9671	9675	9680	122	353	344
93	9685	9689	9694	9699	9703	9708	9713	9717	9722	9727	122	353	344
94	9731	9736	9741	9745	9750	9754	9759	9763	9768	9773	122	353	344
95	9777	9782	9786	9791	9795	9800	9805	9809	9814	9818	122	353	344
96	9821	9827	9833	9836	9841	9845	9850	9854	9859	9863	122	353	344
97	9863	9873	9877	9881	9885	9889	9894	9897	9901	9905	122	353	344
98	9912	9917	9921	9926	9930	9934	9939	9943	9948	9953	122	353	344
99	9956	9961	9965	9969	9974	9978	9983	9987	9991	9996	122	353	344

## ANTilogarithms

	0	1	2	3	4	5	6	7	8	9	
00	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000
01	0043	0043	0043	0043	0043	0043	0043	0043	0043	0043	0043
02	0141	0141	0141	0141	0141	0141	0141	0141	0141	0141	0141
03	0243	0243	0243	0243	0243	0243	0243	0243	0243	0243	0243
04	0348	0348	0348	0348	0348	0348	0348	0348	0348	0348	0348
05	0443	0443	0443	0443	0443	0443	0443	0443	0443	0443	0443
06	0544	0544	0544	0544	0544	0544	0544	0544	0544	0544	0544
07	0642	0642	0642	0642	0642	0642	0642	0642	0642	0642	0642
08	0740	0740	0740	0740	0740	0740	0740	0740	0740	0740	0740
09	0839	0839	0839	0839	0839	0839	0839	0839	0839	0839	0839
10	0937	0937	0937	0937	0937	0937	0937	0937	0937	0937	0937
11	1035	1035	1035	1035	1035	1035	1035	1035	1035	1035	1035
12	1133	1133	1133	1133	1133	1133	1133	1133	1133	1133	1133
13	1232	1232	1232	1232	1232	1232	1232	1232	1232	1232	1232
14	1330	1330	1330	1330	1330	1330	1330	1330	1330	1330	1330
15	1428	1428	1428	1428	1428	1428	1428	1428	1428	1428	1428
16	1445	1445	1445	1445	1445	1445	1445	1445	1445	1445	1445
17	1479	1479	1479	1479	1479	1479	1479	1479	1479	1479	1479
18	1514	1514	1514	1514	1514	1514	1514	1514	1514	1514	1514
19	1549	1549	1549	1549	1549	1549	1549	1549	1549	1549	1549
20	1595	1595	1595	1595	1595	1595	1595	1595	1595	1595	1595
21	1629	1629	1629	1629	1629	1629	1629	1629	1629	1629	1629
22	1663	1663	1663	1663	1663	1663	1663	1663	1663	1663	1663
23	1697	1697	1697	1697	1697	1697	1697	1697	1697	1697	1697
24	1738	1738	1738	1738	1738	1738	1738	1738	1738	1738	1738
25	1778	1778	1778	1778	1778	1778	1778	1778	1778	1778	1778
26	1820	1820	1820	1820	1820	1820	1820	1820	1820	1820	1820
27	1861	1861	1861	1861	1861	1861	1861	1861	1861	1861	1861
28	1905	1905	1905	1905	1905	1905	1905	1905	1905	1905	1905
29	1950	1950	1950	1950	1950	1950	1950	1950	1950	1950	1950
30	1995	2000	2000	2000	2000	2000	2000	2000	2000	2000	2000
31	2042	2046	2051	2056	2061	2065	2070	2075	2080	2084	2088
32	2080	2094	2099	2104	2109	2113	2118	2123	2128	2133	2138
33	2138	2143	2147	2153	2158	2163	2168	2173	2178	2183	2188
34	2185	2193	2198	2203	2208	2213	2218	2223	2228	2233	2238
35	2239	2244	2249	2254	2259	2265	2270	2275	2280	2285	2290
36	2291	2296	2301	2307	2312	2317	2323	2328	2333	2339	2344
37	2344	2350	2355	2360	2366	2371	2377	2383	2389	2395	2400
38	2399	2404	2410	2415	2421	2427	2432	2438	2443	2449	2455
39	2455	2460	2466	2472	2477	2483	2489	2495	2500	2506	2512
40	2513	2518	2523	2529	2535	2541	2547	2553	2559	2564	2570
41	2570	2576	2582	2588	2594	2600	2606	2612	2618	2624	2630
42	2630	2636	2642	2649	2655	2661	2667	2673	2679	2685	2691
43	2692	2698	2704	2710	2716	2722	2728	2735	2742	2748	2754
44	2754	2760	2767	2773	2780	2786	2793	2799	2805	2811	2817
45	2818	2825	2831	2838	2844	2851	2858	2864	2871	2877	2883
46	2884	2891	2897	2904	2911	2917	2924	2931	2938	2944	2950
47	2951	2958	2965	2972	2979	2985	2992	2999	3006	3013	3020
48	3020	3027	3034	3041	3048	3055	3062	3069	3076	3083	3090
49	3090	3097	3105	3112	3119	3126	3133	3141	3148	3155	3162

## ANTILOGARITHMS

0	1	2	3	4	5	6	7	8	9	-1	123	4	5	6	7	8	9	
0	3162	3170	3177	3184	3192	3199	3206	3214	3222	3228	3232	3	4	4	5	6	7	
1	3236	3243	3251	3258	3265	3273	3281	3289	3296	3304	3312	3	4	5	5	6	7	
2	3311	3319	3327	3334	3342	3350	3357	3365	3373	3381	3389	3	4	5	5	6	7	
3	3385	3393	3401	3409	3417	3425	3433	3441	3449	3457	3465	3	4	5	6	6	7	
4	3467	3475	3483	3491	3499	3507	3515	3524	3532	3540	3548	3	4	5	6	6	7	
5	3548	3556	3563	3571	3579	3587	3595	3603	3611	3619	3627	3	4	5	6	7	7	
6	3631	3639	3647	3655	3663	3671	3679	3687	3695	3703	3711	3	4	5	6	7	8	
7	3715	3724	3733	3741	3750	3758	3767	3776	3784	3793	3802	3	4	5	6	7	8	
8	3802	3811	3819	3828	3837	3845	3853	3861	3873	3883	3892	3	4	5	6	7	8	
9	3890	3899	3908	3917	3925	3933	3941	3949	3958	3963	3972	3	4	5	5	6	7	
0	3971	3980	3989	3997	4005	4013	4021	4029	4036	4045	4053	4064	3	4	5	6	7	8
1	4074	4083	4091	4099	4107	4115	4123	4130	4140	4150	4159	4167	3	4	5	6	7	8
2	4159	4178	4186	4193	4207	4217	4227	4236	4246	4256	4265	4273	3	4	5	6	7	8
3	4266	4275	4283	4291	4305	4315	4325	4335	4345	4355	4365	4373	3	4	5	6	7	8
4	4375	4385	4395	4406	4416	4426	4436	4446	4456	4467	4477	4485	3	4	5	6	7	8
5	4497	4517	4527	4535	4543	4551	4559	4567	4575	4583	4590	4598	4606	4	5	6	7	8
6	4571	4581	4592	4603	4613	4624	4634	4643	4653	4663	4673	4683	4693	4	5	6	7	9
7	4677	4685	4699	4710	4721	4732	4744	4753	4764	4775	4785	4795	4805	4	5	6	7	9
8	4786	4797	4805	4819	4831	4842	4853	4864	4875	4887	4897	4909	4920	4	5	6	7	9
9	4909	4920	4932	4943	4953	4960	4977	4987	4999	5000	5003	5005	5007	5	6	7	8	9
0	5012	5023	5035	5047	5058	5070	5082	5093	5105	5117	5129	5141	5153	5165	5177	5189	5191	
1	5129	5140	5152	5164	5176	5188	5200	5212	5224	5236	5248	5260	5272	5284	5296	5308	5310	
2	5245	5260	5272	5284	5297	5309	5321	5333	5340	5353	5365	5377	5389	5396	5408	5415	5422	
3	5370	5383	5395	5403	5410	5413	5445	5458	5470	5483	5495	5508	5515	5528	5535	5542	5550	
4	5495	5508	5521	5534	5540	5559	5572	5585	5600	5610	5618	5630	5645	5658	5671	5684	5692	
5	5643	5656	5669	5682	5695	5707	5719	5731	5743	5755	5767	5779	5791	5803	5815	5827	5839	
6	5754	5768	5781	5794	5803	5812	5824	5836	5848	5860	5872	5884	5896	5908	5920	5932	5944	
7	5858	5902	5916	5929	5943	5957	5970	5984	5993	6012	6024	6036	6048	6060	6072	6084	6096	
8	6026	6030	6053	6067	6081	6095	6109	6124	6133	6152	6171	6188	6207	6226	6245	6264	6283	
9	6160	6160	6164	6209	6223	6237	6252	6266	6281	6295	6314	6326	6345	6364	6383	6402	6421	
0	6310	6324	6330	6353	6368	6383	6397	6412	6427	6442	6458	6474	6488	6494	6504	6517	6525	
1	6457	6471	6486	6501	6516	6531	6546	6561	6577	6592	6607	6622	6638	6653	6669	6684	6694	
2	6607	6612	6637	6653	6668	6683	6699	6714	6730	6745	6761	6776	6791	6806	6821	6836	6844	
3	6761	6776	6792	6808	6823	6838	6853	6868	6881	6897	6912	6928	6943	6958	6973	6984	6994	
4	6913	6934	6950	6966	6983	6995	7015	7031	7047	7063	7079	7095	7110	7125	7140	7153	7165	
5	7070	7096	7112	7129	7145	7161	7178	7194	7210	7225	7245	7255	7270	7284	7298	7312	7325	
6	7244	7261	7278	7295	7311	7328	7345	7363	7379	7396	7413	7427	7442	7456	7471	7485	7498	
7	7413	7430	7447	7463	7482	7499	7516	7534	7551	7568	7585	7602	7619	7636	7653	7670	7686	
8	7550	7603	7621	7641	7658	7674	7691	7709	7727	7745	7763	7781	7801	7818	7836	7854	7872	
9	7762	7780	7798	7816	7834	7852	7870	7889	7907	7923	7941	7959	7977	7995	8013	8031	8049	
0	7943	7962	7980	7993	8017	8033	8054	8072	8093	8110	8130	8146	8163	8181	8198	8215	8232	
1	8128	8147	8166	8185	8204	8223	8241	8260	8279	8299	8316	8334	8351	8368	8385	8402	8419	
2	8318	8337	8356	8375	8395	8414	8433	8453	8473	8492	8512	8532	8552	8572	8592	8612	8632	
3	8511	8531	8551	8570	8590	8610	8630	8650	8670	8690	8710	8730	8750	8770	8790	8810	8830	
4	8710	8730	8750	8770	8790	8810	8830	8850	8870	8890	8910	8930	8950	8970	8990	9010	9030	
5	8913	8933	8954	8974	8993	9010	9030	9057	9078	9099	9120	9140	9160	9180	9200	9220	9240	
6	9120	9141	9162	9183	9204	9225	9247	9268	9290	9312	9334	9356	9379	9399	9421	9443	9465	
7	9333	9354	9376	9397	9410	9431	9453	9474	9496	9515	9537	9557	9579	9599	9621	9643	9665	
8	9550	9572	9594	9616	9639	9661	9681	9703	9727	9750	9774	9797	9821	9843	9865	9887	9909	
9	9773	9795	9817	9840	9863	9886	9908	9932	9954	9977	9997	9999	9999	9999	9999	9999	9999	











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